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1           **Friction in Ultra-thin conjunction of Valve Seals of**  
2                           **Pressurised Metered Dose Inhalers**

3  
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23 **Abstract**

24

25 In many drug dispensing devices, such as syringes and inhalers, a rubber disk is used as a  
26 seal. During device actuation the seal is subjected to friction which in turn causes its  
27 deformation. This can lead to suboptimal performance of the device and consequent  
28 variability in delivered dose. Seal friction is complex, arising from adhesion of rubber in  
29 contact with the moving interface, viscous action of a thin film of fluid and deformation of  
30 seal asperities. Therefore, the first step in understanding the conjunctive behaviour of  
31 rubber seals is the fundamental study of mechanisms of friction generation. A developed  
32 model can then be validated against measurements. The validated model can then be used to  
33 predict product performance, robustness and variability due to manufacturing tolerances.

34 A friction model, based on the aforementioned mechanisms, for prediction of seal friction has  
35 been developed and validated against measured friction tests performed on both nano and  
36 component level scales. Pressure changes in the metering chamber have been taken into  
37 account in the model. Friction data are presented for nitrile rubber, using a silicon nitride  
38 AFM tip for nano-scale interactions and polybutylene terephthalate (PBT) for asperity  
39 interactions at a component level, where a traditional friction test apparatus is utilised.

40 Reasonable agreement is found between measurements and model predictions for the nano-  
41 scale coefficient of friction of rubber against silicon nitride. Similarly, good agreement has  
42 been obtained for the mean coefficient of friction of rubber against PBT. It was found that the  
43 model was capable of predicting static friction coefficient reasonably well and the  
44 contribution to the coefficient of friction was mostly due to adhesive friction. The inputs of  
45 viscous and ploughing friction were negligible.

46

47

48 **Keywords:** pMDI valve, elastomeric seals, friction, adhesion.

49 **Nomenclature:**

50	$A$	Real contact area
51	$A_t$	Asperity contact area
52	$A_c$	Area under the curve of friction force versus pressure
53	$a$	Hertzian contact half-width
54	$b$	Undeformed cross-sectional seal diameter
55	$D_f$	Fractal dimension
56	$D_s$	Diameter of the sealed element
57	$DF$	Degree of freedom
58	$E$	Reduced (effective) elastic modulus of the contacting pair
59	$E_{rub}$	Elastic modulus of the nitrile rubber
60	$E_{stem}$	Elastic modulus of the stem
61	$F_a$	Adhesive friction force
62	$F_d$	Ploughing friction force
63	$F_v$	Viscous friction force
64	$F_f^{av}$	The average total friction force
65	$f_d$	Single asperity ploughing friction force
66	$G$	Scaling constant
67	$g$	Deformed cross-sectional seal diameter
68	$h$	Film thickness
69	$l$	Base diameter of a hemispherical asperity
70	$m$	Equivalent mass of an asperity in sliding motion
71	$N$	Number of asperities

72	$P_w$	Power
73	$p$	Chamber pressure
74	$\Delta p$	Pressure difference
75	$p_{cont}$	Contact pressure
76	$p_m$	Maximum Hertzian pressure
77	$p$ -value	Probability
78	$R_c$	Increased radius of conforming contact
79	$R'$	Radius of a hemispherical-shaped asperity
80	$R_q$	RMS surface roughness
81	$R_q^{comp}$	RMS composite surface roughness
82	$r_a$	Radius of a typical asperity
83	$RSS$	Residual sum of squares
84	$u$	Speed of entraining motion of fluid into the contact area
85	$V$	Relative sliding velocity of the valve
86	$W$	Applied normal load
87	$W_i$	Normal load on a hemispherical asperity
88	$w$	Effective width of the contact seal-stem
89	$z_0$	Height of asperity in ploughing action
90	$\alpha$	Calibration factor
91	$\beta$	Proportion of kinetic energy causing ploughing
92	$\delta_i$	Deflection for an asperity
93	$\varepsilon$	Squeeze ratio
94	$\eta$	Dynamic viscosity of the fluid

95	$\nu_{rub}$	Poisson's ratio of the nitrile rubber
96	$\tau_s$	Average shear strength of the dry contact
97	$\Phi$	Function in ploughing friction
98	$\psi$	Proportion of the contact in direct surface interactions
99		

## 100 **1. Introduction**

101

102 In recent years several significant changes have taken place in pressurised metered dose  
103 inhaler (pMDI) valves. These include the replacement of CFC (chlorofluorocarbon)  
104 propellants, deemed to be damaging to the ozone layer with HFA (hydrofluoroalkane) based  
105 propellants, as well as the introduction of new elastomers for the containing valve seals. This  
106 transition has provided an opportunity to re-evaluate inhaler performance as noted by Everard  
107 [1]. The valve in the pMDI is one of the key integral components for device performance.  
108 This was noted in the studies carried out in the transition from CFC to HFA by Schultz [2].

109

110 In many inhalation devices, an elastomeric material, usually a form of rubber is placed  
111 around a moving stem to seal the formulation within a chamber. During the movement of the  
112 stem the seal is subjected to friction, increasing the deformation of the sealing area. This  
113 deformation contributes towards the perceived challenges relating to valve leakage, drug  
114 adsorption, dose variability changes, “loss of dose” and “ loss of prime” effects [3].  
115 Therefore, the tribological behaviour plays an important role when considering new  
116 propellants with active compounds.

117

118 The tribological behaviour in a medical device is influenced by dimensional tolerance of the  
119 moulded or cut components, as well as by the rheological characteristics of any fluid or  
120 propellant-drug-surfactant mixture, referred to as the formulation. The assessment of seal  
121 friction within the device is crucial in evaluating its design space. Material characteristics are  
122 capable of being measured on a nano-scale possibly as part of the in-line manufacturing  
123 process or as a quality check. In-situ measurement of these characteristics proves  
124 problematic. The benefit of linking the nano-scale to component-scale provides a possible

125 route to the assessment of dimensional or material properties that need to be controlled in  
126 order to guarantee the reliability, robustness and manufacturability of the delivery device.

127

128 When the seal is fitted into the device it undergoes some global deformation, which alters the  
129 shape of its conjunction with the contacting sliding stem, whose motion actuates the inhaler  
130 valve. Therefore, there is a corresponding tensile force which strives to return the seal to its  
131 undeformed state. The shape of the ring is also affected by the canister pressure, which  
132 compresses the seal, with a corresponding outward reaction. These resistive forces are  
133 balanced by the contact force between the seal and the stem, which is as the result of any  
134 generated fluid pressure in the conjunction and asperity pressures. During the device  
135 actuation (motion of stem) the seal is subjected to friction, which is generated by viscous  
136 action of a very thin adsorbed film on the contiguous surfaces and asperity-pair interactions  
137 as described by Grimble *et al* [5].

138

139 Friction is quite complex, arising from adhesion and viscous action of a thin film. Therefore,  
140 the first step in understanding the conjunctive behaviour of such elastomeric seals is the  
141 fundamental study of mechanisms of friction generation. A developed model can then be  
142 validated against measurements, prior to its use in a multi-body dynamic model [6] of the  
143 inhaler valve to predict product performance, robustness and variability due to manufacturing  
144 tolerances. This paper undertakes two distinct studies.

