Determination of mode I and II adhesion toughness of monolayer thin films by circular blister tests

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Abstract

Mechanical models are developed to determine the mode I and II adhesion toughness of monolayer thin films using circular blister tests under either pressure load or point load. The interface fracture of monolayer thin film blisters is mode I dominant for linear bending with small deflection while it is mode II dominant for membrane stretching with large deflection. By taking the advantage of the large mode mixity difference between these two limiting cases, the mode I and II adhesion toughness are determined in conjunction with a linear failure criterion. Thin films under membrane stretching have larger adhesion toughness than thicker films under bending. Experimental results demonstrate the validity of the method.

Keywords: adhesion toughness, circular blisters, energy release rate, interface fracture, thin films

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Nomenclature	
h	thickness of film
p	pressure load
E	Young's modulus of film
G , $G_{\rm I}$, $G_{\rm II}$	total, mode I and mode II ERRs
$G_{ m Ic}$, $G_{ m IIc}$	pure mode I and II interface adhesion toughness
$G_{ m c}$	interface adhesion toughness
$G_{ m J}$	Jensen's component in total ERR
$G_{ m s}$	through-thickness shearing ERR
$M_{ m B}$	crack tip radial bending moment
$N_{ m B}$	crack tip in-plane force
Р	central point load
$P_{ m B}$	crack tip through-thickness shear force
$R_{ m B}$	blister radius
δ	blister central deflection
η	ratio of through-thickness shearing ERR and Jensen's ERR
ρ	mode mixity ratio of pure mode II to mode I.
V	Poisson's ratio of film
Abbreviation	
ERR	Energy release rate

1. Introduction

Thin solid films are found in many different applications fulfilling various roles [1,2] such as confinement of electric charge in integrated electronic circuits, in thermal insulation like in thermal barrier coatings (TBCs), and in surface coatings that protect against corrosion, friction and wear. Although thin films are not usually expected to have a primary load-carrying capability, their adhesion toughness is still a major concern in engineering applications due to various factors such as buckling [3–9] or pockets of energy concentration [10–15], which can cause delamination and then often, loss of function.

Several tests to determine the adhesion toughness of a film to its substrate have been developed over the past century, for example, peeling tests [16,17], indentation tests [18], scratching tests [19], and blister tests [20–22]. Blister tests are widely applied in the fields of microelectronics and coatings. The first blister test was reported by Dannenberg in 1961 [20], which was further developed by Jensen [21,22]. In addition, multiple theoretical models have

been developed [23–25] to correlate the adhesion toughness of thin films with the blister morphology that is induced by either a pressure load or a point load. Films, such as graphene, and substrates with various material properties and thickness are employed in the blister tests; therefore, mechanical models are needed for the limits of membrane stretching with large deflections, linear bending with small deflections, and the transition between these limits, in order to derive a film's adhesion toughness. Furthermore, adhesion toughness is influenced by through-thickness shearing and film sliding [26] and its effect on mode mixity. This gives the idea of the present work: By taking advantage of the large difference in mode mixity between cases of linear bending with small deflections, and membrane stretching with large deflections, the mode I and II adhesion toughnesses can be determined.

The present work aims to develop mechanical models to determine the mode I and II adhesion toughness of thin films by using circular blister tests. A mechanical model for circular blisters under a pressure load is developed in Section 2 while a mechanical model for circular blisters under a point load is developed in Section 3. The developed models are assessed with experimental results [27] in Section 4. Conclusions are drawn in Section 5.

2. Analytical mechanical model for the circular blister test with a pressure load

In this section, a mechanical model is developed to determine the mode I and II adhesion toughness between thin films and thick substrates by using the circular blister test with a pressure load. Figure 1 shows a circular blister under pressure p. The blister radius is R_B with the subscript B denoting the blister tip, and the central deflection is represented by δ . The thickness of the film h is much smaller than the thickness of the substrate, and the substrate is therefore assumed to have negligible global deformation due to the film deformation. Both the film and substrate materials are assumed to be homogeneous and isotropic. The film material has Young's modulus E and Poisson's ratio ν . The development here includes both linear bending for small deflection and membrane stretching for large deflection. These two cases are often used in experimental tests [27–29] to determine adhesion toughness of thin films.



Fig. 1. A circular blister test with a thin film under a pressure load on a thick substrate.

