Microstructural and Mechanical Characterisation of Laser Welded High Carbon and Stainless Steel

M.R Nekouie Esfahani^{*}, J Coupland and S Marimuthu

Optical Engineering Group, Wolfson School of Mechanical and Manufacturing, Loughborough University, Loughborough, LE11 3TU, United Kingdom

Abstract

Laser welding is becoming an important joining technique for welding of stainless steel to carbon steel and is extensively used across various sectors, including aerospace, transportation, power plants, electronics and other industries. However, welding of stainless steel to high carbon steel is still at its early stage, predominantly due to the formation of hard brittle phases, which undermine the mechanical strength of the joint. This study reports a scientific investigation on controlling the brittle phase formation during laser dissimilar welding of high carbon steel to stainless steel. Attempts have been made to tailor the microstructure and phase composition of the fusion zone through influencing the alloying composition and the cooling rate. Results show that the heat affected zone (HAZ) within the high carbon steel has significantly higher hardness than the weld area, which severely undermines the weld quality. To reduce the hardness of the HAZ, a new heat treatment strategy was proposed and evaluated using a finite element analysis based numerical simulation model. A series of experiments has been performed to verify the developed thermo-metallurgical FEA model and a qualitative agreement of predicted martensitic phase distribution is shown to exist.

Keywords: Dissimilar welding; Laser; Microstructure; Hardness; Alloy concentration; FEA Modelling

^{*} Corresponding author:

Tel: +44 (0)7576175080, Fax: +44 (0)1509 227648, E-mail: m.esfahani@lboro.ac.uk.

1. Introduction

Laser welding of metals and alloys are extensively used in industry due to advantages of controlled heating, narrow weld bead and low heat affected zone (HAZ) [1]. Recently, laser dissimilar welding has been investigated extensively due to the increased demand across various industrial sectors [2, 3]. However, dissimilar laser welding of metals like high carbon steels (HCS) to stainless steel (SS) is still a challenging task due to the formation of brittle phases and solidification cracking in the fusion zone [4], and martensitic formation in the HAZ of carbon steel [5-7]. These issues can significantly deteriorate the strength of the welded joint and a robust methodology needs to be developed.

Many attempts have been made in the past to address the issues in dissimilar welding. Esfahani et al. [8] studied the martensite formation in dissimilar laser welding of low carbon steel (LCS) to stainless steel and showed that martensitic formation can be controlled by varying the beam positioning away from the weld centre. Nikulina et al. [9], revealed that the martensitic formation at the HAZ can leads to fatigue crack formation and subsequent failure in dissimilar flash butt welded joint of high carbon steel and chrome–nickel steel. The effect of weld chemical composition and heat input was investigated by Muthupandi et al. [10] and demonstrated that the alloying elements concentration have more significant role than the heat input. The final microstructure of the weld bead is a critical factor in laser welding, and David et al. [11, 12] showed that it can be influenced by controlling the cooling rate. An investigation conducted by Hajiannia et al. [13] showed that the carbon migration from the HAZ of low alloy steel toward the fusion zone result in formation of martensitic zone in the weld boundary with high hardness value and the optimal hardness value for HCS HAZ was found to be around 650HV_{0.05} [14].

Most of the previous studies on dissimilar laser welding concentrated on of LCS and SS, and the issues on laser welding of HCS and SS still prevails. The laser welding of HCS and SS is more complex due to the high cooling rate associated with laser processing, which can accelerate the martensitic formation in HCS. The objective of this study is to investigate the significance of alloying composition and cooling rate on controlling the microstructure and mechanical properties of the laser welded HCS to SS joint. Along with experimentation, a finite element analysis (FEA) based numerical model was used to develop a heat treatment methodology that will produce a weld with optimum in-service performance.

2. Experimental procedure

The base materials used in this study were hyper-eutectoid high carbon steel (BS 4659B01) and stainless steel (AISI 316L) sheets with a thickness of 1mm, such as those commonly used for heat exchangers in petrochemical and refinery industries [13]. The chemical composition of the high carbon steel and the stainless steel is given in Table 1. The sample edges were cleaned and ground prior to welding and were positioned in full contact during the welding.

Elements	С	Si	Tu	Va	Mn	Р	S	Si	Cr	Ni	Mo	Nb	Fe
SS	0.03	-	-	-	2	0.01	0.03	1	18.02	10.15	2-3	0.09	Bal.
HCS	0.95	0.4	0.5	0.15	1.2	0.045	0.045	0.011	0.55	0.035	0.003	0.001	Bal.