145

146 Firstly, a friction model for the rough elastomeric material, typically used for valve seals is  
147 developed. The model is then validated against measurements at nano-scale. Friction data is  
148 presented for nitrile rubber, using a silicon nitride AFM tip for nano-scale interactions. The  
149 validation is then extended to macro-scale motion of an instrumented trolley, incorporating



150 an elastomeric surface sliding on a polymeric counterface. Therefore, these tests carried out  
151 for polybutylene terephthalate (PBT) give a component-scale measure of performance.

152

153 Secondly, the validated friction model is used in an elastomeric seal model in-situ within the  
154 valve and in contact with a polymeric stem surface and subject to both global fittment  
155 deformation and canister pressure.

156

157

## 158 **2. Metered dose inhaler and its valve design and principles of operation**

159

160 Several types of device are used to deliver a metered dose of aerosolised medication to the  
161 respiratory tract. pMDIs refer to those devices that incorporate a propellant under pressure to  
162 generate a metered dose of an aerosol through an atomisation nozzle. These devices consist  
163 of several components as shown in Figure 1. The active substance formulated with a  
164 propellant and excipients are contained in a canister. A metering valve is crimped onto the  
165 canister with an actuator that connects the metering valve to an atomisation nozzle and a  
166 mouth piece. The metered volume is typically between 20 to 100  $\mu\text{l}$ . The metered volume is  
167 rapidly expelled from the valve through the actuator orifice where atomisation occurs [7].

168

169 The key stages in the drug delivery process of standard valves include filling of the metering  
170 chamber, storage and delivery of the dose. During these processes a combination of seals are  
171 used to open and close the channels that allow the fluid to freely flow. In Figure 2 two  
172 extreme cases are presented. On the left, the valve is at rest; whilst on the right, the stem is  
173 fully depressed and the drug is released to the patient. For the valve depicted in Figure 2 the  
174 drug delivery process is as follows:

- 175 1. The stem component is in the rest position. The metering chamber contains a metered  
176 volume of the formulation.
- 177 2. The stem is depressed slowly, closing the channel linking the metering chamber to the  
178 bulk.
- 179 3. The stem is depressed further, opening the channel in the upper stem and allowing the  
180 formulation to flow towards the actuator nozzle.
- 181 4. The depressed valve is released, closing the metering chamber to the actuator nozzle.
- 182 5. The depressed valve is released further, opening the metering chamber to the bulk  
183 formulation in the canister, thus allowing the valve to pre-meter the required next  
184 dose.

185 During these phases the seals deform and slide in relation to other valve components,  
186 controlling the metering volume and the dynamic performance of the system.

187

188

### 189 **3. The friction model**

190

191 As an initial study a one-dimensional contact between the deformed seal face-width and the  
192 sliding stem is considered. Such an analysis considers the contact behaviour per unit length of  
193 the seal contact, when subjected to a sliding motion and fluidic pressure loading. It is,  
194 therefore, an approximation, which has also been used by other investigators, dealing with  
195 tribology of seals such as Hooke *et al* [8], Karaszkiwicz [9] and Nikas [10] for seals and o-  
196 rings. However, it should be noted that whilst this is a reasonable simplifying assumption,  
197 yielding an analytic solution, the contact geometry is in fact at least partially conforming,  
198 requiring a 2-D numerical solution. The resulting 1-D analytical model is then used to obtain

199 an estimate of friction due to adhesion, viscous action of a thin film of formulation, as well as  
200 any asperity ploughing action.

201

202 The values of the contact pressure between the stem and seal during HFA release are used in  
203 the friction model, based on the works of Bhushan [11], Bowden and Tabor [12] and Gohar  
204 and Rahnejat [13]. The proposed model is appropriate for lightly loaded contacts. This initial  
205 study assumes that the fluid viscous behaviour remains Newtonian. However, more details  
206 are included for asperity interactions. The total friction force is, therefore, contributed by  
207 three phenomena:

208

$$209 \quad F = F_a + F_v + F_d \quad (1)$$

210 where  $F_a$  represents adhesive friction which is the effort required to break the cold-welded  
211 junctions between the asperity pairs on the contiguous surfaces. The adhesive friction is  
212 obtained as:

213

$$214 \quad F_a = A \psi \tau_s \quad (2)$$

215

216 where the value of  $\psi$  corresponds to the proportion of the contact in direct surface  
217 interactions.  $A$  is the real contact area, rather than the apparent one, and is given by Bhushan  
218 [11] and Gohar and Rahnejat [13] as:

219

$$220 \quad A = 3.2 \frac{W}{E} \sqrt{\frac{r_a}{R_q^{comp}}} \quad (3)$$

221

222 The second term on the right hand side of (1) is due to viscous friction, where:

$$223 \quad F_v = A(1-\psi)\frac{\eta u}{h} \quad (4)$$

224 The third term;  $F_d$  is the ploughing or deformation friction described later.

225

226 Assuming iso-viscous conditions and noting that the speed of entraining motion of any fluid  
227 film,  $u$  into the conjunction is half the sliding velocity of the seal, one needs to obtain the film  
228 thickness  $h$  in order to evaluate  $F_v$ . This is described in section 4.

229

230 Now returning to the third component of friction,  $F_d$  in equation (1), this is due to the  
231 oblique contact of asperity pairs, where those on the harder counterface (in this case on the  
232 stem) plough through those on the softer material (the elastomeric seal). This ploughing  
233 action may result in elastic or plastic deformation of the softer asperities. Here elastic  
234 ploughing of rubber seal asperities is assumed to occur. Thus, according to Gohar and  
235 Rahnejat [13]:

236

$$237 \quad F_d = \pi N f_d \left( 1 - e^{-\Phi V^{\frac{4}{3}}} \right) \quad (5)$$

238 In this study elastic ploughing of asperities is considered, thus:

$$239 \quad f_d = \pi(8R'z_0)E \left( \frac{R_q^{comp}}{r_a} \right)^{\frac{1}{2}} \quad (6)$$

240 And  $\Phi$  for the elastic case is given as:

$$\Phi = \frac{1}{8R'} \left\{ \frac{\beta m}{2\pi E} \left( \frac{r_a}{R_q^{comp}} \right)^{\frac{1}{2}} \right\}^{\frac{2}{3}} \quad (7)$$

The accuracy of predictions partly depends on the validity of the assumption concerning elastic ploughing of asperities and partly on the proportion of kinetic energy expended in asperity deformation,  $\beta$ , which is assumed to be  $\beta = 0.8$  in this study [14].

#### 4. Determination of film thickness in the contact conjunction

Figure 3 shows the cross-section of a seal (for simplicity considered to be circular (a), squeezed in its retaining groove (b) and under metered chamber pressure (c). Following the simplified analytical approach of Karaszkiwicz [9] a Hertzian contact may be assumed in the fitment of the seal, where the length of the contact is given as  $\pi(D_s + b)$ , which is large compared with  $b$ . Also, the effective modulus for the contact  $E = E_{rub}$ , since:  $E_{stem} \gg E_{rub}$ . Thus, using Hertzian theory, Karaszkiwicz [9] showed that the average transverse contact pressure for the assumed infinite line contact condition becomes (see Figure 3(b)):

$$p_{cont} = \frac{\pi}{6} \left( \frac{2a}{b} \right) E_{rub} \quad (8)$$

For an analytic solution it is necessary to determine the contact load as the result of this mean pressure, which requires evaluation of the Hertzian contact width  $2a$ . Karaszkiwicz [9] measured the width  $2a$  of a seal squeezed between a glass and a steel plate and obtained an empirical relationship for the ratio  $\frac{2a}{b}$ , which agrees well with the finite element results of

263 George *et al* [16]. Thus, the mean pressure in equation (8) can be obtained. His empirical  
264 relationship is used here as:

265

$$266 \quad \frac{2a}{b} = 2\varepsilon + 0.13 \quad (9)$$

267

268 where  $\varepsilon$  is the squeeze ratio described below.