Based on 2D elasticity partition theories [26,30–32], the mode I and II energy release rates (ERRs) can be written in the following forms:

$$G_{\rm I} = 0.6227 \times \frac{6}{Eh^3} \left(1 - \nu^2 \right) \left(M_{\rm B} - \frac{N_{\rm B}h}{4.450} + \frac{P_{\rm B}h}{1.0063} \right)^2 \tag{1}$$

$$G_{\rm II} = 0.3773 \times \frac{6}{Eh^3} \left(1 - \nu^2 \left(M_{\rm B} + \frac{N_{\rm B}h}{2.697} \right)^2 \right)$$
(2)

The loads at the crack tip in the thin film are the bending moment $M_{\rm B}$ (Nm/m), the in-plane force $N_{\rm B}$ (N/m), and the through-thickness shear force $P_{\rm B}$ (N/m). They take different values in linear bending for small deflection and membrane stretching for large deflection; hence, the mode mixity, $G_{\rm II}/G_{\rm I}$ or ρ , also takes different values.

2.1. Linear bending mechanical model for small deflection

For small deflections within the linear range, the crack tip loads in Eqs. (1) and (2) are [5–7]

$$M_{\rm Bb} = \frac{1}{8} p R_{\rm B}^2, \ N_{\rm Bb} = 0 \text{ and } P_{\rm Bb} = \frac{1}{2} p R_{\rm B}$$
 (3)

The subscript b denotes bending with small deflections. The deflection δ_{b} at the centre of the blister is

$$\delta_{\rm b} = \frac{3}{16} \frac{(1 - \nu^2) p R_{\rm B}^4}{Eh^3} \tag{4}$$

Substituting Eqs. (3) and (4) into Eqs. (1) and (2) gives

$$G_{\rm I} = 0.6227 \times \frac{1}{2} p \delta_{\rm b} (1+\lambda)^2 \tag{5}$$

$$G_{\rm II} = 0.3773 \times \frac{1}{2} p \delta_{\rm b} \tag{6}$$

where

$$\lambda = \frac{P_{\rm Bb}h}{1.0063M_{\rm Bb}} = \frac{4h}{1.0063R_{\rm B}} \tag{7}$$

which represents the through-thickness shear effect. By combining Eqs. (5) and (6), the total ERR can be expressed as

$$G = G_{\rm s} + G_{\rm J} = G_{\rm J} (1+\eta) \tag{8}$$

in which

$$G_{\rm J} = \frac{1}{2} p \delta_{\rm b} \tag{9}$$

$$\eta = \frac{G_{\rm s}}{G_{\rm J}} = 0.6227\lambda(2+\lambda) \tag{10}$$

The ERR component G_J is from Jensen's work [5–7], which does not account for throughthickness shear. The additional ERR contribution from the crack tip through-thickness shear force $P_{\rm Bb}$ is the ERR component $G_{\rm S}$, which is related to G_J through the ratio η .

The mode mixity $\rho = G_{II}/G_{I}$ is readily obtained as

$$\rho = \frac{G_{\rm II}}{G_{\rm I}} = 0.6059 \frac{1}{\left(1 + \lambda\right)^2} \tag{11}$$

It is seen that the effect of through-thickness shear is to decrease the mode mixity and consequently to reduce the adhesion toughness. Figure 2a shows the variation of mode mixity ρ with respect to $R_{\rm B}/h$, which, as per Eq. (7), is effectively λ . The mode mixity approaches zero (pure mode I) for small $R_{\rm B}/h$ (or large λ), and it decreases with increasing film thickness and approaches 0.6059 for large $R_{\rm B}/h$ (or small λ).



Fig. 2. Variation of mode mixity ρ with respect to $R_{\rm B}/h$ for linear bending under point or pressure loads (a), and for membrane stretching under point or pressure loads (b).