Table 1 Chemical composition of parent metals in % wt [15]

Dissimilar conduction mode laser welds were made on 50×50×1mm metal sheets using a continuous wave (CW) carbon di-oxide (CO₂) laser. A schematic diagram of the laser welding set-up is shown Fig. 1. A coaxial nozzle with a focusing lens of 127mm focal length was used to focus the beam onto the specimen surface. The focus spot size of the laser beam was found to be 0.5mm with Gaussian intensity distribution, and the nozzle-workpiece stand-off distance was kept constant at 5mm. Initial trial experiments were carried out to identify feasible processing parameters for the laser welding of HCS to SS. Initial trial experiments showed optimal shielding with argon gas at 2bar gas pressure and 2l/min, and these parameters were used for all experimentation. A CNC controlled table was used to move the samples relative to the laser nozzle.

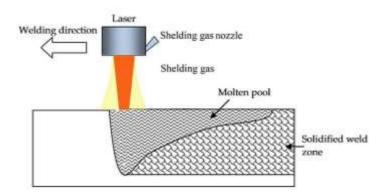


Fig. 1. Schematic diagram of a laser welding process

A total of 80 experiments were performed with various parameters as per table 2. Each experiment was repeated twice to confirm the repeatability. Various specific point energies (that will result in a wide range of cooling rate) were chosen, so as to investigate the influence of cooling rate on weld microstructure. The beam position with reference to the joint was shifted by up to ± 0.4 mm with an increments of 0.05mm, to study the influence the alloying concentration [8] on weld quality. The specific point energy was controlled based on the scanning speed with constant laser power [16] . Specific point energy (Equation 1) takes into account welding speed (*V*), laser beam diameter (*D*) and laser power (*P*) and is given by Eq.1 [16]:

Specific Point energy =
$$\frac{P \times D}{V}$$
 Eq. 1

	Speed (mm/s)	Power (W)	Specific point energy (J)	Beam offset (mm)		
1	5	500	50	±0.4mm, increments of 0.05mm		
2	7.5	500	33	±0.4mm, increments of 0.05mm		
3	10	500	25	±0.4mm, increments of 0.05mm		
4	12.5	500	20	±0.4mm, increments of 0.05mm		
5	15	500	17	±0.4mm, increments of 0.05mm		

Table 2 Laser dissimilar welding parameters used in present investigation

The cooling rates $\left(\frac{\partial T}{\partial t}\right)_{\chi}$ values used in this study were calculated from one dimensional heat transfer equation proposed by Adams Jr [17], which takes into account the effect of laser power (*P*), welding speed (*V*), thermal conductivity (*K*), liquidus temperature (*T*) and preheating temperature (*T*₀) and can be expressed as [18]:

$$\left(\frac{\partial T}{\partial t}\right)_{x} = \left(\frac{\partial T}{\partial x}\right)_{t} \left(\frac{\partial x}{\partial t}\right)_{T} = -2\pi K V \frac{(T-T_{0})^{2}}{P} \qquad Eq.2$$

The thermal conductivity (in W/(m $^{\circ}$ C)) of the weld zone in the cooling rate equation was calculated based on the alloying concentration (dilution) of the weld zone [8] and the preheating temperature was taken as room temperature (in $^{\circ}$ C). The cooling rates (Equation 2) were calculated for a liquidus temperature of 1450 $^{\circ}$ C.

The laser welded samples were prepared for metallographic analysis as per ASTM E3-11 standards [19]. Metallographic samples were etched using three etchants. The HCS side of the

weldment was etched using Nital 5% regent, stainless steel side was etched using Kalling's No.2 (5 g CuCl₂, 100 ml HCl, 100 ml ethanol), and the fusion zone was etched using (Ferric chloride 5g FeCl₃, 50 ml HCL, HNO₃). Microstructural characterizations of dissimilar joints were performed on their cross-sections using an optical microscopy and a scanning electron microscopy accompanied by energy dispersive x-ray spectroscopy. Vickers hardness profile of the weld metal and heat affected zone was measured using a KV400 micro-hardness tester with a load of 50g. XRD analyses were carried out in order to identify the phases of the samples and to determine their relative amount using the integral breadth method.

3. Results and Discussion

Fig. 2 illustrates the optical microstructure of a typical laser welded HCS-SS joint. Fig. 2a and 2b shows the optical microstructure of as received (parent material) SS and HCS respectively. The microstructure of HCS consists of fine pearlite and spheroidal cementite in a ferrite matrix, and SS contains equiaxed austenitic grains (γ).