269

270 When the seal is subjected to the canister pressure  $p$ , the contact pressure distribution alters  
271 as shown in Figure 3 (c), pushing the seal against the groove wall. As the rubber seal is  
272 considered to be incompressible ( $\nu_{rub} \approx 0.5$ ), the contact width alters. A series of  
273 experiments carried out by Johannesson [17] suggest that:

274

$$275 \quad w = \left( (2\varepsilon + 0.13) + \left[ 0.39(1 - \varepsilon)^{-1} - 0.5(2\varepsilon + 0.13) \right] \left[ 1 - e^{\left( \frac{-4.6p}{E_{rub}} \right)} \right] \right) b \quad (10)$$

276

277 The film thickness required in (3) is estimated from Karaszkievicz [9] where:

278

$$279 \quad h = 4.4(\eta u)^{0.65} (R_c)^{0.56} (W)^{-0.21} (E)^{-0.44} \quad (11)$$

280

281  $W$ , the total applied load on the seal is due to a seal fitting into its groove with the fluid  
282 pressure load acting behind it:

283

284 
$$W = w \left\{ \left( \frac{\pi}{6} \right) (2\varepsilon + 0.13) E_{rub} + \frac{V_{rub}}{1 - V_{rub}} P \right\} \quad (12)$$

285 where  $\varepsilon$  is the squeeze ratio given as:  $\varepsilon = \frac{b-g}{b}$ . In the present case it is  $\varepsilon = 0.102$ .

286  $w$  is the effective width of the contact that the seal makes with the stem, when fitted *in-situ*  
287 and subjected to a pressure,  $p$ .

288

289

## 290 **5. Materials used and methods of measurement**

291

292 Nitrile rubber and PBT samples were used for friction tests described below. All experiments  
293 were performed under ambient conditions ( $40 \pm 1\%$  RH, temperature  $20 \pm 0.5$  °C).

294 The simulations were carried out assuming that the physical properties of the liquid contained  
295 in the metered chamber are those of pure HFA 227a. The presence of surfactant and drug in  
296 the mixture was neglected due to their low concentrations.

297

298

### 299 **5.1 AFM imaging and nano-scale friction force acquisition**

300

301 An atomic force microscope (Nanoscope IV, Digital Instruments) was used to initially  
302 characterise the surface topography of counterfaces. This data is required for the adhesive and  
303 ploughing components of the developed friction model. The AFM is also used to determine  
304 the coefficient of friction.

305

306 Roughness measurements were carried out in the tapping mode, while friction measurements  
307 were conducted in lateral force mode. V-shaped micro-fabricated ( $100 \mu\text{m}$ ) cantilevers with

308 pyramidal, oxide-sharpened Si<sub>3</sub>N<sub>4</sub> tips, supplied by Digital Instruments (model DNP, spring  
309 constant of 0.58 N/m) were used for all the friction measurements. Surface friction force data  
310 was acquired by simultaneously scanning in the forward (+*x*) and reverse (-*x*) directions with  
311 disabled scanning in the *y* direction. The sliding tip velocity was set at 50 μm/s with the scan  
312 frequency of 1 Hz. Each measurement used here represents an average of at least five  
313 independent scans.

314

315 The raw friction data in volts output was determined from half the difference between the  
316 retrace (right-to-left) and trace (left-to-right) 512- by 512-pixel lateral force images. The  
317 friction force image with subtraction is shown in Figure 4. All the measured friction data sets  
318 were fitted with Gaussian distribution in order to obtain mean values and standard deviations.

319

320 The static friction coefficient between rubber and Si<sub>3</sub>N<sub>4</sub> tip was determined by measuring the  
321 maximum value of the lateral deflection of the AFM tip [18].

322

323 To convert the raw friction data (in volts) into lateral forces (in Newton) a lateral force  
324 calibration factor  $\alpha$  (in V/nN) was obtained according to the calibration procedure described  
325 in Ahimou *et al* [19]. Silicon wafers were used as the calibration standard. The silicon wafers  
326 were cleaned for 10 min in acetone, rinsed with deionised water and dried by adding a few  
327 drops of ethanol to remove excess water. Measurements were performed before and after  
328 each rubber test to ensure that the state of the AFM probe remained unaltered. A step increase  
329 in applied load between 0-200 nN was employed per image from a 100 μm<sup>2</sup> region of silicon  
330 wafer surface (Figure 5). The scan velocity was 50 μm/s at 0.5 Hz scan frequency. In each  
331 case, the plot of raw friction force in volts versus the applied load in nN was reproduced by a  
332 linear fit, consistent with Amontons' law of friction [20] with the slope  $k_{\text{SiO}_x}$  determined in



333 units of V/nN. This slope is equal to the “to- be-determined” apparatus coefficient times the  
334 actual friction coefficient obtained by  $\mu_{\text{SiO}_x} = 0.19 \pm 0.01$ , averaged from the data obtained by  
335 Buenvuaje *et al* [21] and Putman *et al* [22]. All the raw friction force values (volts) measured  
336 during friction tests for rubber were divided by the value for  $\alpha$  (V/nN) =  $k_{\text{SiO}_x}/0.19$  to convert  
337 them to calibrated friction force levels in units of nN. The friction coefficient was determined  
338 dividing the measured nano-scale friction force by the applied load of 50nN.

339

340

## 341 **5.2 Tribometric device**

342

343 Component-level (macro-scale) friction between the nitrile rubber and a PBT flat sheet was  
344 measured using a traditional friction test apparatus; an instrumented trolley test. A schematic  
345 of the device is shown in Figure 6. The force transducer measures the friction between the  
346 contacting surfaces, whilst the sliding velocity is recorded by a laser vibrometer (Polytec  
347 model 302), shun on the sliding trolley surface.

348

349 The raw friction data (volts) and sliding velocity (volts) were recorded in real time. Knowing  
350 the sensitivity (25 mm/s/V) of the vibrometer, the sliding velocity was obtained. The  
351 measured sliding velocity during the experiments was up to 0.06 m/s. The calibration  
352 procedure was adopted to convert the acquired friction signals from Volts to Newtons.  
353 Before experiments a load cell (capacity: 0.3-3 kg) was calibrated with known weights to  
354 obtain measurement friction sensitivity. All raw friction force values (in Volts) were  
355 multiplied by the friction sensitivity (1.18 N/V) to convert them to friction force. The friction  
356 coefficient was obtained by dividing the friction force by the applied normal load (4.51 N).

357

### 358 **5.3 Statistical analysis**

359 To determine whether the average of the measurements of  $Rq$  roughness values for a sample  
360 of ten gaskets was statistically sufficient to represent this parameter; the following procedure  
361 was followed [23].