The linear failure criterion, shown in Eq. (12), can be used to derive the mode I and II adhesion toughness G_{Ic} and G_{IIc} . The linear failure criterion is an accurate failure criterion for interfaces with low adhesion toughness [10–13,26,33,34].

$$\frac{G_{\rm I}}{G_{\rm Ic}} + \frac{G_{\rm II}}{G_{\rm IIc}} = 1 \tag{12}$$

For any given mode mixity ρ , the corresponding adhesion toughness G_c can be obtained as the following by combining Eq. (12) with $G_c = G = G_I + G_{II}$:

$$G_{\rm c} = \frac{(1+\rho)G_{\rm Ic}G_{\rm IIc}}{\rho G_{\rm Ic} + G_{\rm IIc}}$$
(13)

By choosing two values of $R_{\rm B}/h$ with the corresponding mode mixities ρ_1 and ρ_2 , and the measured adhesion toughness $G_{\rm c1}$ and $G_{\rm c2}$, the mode I and II adhesion toughness $G_{\rm Ic}$ and $G_{\rm Ic}$ can be determined from Eq. (13) as

$$G_{\rm Ic} = \frac{G_{c1}G_{c2}(\rho_1 - \rho_2)}{\rho_1 G_{c1}(1 + \rho_2) - \rho_2 G_{c2}(1 + \rho_1)}$$
(14)

$$G_{\rm IIc} = \frac{G_{\rm c1}G_{\rm c2}(\rho_1 - \rho_2)}{G_{\rm c2}(1 + \rho_1) - G_{\rm c1}(1 + \rho_2)}$$
(15)

To obtain accurate predictions of $G_{\rm Ic}$ and $G_{\rm IIc}$ from Eqs. (14) and (15), it is better to use a large mode mixity difference $(\rho_1 - \rho_2)$. This can be achieved by choosing a small value of $R_{\rm B}/h$ for ρ_1 , and a large value of $R_{\rm B}/h$ for ρ_2 . The fracture resistance curve can be

obtained based on Eqs. (4), and (7) to (10). It is found that G_{c1} can be expressed by a higherorder polynomial function in terms of $R_{\rm B}/h$, hence the adhesion toughness maybe unreliable for small experimental values of $R_{\rm B}/h$. To overcome this difficulty, an alternative method is developed next.

2.2. Membrane stretching mechanical model for large deflection

At the limit of membrane stretching, the crack tip loads in Eqs. (1) and (2) for the circular blister of radius $R_{\rm B}$ under pressure load p become [5–7]

$$M_{\rm Bm} = \frac{h}{4} \frac{\left(Ehp^2 R_{\rm B}^2\right)^{1/3}}{\left[3(1-\nu^2)\varphi(\nu)\right]^{1/2}}$$
(16)

$$N_{\rm Bm} = \left(Ehp^2 R_{\rm B}^2\right)^{1/3} \varphi(\nu) \tag{17}$$

$$P_{\rm Bm} = \frac{1}{2} p R_{\rm B} \tag{18}$$

The subscript m denotes the membrane limit case and the parameter $\varphi(v)$ is

$$\varphi(\nu) = \frac{(1.078 + 0.636\nu)^{2/3}}{2[6(1-\nu^2)]^{1/3}}$$
(19)

The deflection $\, \delta_{\rm m} \,$ at the centre of the blister is

$$\delta_{\rm m} = f\left(\nu\right) \left(\frac{pR_{\rm B}^4}{Eh}\right)^{1/3} \tag{20}$$

with

$$f(\nu) = 0.9635 \left[\frac{3(1-\nu)}{7-\nu} \right]^{1/3}$$
(21)

The mode I and II energy release rates (ERRs) can then be obtained [26,30–32] as follows:

$$G_{\rm I} = 0.6227 \times \frac{p\delta_{\rm m}}{8} \frac{\left(0.7578 - 0.1429\nu\right)^2}{\varphi(\nu)f(\nu)} \tag{22}$$

$$G_{\rm II} = 0.3773 \times \frac{p\delta_{\rm m}}{8} \frac{(1.400 + 0.2358\nu)^2}{\varphi(\nu)f(\nu)}$$
(23)

The effect of the through-thickness shear force $P_{\rm B}$ in Eq. (1) disappears at the membrane stretching limit. Note, however, that in the case of multilayer membranes, interlayer sliding can activate the effect again and this results in extra mode I ERR contribution. This has been considered in detail in a study on the adhesion toughness of multilayer graphene membranes using circular blister tests [26]. Excellent agreement on adhesion toughness was observed in that study [26] between predictions from the mechanical model and experimental results. In the present work, only monolayer membranes are considered. From Eqs. (20), (22) and (23), the total ERR is

$$G = \zeta(\nu) \frac{p\delta_{\rm m}}{f(\nu)} \tag{24}$$

in which the parameter ζ is

$$\zeta(\nu) = \frac{1}{8\varphi(\nu)} + \frac{(1-\nu^2)\varphi(\nu)^2}{2}$$
(25)

The mode mixity $\rho = G_{II}/G_{I}$ is obtained from Eqs. (22) and (23) as

$$\rho = 0.6059 \left(\frac{1.400 + 0.2358\nu}{0.7578 - 0.1429\nu} \right)^2 \tag{26}$$

It varies from 2.0680 for v = 0 to 2.9634 for v = 0.5, and remains constant during radial growth. It is shown in Fig. 2b as the dark shaded area. The adhesion toughness G_c therefore remains constant with mode II dominant, and consequently it is expected to be larger than the adhesion toughness of films under linear bending.

Equations (14) and (15) cannot be applied here to determine G_{Ic} and G_{IIc} when using the membrane mechanical model alone; however, when used in conjunction with the linear bending model, more accurate predictions for G_{Ic} and G_{IIc} can be determined than from using just the linear bending model alone. Eqs. (14) and (15) now change to be

$$G_{\rm Ic} = \frac{G_{\rm cb}G_{\rm cm}(\rho_{\rm b} - \rho_{\rm m})}{\rho_{\rm b}G_{\rm cb}(1 + \rho_{\rm m}) - \rho_{\rm m}G_{\rm cm}(1 + \rho_{\rm b})}$$
(27)

$$G_{\rm IIc} = \frac{G_{\rm cb}G_{\rm cm}(\rho_{\rm b} - \rho_{\rm m})}{G_{\rm cm}(1 + \rho_{\rm b}) - G_{\rm cb}(1 + \rho_{\rm m})}$$
(28)

The improved accuracy comes from the fact that the linear bending model is mode I dominant while the membrane stretching model is mode II dominant.

3. Analytical mechanical model for the circular blister test with a point load

3.1. Linear bending mechanical model for small deflection

Figure 3 shows a circular blister of radius $R_{\rm B}$ under a central point load P.



Fig. 3. A circular blister test with a thin film under a central point load on a thick substrate. For small deflections within the linear range, the crack tip loads in Eq. (1) are [5–7]

$$M_{\rm Bb} = \frac{P}{4\pi}, \ N_{\rm Bb} = 0 \text{ and } P_{\rm Bb} = \frac{P}{2\pi R_{\rm B}}$$
 (29)

The deflection $\,\delta_{\rm b}\,$ at the centre of the blister is

$$\delta_{\rm b} = \frac{3}{4} \frac{(1 - \nu^2) P R_{\rm B}^2}{\pi E h^3}$$
(30)

Substituting Eqs. (29) and (30) into Eqs. (1) and (2) gives

$$G_{\rm I} = 0.6227 \times \frac{1}{2} \frac{P}{\pi R_{\rm B}^2} \delta_{\rm b} (1+\lambda)^2$$
(31)

$$G_{\rm II} = 0.3773 \times \frac{1}{2} \frac{P}{\pi R_{\rm B}^2} \delta_{\rm b}$$
(32)

where

$$\lambda = \frac{P_{\rm Bb}h}{1.0063M_{\rm Bb}} = \frac{2h}{1.0063R_{\rm B}}$$
(33)

Note that Eqs. (31) and (32) can be directly obtained from Eqs. (5) and (6) by replacing pressure load p with $P/(\pi R_B^2)$. The mode mixity ρ has the same expression as Eq. (11), but with parameter λ given by Eq. (33). Its variation with respect to R_B/h is also shown in Fig. 2a. Again, it is seen that the through-thickness shear effect is to decrease the mode mixity and reduce the adhesion toughness. It is also mode I dominant.

3.2. Membrane stretching mechanical model for large deflection

The mechanical model in the point load case is very similar to the model developed above for pressure load. Some essential formulae are recorded here. The parameter $\varphi(v)$ becomes

$$\varphi(\nu) = 0.382\nu^3 + 0.013\nu^2 + 0.248\nu + 0.422 \tag{34}$$

The function f(v) now becomes

$$f(v) = 1/[2\varphi(v)] + 2\varphi^{2}(v)(1-v^{2})$$
(35)