362

363 The  $RSS$  (residual sum of squares) was estimated for the ten  $Rq$  values and for each of the  
364 combinations with 9 values. Then the value of “ $f$ ” was determined as:

$$365 \quad f = \frac{(RSS_2 - RSS_1)/(DF_1 - DF_2)}{RSS_1 / DF_1} \quad (13)$$

366 where  $DF$  is the degree of freedom (number of  $Rq$  values for average determination – 1) and  
367 the subscript 1 refers to the ten samples and 2 to each of the combinations of nine samples.

368 The value of  $f$  was compared with the values from the  $F$  distribution with  $DF_1$ -  $DF_2$  and  $DF_1$   
369 values of freedom ( $F_{DF_1}^{DF_2-DF_1}$ ) at a set probability (for this work it was set at 0.05); if  $f >$

370  $F_{DF_1}^{DF_2-DF_1}$  then the addition of the tenth  $Rq$  value is of benefit, otherwise the difference between  
371  $RSS_1$  and  $RSS_2$  is smaller than the measuring error ( $RSS_1$ ).

372

373 The average values of surface roughness  $Rq$  determined in three points along the face-width  
374 of the seal (Figure 7) were compared with the one way ANOVA test followed *post hoc* by the  
375 Tukey’s test for individual pairs ( $p$ -value <0.05). These analyses were performed using the  
376 SPSS software.

377

## 378 **6. Results and discussion**

### 379 **6.1 Determination of parameters for the friction model**

380 Input data for the friction model (section 3) requires measurement of surface roughness  
381 parameters such as those for rubber and PBT,  $R_q$ , and the RMS composite surface

382 roughness,  $R_q^{comp}$ , average tip radius of asperities,  $r_a$ , as well as determining a representative  
383 value for radius of hemispherical asperities,  $R'$ . It is also necessary to determine the number  
384 of asperities in the real contact area,  $N$ .

385

386 Surface roughness ( $Rq$ ) for rubber and PBT samples were obtained from samples of 10 by 10  
387  $\mu\text{m}$  AFM images. An example of an AFM image for the nitrile rubber is shown in Figure 8.  
388 A statistical  $F$ -test revealed that the average value of  $Rq$  obtained from nine measurements  
389 was adequate to describe this parameter.

390

391 The value of  $Rq$  was also estimated in different locations along the seal facewidth to  
392 determine if the manufacturing method makes any significant differences. It was found that  
393 the values of roughness were statistically different ( $p$  – value  $<0.05$ ). Moreover the Tukey’s  
394 test showed that the roughness in position A was different from that in locations B and C. The  
395 normalised frequency of  $Rq$  at the three locations chosen is shown in Figure 9. It can be seen  
396 that the average value of  $Rq$  in B ( $Rq = 1.04$ ) and C ( $Rq = 1.13$ ) are very close, whilst that at  
397 position A, it was ( $Rq = 1.51$ ), the standard deviation of  $Rq$  at B is smaller (0.12) than at A  
398 and C (0.28 and 0.30 respectively). As there are two statistically different values for  $Rq$ , the  
399 friction model simulations were carried out with both the values of  $Rq$  at positions A and B  
400 (see Table 1).

401

402 The composite surface roughness was calculated as  $R_q^{comp} = \sqrt{R_{q\_rub}^2 + R_{q\_stem}^2}$ , where  $R_{q\_rub}$   
403 and  $R_{q\_stem}$  are the surface roughness values for rubber and PBT stem respectively.

404

405 Other surface parameters required for the friction model are the average asperity tip radius  
406 and height. The asperities were assumed to be hemispherical in shape with a radius  $R'$  and a  
407 base diameter  $l$ , such that the base area is proportional to  $l^2$ . The radius of curvature,  $R'$ ,  
408 for the asperity can be found as (Bhushan [11]):

$$409 \quad R' = \frac{l^{D_f}}{G^{(D_f-1)}} \quad (14)$$

410 The fractal dimension,  $D_f$ , of the roughness profile is then calculated using two methods: (i)-  
411 enclosing boxes and (ii)- morphological envelopes. The average value of fractal dimension  
412 obtained from these two methods is used to calculate the radius of curvature and the height of  
413 an asperity.

414

415 Also the average typical radius of the asperity was determined independently. A surface (10 x  
416 10  $\mu\text{m}$ ) was scanned along lines spaced by intervals of 0.25  $\mu\text{m}$ . For each line the  $z$  –  
417 coordinate of the surface was measured. Along each line the peaks (local maxima) were  
418 identified as points, whose  $z$ - coordinate was higher than the coordinates of three consecutive  
419 points prior to and after it. This procedure led to the estimation of the total number of peaks  
420 in the scanned area (number of peaks/ $\mu\text{m}^2$ ). This value was later used to estimate the total  
421 number of peaks presented in the real area of contact. The coordinates of these seven points  
422 were interpolated with a parabolic equation (the values of the three parameters were  
423 estimated according to the minimal residual sum of square methods with an in-house  
424 algorithm running in Excel 2003).

425

426 For each peak the curvature radius was determined from the fitting equation using the  
427 following expression:

428

$$r_a = \frac{\left[1 + \left(\frac{\partial z}{\partial x}\right)^2\right]^{3/2}}{\frac{\partial^2 z}{\partial x^2}} \quad (15)$$

430

431 Finally, the average value and standard deviation of the curvature radius of the surface peaks  
432 was determined.

433

434 The number of asperities was determined both experimentally (see above) and numerically.

435 The numerical procedure was based on expressions for circular contact footprints described  
436 by Gohar and Rahnejat [13]. This assumes that both surfaces are nominally flat, but one of  
437 them has isotropic roughness features with identical spherically shaped asperities on it.

438

439 The normal load on each asperity is defined as:

$$W_i = \frac{4}{3} \left( ER'^{1/2} \delta_i^{3/2} \right) \quad (16)$$

441 and the contact centre deflection for each asperity according to the classical Hertzian theory  
442 is:

$$\delta_i = \left( \frac{9W_i^2}{16E^2 R'} \right)^{1/3} \quad (17)$$

444 The contact area for one elastic spherical asperity in terms of its deflection is then defined as:

$$A_i = \pi R' \delta \quad (18)$$

446 An iteration procedure is adopted to determine the contact area for one asperity.

447 Knowing  $A_i$  the total number of asperities can then be found as:

448 
$$N = \frac{A}{A_i} \quad (19)$$

449 The numerically obtained number of asperities agrees reasonably with the experimentally  
450 extracted values (Table 1). The experimentally obtained surface roughness parameters used in  
451 the development of the friction model are also summarised in Table 1.

452

## 453 **6.2 Validation of the friction model**

454

455 The friction model was validated against experimental results performed at both nano and  
456 component level (macro) scales. The friction on nano-scale was measured using AFM while  
457 a sliding trolley test rig was used for obtaining friction data on the macro-scale. The  
458 experiments were carried out under dry conditions, consequently, there was no viscous force  
459 involved due to the absence of the lubricant film.