The pressure load p can now be replaced everywhere with $P/(\pi R_B^2)$. The mode I and II ERRs can be obtained [26] as

$$G_{\rm I} = 0.6227 \times \frac{P\delta}{8\pi R_{\rm B}^2} \frac{\left[1 - 1.557\sqrt{\left(1 - v^2\right)}\varphi(v)^3}\right]^2}{\varphi(v)f(v)}$$
(36)

$$G_{\rm II} = 0.3773 \times \frac{P\delta}{8\pi R_{\rm B}^2} \frac{\left[1 + 2.569\sqrt{\left(1 - v^2\right)}\varphi(v)^3\right]^2}{\varphi(v)f(v)}$$
(37)

The mode mixity is then

$$\rho = 0.6059 \left[\frac{1 + 2.569 \sqrt{(1 - v^2)} \varphi(v)^3}{1 - 1.557 \sqrt{(1 - v^2)} \varphi(v)^3} \right]^2$$
(38)

The mode mixity varies from 5.3568 for v = 0 to 17.4090 for v = 0.5. Again, it is constant and mode II dominant. It is also shown in Fig. 2b as the light shaded area. Similarly, $G_{\rm Ic}$ and $G_{\rm IIc}$ can be determined by using Eqs. (27) and (28).

4. Experimental validation

In this section, the mechanical models developed above are assessed using the experimental results in Ref. [27]. Two groups of experimental results are reported in Ref. [27]. In both groups, the substrate was copper with a thickness of 80 μ m. Each film was transferred to the copper substrate and suspended over a 3 mm-diameter hole. Pressurisation was achieved by pumping deionised water through the hole, resulting in a pressure-blister deflection response and blister growth. The blister deflection and blister radius were measured simultaneously using two microscopes with synchronised cameras, positioned horizontally and vertically respectively.

In the first group, photoresist films are tested under a pressure load at three different thicknesses, namely $h = 10 \,\mu\text{m}$, 31 μm and 60 μm . The photoresist films have a Young's modulus of E = 3.6 GPa and a Poisson's ration of v = 0.35. Although the thickness of the substrate is not much larger than the thickness of the film, the Young's modulus of copper is in the region of 128 GPa which is much larger than that of the photoresist films. Therefore, the present thin film models are still applicable. Predictions of adhesion toughness, based on the analytical models for various film thicknesses, are summarised in Table 1, in which the predicted value for adhesion toughness (based on the calculated mode I and II adhesion toughness values) for thickness $h = 31 \,\mu\text{m}$ is shown in brackets.

Table 1. Analytical predictions of the adhesion toughness for various photoresist film thicknesses on a copper substrate.

Thickness (µm)	Mode mixity	Measured adhesion toughness (J m ⁻²)	Mode I toughness (J m ⁻²)	Mode II toughness (J m ⁻²)
10	2.6583 Eq. (26)	0.3487 Eq. (24)		
31	0.5189 Eq. (11)	0.2827 Eq. (8) (0.2845 Eq. 13)	0.2446 Eq. (27)	0.4152 Eq. (28)
60	0.4535 Eq. (11)	0.2805 Eq. (8)		

The experimental results reported in Ref. [27] show that the films with the thickness of $h = 10 \ \mu\text{m}$ behave in the manner of membrane stretching. The measured adhesion toughness $G_{\rm cm}$ based on Eq. (24) is $G_{\rm cm} = 0.3487 \ \text{Jm}^{-2}$. Note that this value is 1.1285 times greater than the value reported in Ref. [27] because of the difference between Cao et al.'s formula to calculate *G* and Eq. (24). The mode mixity $\rho_{\rm m}$ from Eq. (26) is $\rho_{\rm m} = 2.6583$. The experimental results also show that the films with the thicknesses of $h = 31 \ \mu\text{m}$ and 60 $\ \mu\text{m}$ behave in the manner of linear bending. From Eq. (8), the steady-state adhesion toughness $G_{\rm cb}$ at blister radius $R_{\rm B} = 1530 \ \mu\text{m}$ are $G_{\rm cb} = 0.2827 \ \text{Jm}^{-2}$ and $0.2805 \ \text{Jm}^{-2}$ respectively. Note that the values reported in Ref. [27] for the films with the thicknesses of $h = 31 \ \mu\text{m}$ and 60 $\ \mu\text{m}$ correspond to $G_{\rm J}$ in this work. The respective mode mixities $\rho_{\rm b}$ from Eq. (11) are $\rho_{\rm b} = 0.5189$ and 0.4535. Now substituting the results, $G_{\rm cm} = 0.3487 \ \text{Jm}^{-2}$, $\rho_{\rm m} = 2.6583$ for the linear bending film of thickness $h = 10 \ \mu\text{m}$, and $G_{\rm cb} = 0.2805 \ \text{Jm}^{-2}$, $\rho_{\rm b} = 0.4535$ for the linear bending film of thickness $h = 60 \ \mu\text{m}$ into Eqs. (27) and (28), the mode I and II adhesion toughness are determined to be $G_{\rm Ic} = 0.2446 \ \text{Jm}^{-2}$ and $G_{\rm Ic} = 0.4152 \ \text{Jm}^{-2}$. To examine the accuracy of these values, the adhesion toughness of the film with the thickness

of $h = 31 \,\mu\text{m}$ is now calculated analytically using Eq. (13). Substituting $G_{\text{Ic}} = 0.2446 \,\text{J m}^{-2}$, $G_{\text{IIc}} = 0.4152 \,\text{J m}^{-2}$ and $\rho = \rho_{\text{b}} = 0.5189$ for the film with thickness of $h = 31 \,\mu\text{m}$ into Eq. (13) gives $G_{\text{c}} = 0.2845 \,\text{J m}^{-2}$, which is in excellent agreement with the test result of $G_{\text{cb}} = 0.2827 \,\text{J m}^{-2}$.



Fig. 4. Variation of adhesion toughness G_c at the photoresist/copper interface with respect to R_B/h under the four test conditions.

Figure 4 shows the variation of the adhesion toughness G_c with respect to R_B/h under the four test conditions, namely, linear bending and membrane stretching under pressure and point loading conditions. The adhesion toughness G_c approaches G_{Ic} for small R_B/h and approaches $G_c = 1.6059G_{Ic}G_{IIc}/(0.6059G_{Ic} + G_{IIc})$ for large R_B/h for linear bending with both pressure and point loading, as seen from Eqs. (11) and (13). It is interesting to note that thicker films have smaller adhesion toughness. Also, note that the two curves under linear bending conditions appear similar to the usual fracture resistance curve, but they have different meanings: Here, the variation of adhesion toughness is due to the changing mode mixity with the mode I and II adhesion toughness G_{Ic} and G_{IIc} remaining constant. In the fracture resistance curve, however, the variation is due to nonlinear behaviour like ductile fracture, in which there is a plastic zone at the crack tip which increases in size with crack extension; or in fibre-reinforced materials it can be caused by fibre-bridging. The fracture resistance curve results from the increasing mode I and II adhesion toughness G_{Ic} and G_{IIc} with crack extension rather than from the changing mode mixity. In contrast, for membrane stretching conditions, the adhesion toughness G_c remains constant with respect to R_B/h under both pressure and point loading conditions due to the constant mode mixity, as shown in Eqs. (26) and (38) respectively. Since mode II is dominant, G_c is always larger than for linear bending test conditions, for which mode I is dominant.

In the second group of test results, monolayer graphene is sandwiched by the same copper substrate and the photoresist film as used in the first group of tests. The thickness of the monolayer graphene is about 0.347 nm [26]. Even taking into account the large Young's modulus of graphene at about 1000 GPa, its effective thickness is still much smaller than the thickness of the photoresist films and it is therefore ignored in the present work. The addition of the graphene layer, however, changes the adhesion toughness of the photoresist film. Predictions of adhesion toughness, based on the analytical models for various film thicknesses, are summarised in Table 2, in which the predicted value for adhesion toughness (based on the calculated mode I and II adhesion toughness values) for thickness $h = 31 \,\mu\text{m}$ is shown in brackets.

Table 2. Analytical predictions of the adhesion toughness for various thicknesses of a monolayer graphene/photoresist sandwich film on a copper substrate.