460

461 Experimentally obtained friction results are presented in Table 2. Friction model predictions  
462 give the value of coefficient of friction as 0.69 for the nitrile rubber-PBT combination. The  
463 same model applied for the nano-scale friction returns a coefficient of friction of 0.17, when  
464 the input parameters are those for the nitrile rubber and the silicon nitride AFM tip.  
465 Therefore, the predictions for the coefficient of friction for the nano-scale conforms  
466 reasonably well to the measured values, with an average percentage error of around 14%,  
467 while for the component-level (macro-scale) scale the predictions give an error of around  
468 23%. The effect of different surface roughness parameters of position A and B was to have  
469 negligible effect on the outcome of the model simulations.

470

471

### 472 **6.3 Friction results for the pMDI valve**

473

474 The validated friction model is then used for the pMDI valve operation. During the stem  
475 movement the pressure decreases from the initial 3.9 bar to atmospheric. The calculations of  
476 friction forces, their coefficients and the lubricant film thickness have been performed at  
477 several pressures within this range at a fixed sliding velocity of 20 mm/min. This velocity was  
478 chosen as it is the typical sliding velocity in the pMDI valve. The static friction coefficient is  
479 of main interest in this work, since the highest friction is observed during start up of the  
480 inhaler mechanism.

481

482 The total friction force (Figure 10) increases with pressure in the metering chamber due to an  
483 increase in the contact area with applied load. Therefore, the coefficient of friction remains  
484 almost constant at a value of 0.69 through pressure changes (Figure 11). The film thickness  
485 variation is negligible with increase of pressure in the metering chamber and stays in the  
486 range of a fraction of a nanometer (0.21-0.22 nm). This explains the insensitivity of friction  
487 variation with sliding velocity, indicating dominance of adhesive component of friction.

488

489 The total friction coefficient and its friction force are the sum of adhesive, viscous and  
490 ploughing terms contributions. The adhesive friction is dominant. Viscous and ploughing  
491 contributions are found to be insignificant. In fact, with pressure increases in the metered  
492 chamber the viscous friction force varies from 5.97 to 4.20  $\mu\text{N}$ , while the ploughing friction  
493 force changes from 15.5 to 11.6  $\mu\text{N}$ . The viscous friction is negligible because no film is in  
494 effect formed and the working sliding velocity is also very low (20 mm/min). This low  
495 sliding velocity, together with the rather smooth surface roughness profile of the contiguous  
496 surfaces makes the ploughing contribution also insignificant. Ploughing is as a result of hard,

497 mostly conical shape asperities deforming their counterparts on the softer material.. When, as  
498 in this case, the asperity angle is large the ploughing component of friction is correspondingly  
499 insignificant. Thus, the calculated points in figure 11 are really due to adhesive friction.

500

## 501 **7. Conclusions**

502

503 The friction model has been developed and validated on both nano and component level  
504 (macro) scales. Results show that the adhesive friction is dominant. Contributions of viscous  
505 and ploughing frictions are minor. To improve frictional behaviour, edge profiling of the seal  
506 may be undertaken in order to encourage lubricant entrainment into the contact by wedge  
507 effect (see Nikas [24]). However, seal edge-profiling can cause loss of effective sealing and  
508 detailed numerical analysis would be required, which points to one aspect of future work. The  
509 edge profiles also require manufacturing control, which may become cost ineffective.

510

511 The effort required to actuate the valve is a very important performance parameter because of  
512 the wide range of possible users with different strength; the measurement can be achieved  
513 through the hysteresis cycle (see Grimble *et al* [5]). This work can be used to predict the  
514 frictional behaviour of pMDIs and form the basis for their further development.

515



## 516 8. Acknowledgements

517

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519 technical support extended to this investigation.

520

## 521 9. References

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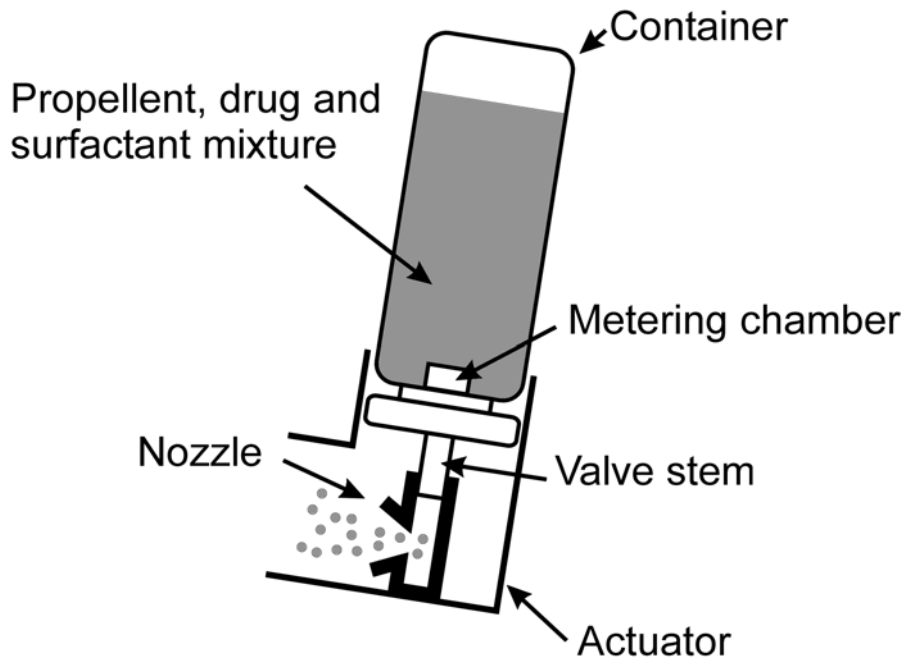
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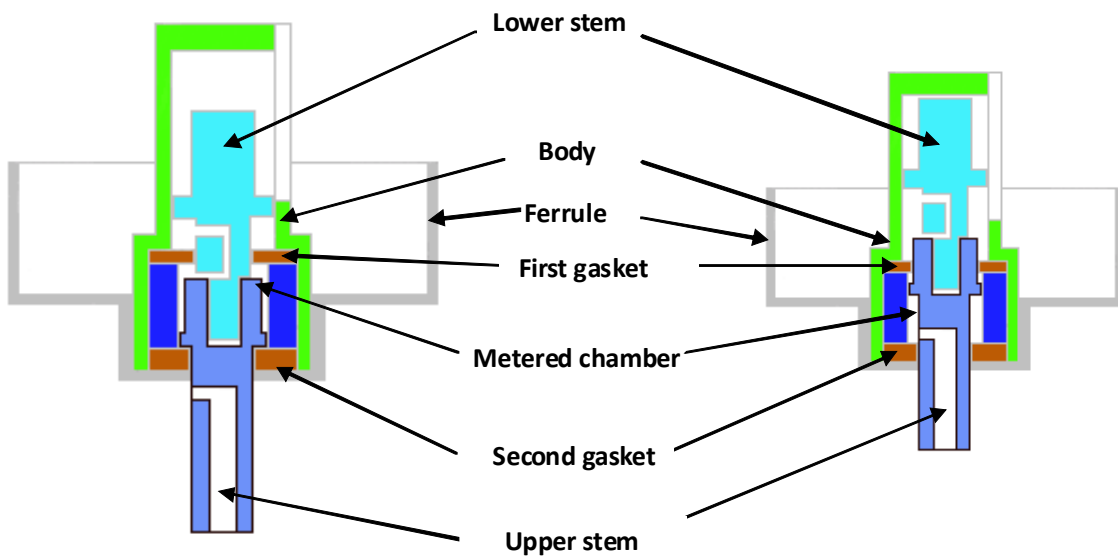
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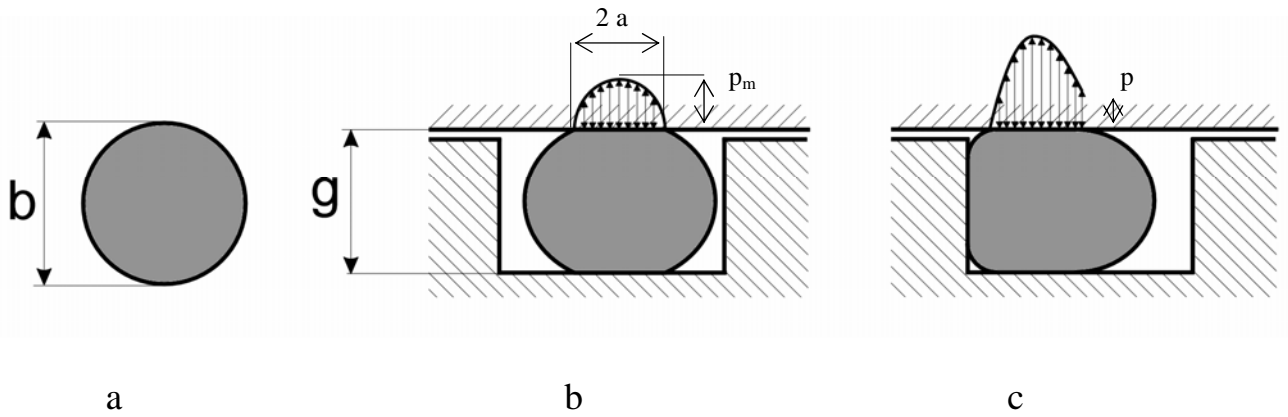
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**Figure 1: Schematic of a pressurised metered dose inhaler**



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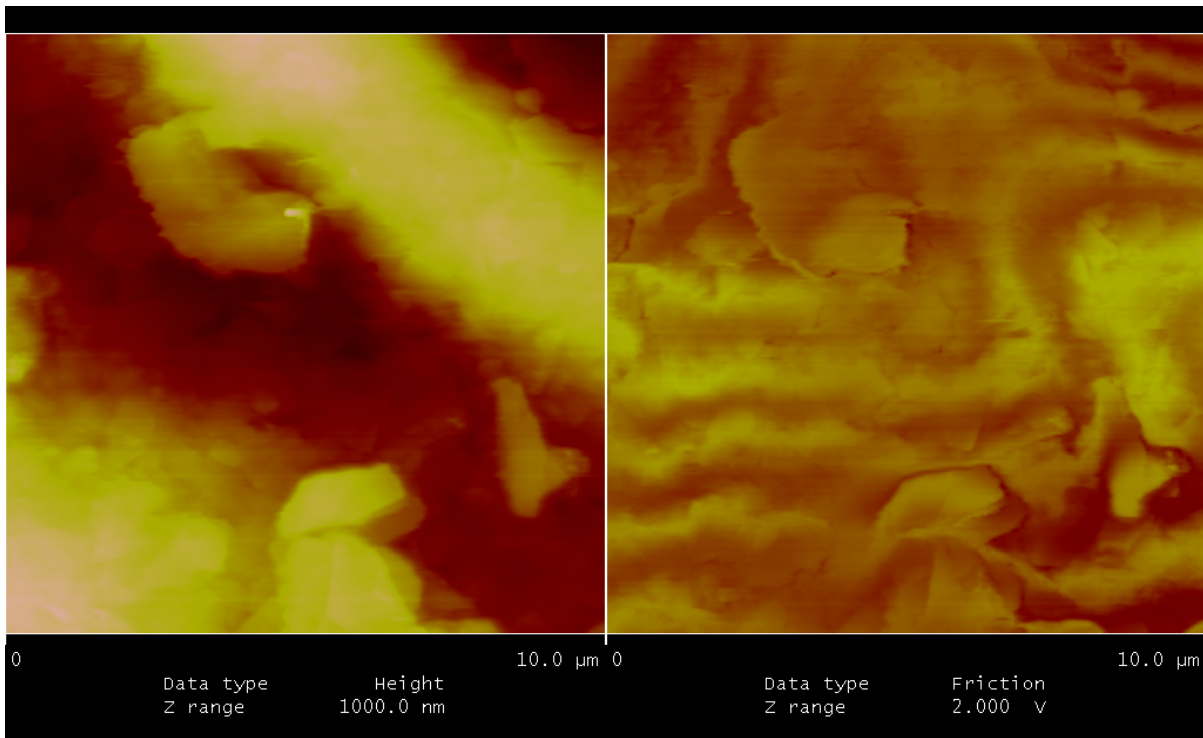
**Figure 2: Schematic of a typical valve configuration: on the left – valve at rest; on the right – stem fully depressed and drug released to recipient.**



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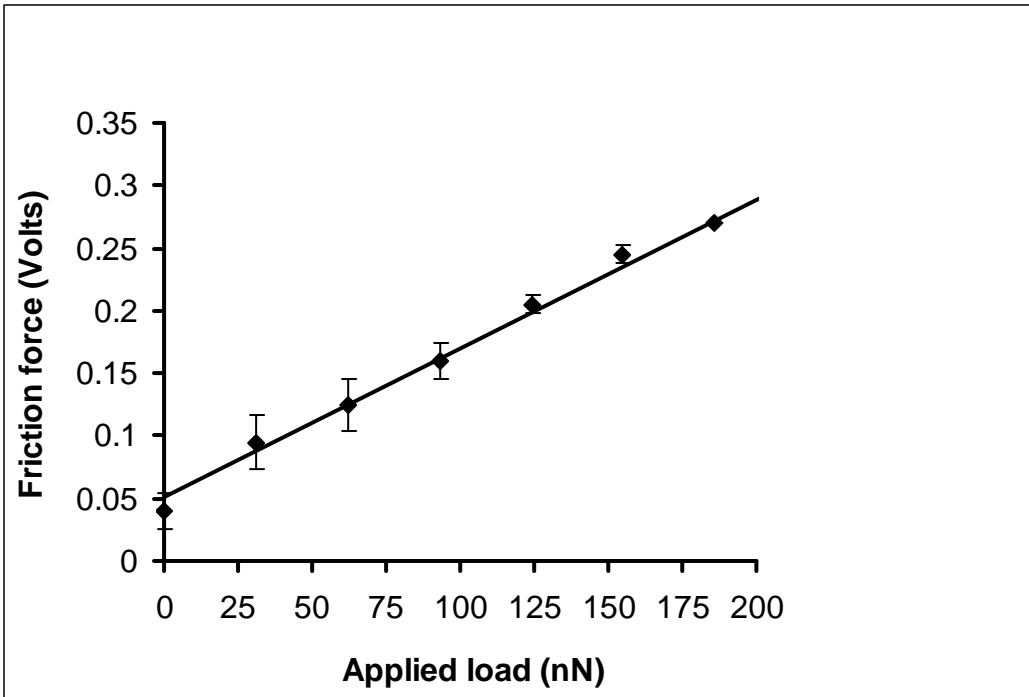
**Figure 3: Distribution of contact pressure and geometry of the O-ring mounted in the seal groove and subjected to sealed pressure: (a) undeformed seal; (b) deformed *in-situ* due to fitment . (c) at metered chamber pressure of  $p$  .**