Thickness (µm)	Mode mixity	Measured adhesion toughness $(J m^{-2})$	Mode I toughness (J m ⁻²)	Mode II toughness (J m ⁻²)
10	2.6583 Eq. (26)	0.4435 Eq. (24)		
31	0.5189 Eq. (11)	0.3711 Eq. (8) (0.3710 Eq. 13)	0.3240 Eq. (27)	0.5149 Eq. (28)
60	0.4535 Eq. (11)	0.3664 Eq. (8)		
60	0.4535 Eq. (11)	0.3664 Eq. (8)		

Again, the experimental results reported in Ref. [27] show that the films with the thickness of $h = 10 \,\mu\text{m}$ behave in the manner of membrane stretching. The measured adhesion toughness $G_{\rm cm}$ based on Eq. (24) is $G_{\rm cm} = 0.4435 \,\text{J m}^{-2}$. Note that this value is 1.1285 times greater than the value reported in Ref. [27] because of the difference between Cao et al.'s formula to calculate G and Eq. (24). The mode mixity $\rho_{\rm m}$ from Eq. (26) is $\rho_{\rm m} = 2.6583$. Also, the experimental results show that the films with thicknesses of $h = 31 \,\mu\text{m}$ and 60 μm behave in the manner of linear bending. From Eq. (8), the steady-state adhesion toughness $G_{\rm cb}$ at blister radius $R_{\rm B} = 1530 \,\mu\text{m}$ are $G_{\rm cb} = 0.3711 \,\text{J m}^{-2}$ and 0.3664 J m⁻² respectively. Note that the values reported in Ref. [27] for the films with the thicknesses of $h = 31 \,\mu\text{m}$ and 60 µm correspond to $G_{\rm J}$ in this work. The respective mode mixities $\rho_{\rm b}$ from Eq. (11) are $\rho_{\rm b} = 0.5189$ and 0.4535. Now, substituting the results, $G_{\rm cm} = 0.4435 \,{\rm J} \,{\rm m}^{-2}$, $\rho_{\rm m} = 2.6583$ for the membrane film of thickness $h = 10 \,{\rm \mu m}$, and $G_{\rm cb} = 0.3664 \,{\rm J} \,{\rm m}^{-2}$, $\rho_{\rm b} = 0.4535$ for the linear bending film of thickness $h = 60 \,{\rm \mu m}$ into Eqs. (27) and (28), mode I and II adhesion toughness are determined to be $G_{\rm Ic} = 0.3240 \,{\rm J} \,{\rm m}^{-2}$ and $G_{\rm IIc} = 0.5149 \,{\rm J} \,{\rm m}^{-2}$, which are significantly larger than the corresponding $G_{\rm Ic} = 0.2446 \,{\rm J} \,{\rm m}^{-2}$ and $G_{\rm IIc} = 0.4152 \,{\rm J} \,{\rm m}^{-2}$ from the first group of tests. Similarly, to examine the accuracy of these values, the adhesion toughness of the film with the thickness of $h = 31 \,{\rm \mu m}$ is now calculated analytically using Eq. (13). Substituting $G_{\rm Ic} = 0.3240 \,{\rm J} \,{\rm m}^{-2}$, $G_{\rm IIc} = 0.5149 \,{\rm J} \,{\rm m}^{-2}$, which again is in excellent agreement with test result of $G_{\rm cb} = 0.3711 \,{\rm J} \,{\rm m}^{-2}$.



Fig. 5. Variation of adhesion toughness G_c at the graphene/copper interface with respect to $R_{\rm B}/h$ under the four test conditions.

Figure 5 shows the variation of the adhesion toughness G_c at the graphene/copper interface with respect to R_B/h under the four test conditions. Similar facts are observed to those from Fig. 4 (which shows G_c for the photoresist/copper interface), but with a distinct difference: The adhesion toughness G_c in all the four test conditions are now significantly larger than the corresponding ones for the photoresist/copper interfaces. The mono graphene layer increases the adhesion toughness.

Due to the lack of experimental results for the case of point loads, it is not possible to assess the developed mechanical model for the point load case. In the case of multilayer graphene membranes, however, the latest work [26] reports comparisons between the model and experimental results and excellent agreement is observed.

5. Conclusions

For linear bending with small deflection, the interface fracture of thin film blisters is mode I dominant. The through-thickness shear force makes an extra contribution to the mode I ERR and decreases the mode mixity. The thicker the film is, the smaller the adhesion toughness is. For membrane stretching with large deflection, the interface fracture of thin film blisters is mode II dominant. Membrane films consequently have larger adhesion toughness. Furthermore, the through-thickness shear force has no effect on the mode mixity which is only dependent on the Poisson's ratio. The large mode mixity difference between these two limiting cases enables the mode I and II adhesion toughness of thin films to be accurately determined. Experimental results show that the method has a good capability.

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