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**Figure 4: Topographic (on the left) and friction force with subtraction (on the right) images of 10 by 10 μm of nitrile rubber**



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627 **Figure 5: Calibration curve for silicon wafer**

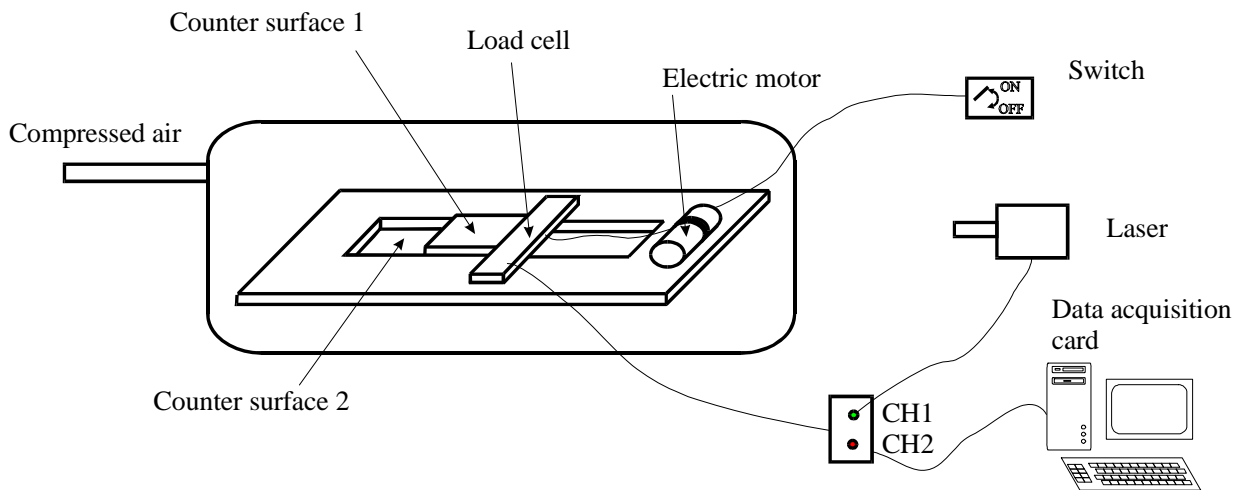
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638 **Figure 6: A schematic of the friction test apparatus**

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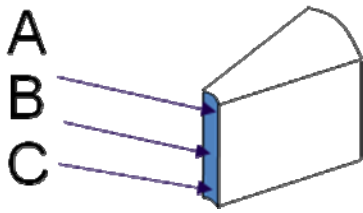
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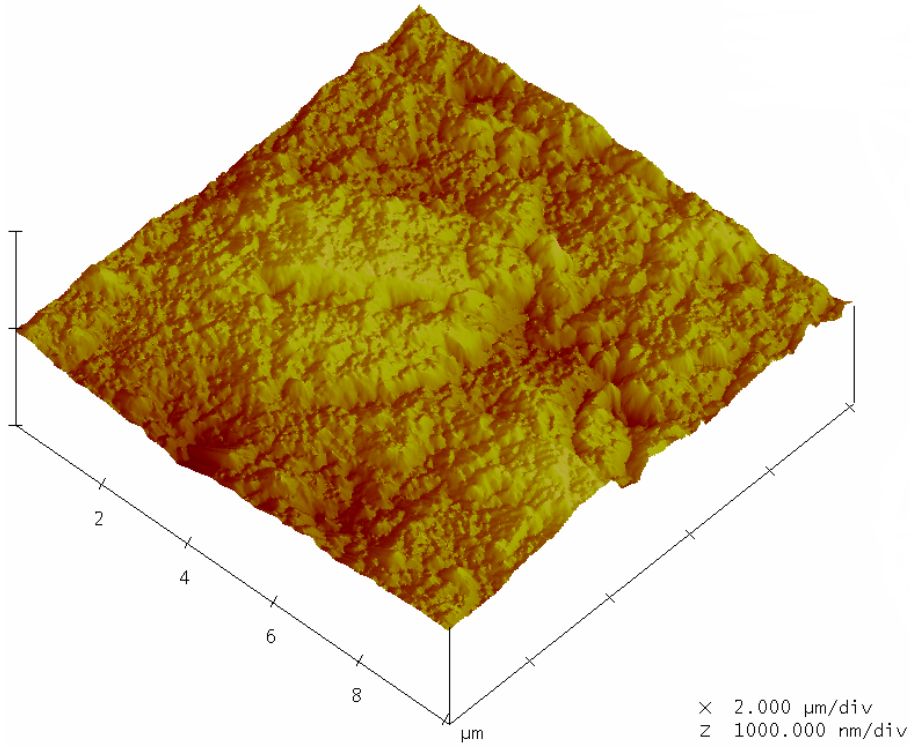


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**Figure 7: Cross section of the rubber seal**

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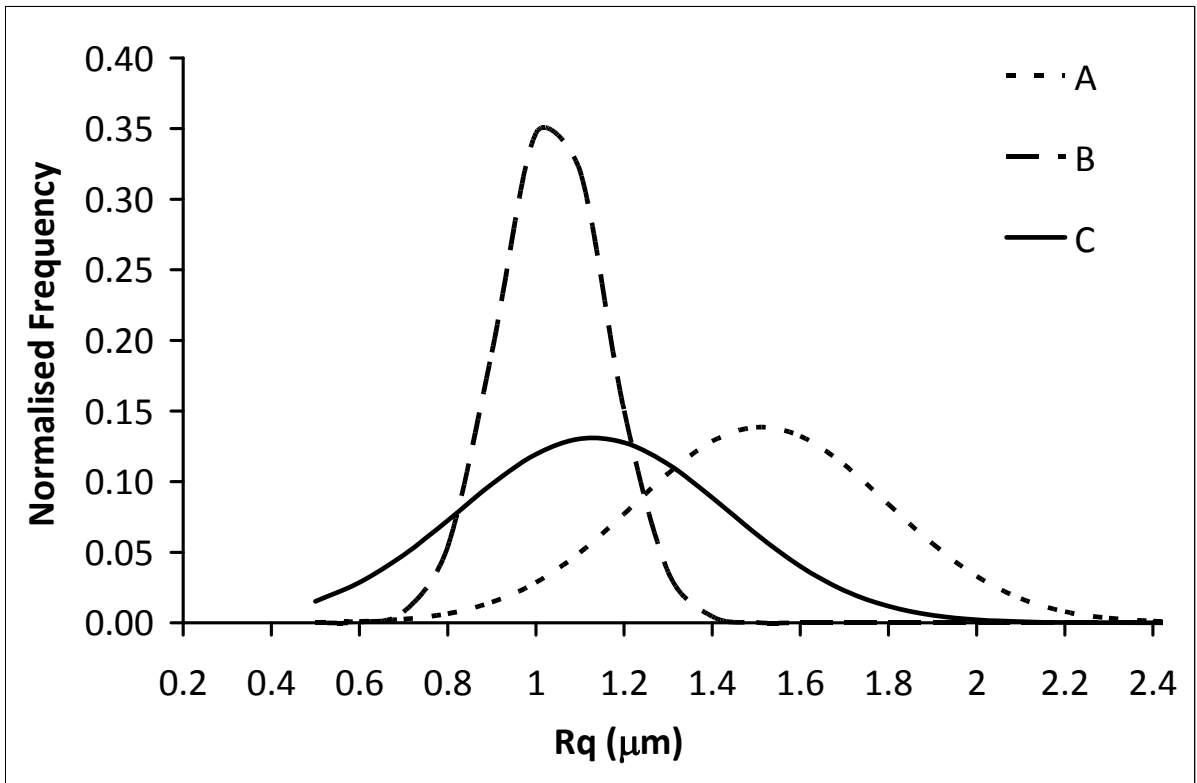
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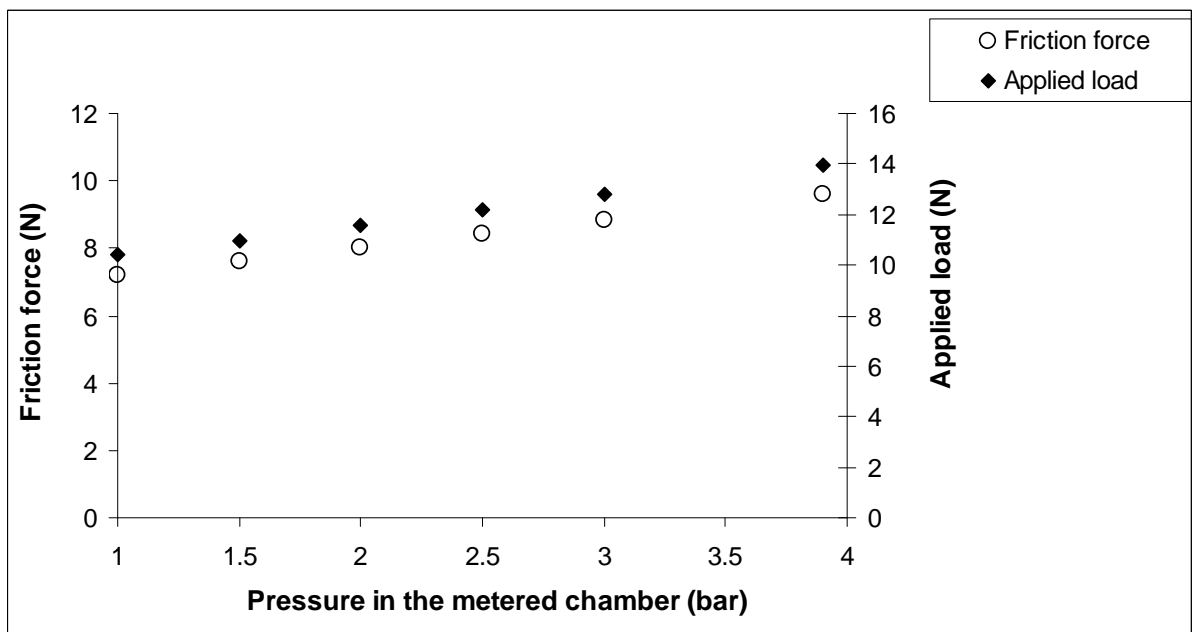
**Figure 8: An AFM image of the nitrile rubber surface**

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**Figure 9: Statistical analysis of  $R_q$  roughness data for the rubber seals**

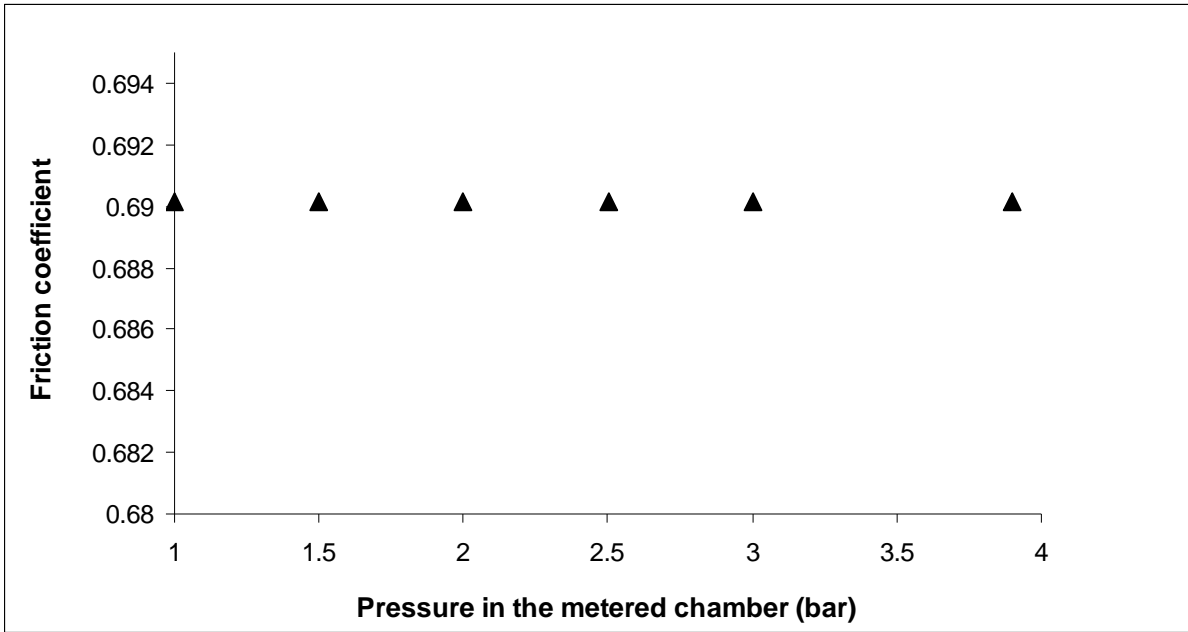


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**Figure 10: Friction force and applied load variations with chamber pressure**



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671 **Figure 11: Coefficient of friction variation with chamber pressure**

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678 **Tables**

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681 **Table 1: Experimentally obtained surface roughness parameters**

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Roughness parameters	Rubber gasket, position A	Rubber gasket, position B	PBT
$R_q$ ( $\mu\text{m}$ )	$1.51\pm 0.28$	$1.04\pm 0.12$	$0.31\pm 0.03$
$R'$ ( $\mu\text{m}$ )	$1.84\pm 0.09$	$2.12\pm 0.08$	
$z_0$ ( $\mu\text{m}$ )	$1.76\pm 0.04$	$1.72\pm 0.05$	
$r_a$ ( $\mu\text{m}$ )	$1.53\pm 0.04$	$1.55\pm 0.07$	
$N$ (experimental)	$1.4*10^{10}$	$1.4*10^{10}$	
$N$ (numerical)	$2.5*10^{10}$	$2.5*10^{10}$	

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688 **Table 2: Coefficients of friction on nano- and component level scales**

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Friction coefficient	Nitrile rubber/PBT		Nitrile rubber/Si <sub>3</sub> N <sub>4</sub> AFM tip	
	Experimental	analytical	experimental	analytical
	$0.59\pm 0.03$	0.69	$0.21\pm 0.025$	0.17

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