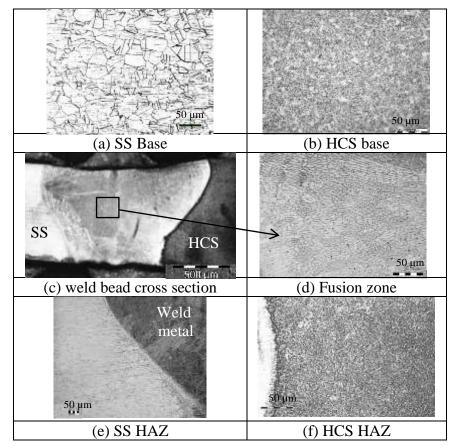


Fig. 2. Optical micrograph of the parent metals and microstructures gradient in the HAZ of HCS (power=500W, welding speed=10mm/s, beam offset=0mm)

Fig. 2c shows the dissimilar weld bead and Fig. 2d illustrates the fusion zone which is predominantly of columnar dendrites with nucleated fusion boundary. As noted from the figure, the microstructure of fusion zone was predominantly homogeneous, which is attributed to the high magnitude of melt pool convention in the fusion zone, which homogenizes the fusion zone microstructure [8]. Fig. 2e and 2f show the optical microstructure of the SS HAZ and the HCS HAZ respectively. The microstructure of the HCS HAZ shows significant variations, possibly attributed to the high thermal gradient and high carbon content in HCS. Also noted from the figure is that the microstructure variation is not significant in the HAZ of SS due to non-transformable nature of austenitic stainless steel [8]. Some austenite recrystallized grains was seen in the SS HAZ (Fig. 2e) but they are not of significant concern [20].

Table 3 summarises the key results of the experimentation (effect of the cooling rate and alloying element concentration on the consequent microstructure of the weld zone) performed using the parameters shown in table 2. The results were organised, so as to study the effect of alloying concentration with constant cooling rate, and the effect of cooling rate with constant alloying concentration. The alloying concentration (Cr%; Ni%) given in Table 3 was established through EDS analysis of the weld bead, and the microstructure was established by optical microscopy. The cooling rate given in Table 3 was calculated using equation 2. The variation of cooling rate with beam offset (alloying concentration) at each level of specific point energy was insignificant (0.009 ± 10^{6} °C/s) and an average was considered.

Specific		Average						
point	Cr 13%	Cr 11%	Cr 9.6%	Cr 7.37%	Cr 4%	cooling rate		
energy (J)	Ni 7%	Ni 6%	Ni 5.2%	Ni 3.8%	Ni 2.1%	$(10^{6} ^{\circ} C/s)$		
50	$(\gamma + \delta)$	$(\gamma + \delta)$	(<i>γ</i> + <i>M</i>)	(<i>γ</i> + <i>M</i>)	<i>(M)</i>	0.028		
	-0.4	-0.3	-0.25	0	0.1			
33	$(\gamma + \delta)$	$(\gamma + \delta)$	$(\gamma + M)$	(<i>γ</i> + <i>M</i>)	<i>(M)</i>	0.043		
	-0.35	-0.25	-0.1	0.1	0.15			
25	$(\gamma + \delta)$	$(\gamma + \delta)$	<i>(M)</i>	<i>(M)</i>	<i>(M)</i>	0.057		
	-0.3	-0.2	0	0.15	0.2			
20	$(\gamma + \delta)$	(γ+M)	<i>(M)</i>	<i>(M)</i>	<i>(M)</i>	0.071		
	-0.1	0	0.1	0.25	0.3	0.071		
17	$(\gamma + \delta)$	$(\gamma + M)$	<i>(M)</i>	<i>(M)</i>	<i>(M)</i>	0.085		
	0	0.15	0.2	0.3	0.4	0.085		
	$\gamma + \delta = A$							
	Martensitic							

Table 3 Effect of cooling rate and alloying concentration on weld microstructure

As can be seen from the table, three distinct microstructures of $(\gamma + \delta, \gamma + M, M)$ were noticed in the weld bead. Decrease in alloying content results in change of the microstructure from austenitic-ferritic $(\gamma + \delta)$ to completely martensitic (M). Fig. 3a, 3b and 3c illustrate the optical micrograph of various alloying elements at a constant cooling rate of 0.057×10^6 °C/s.

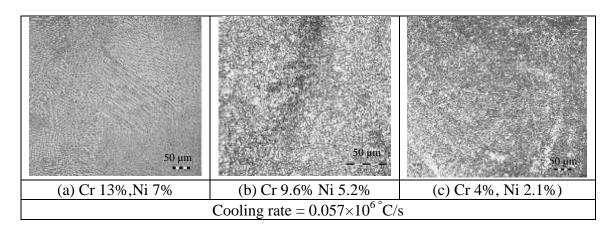


Fig. 3. Effect of alloying concentration on the microstructure (a) primary austenitic γ dendrites (light) with interdendritic δ ferrite, (b) Martensite, (c) Martensite

Fig. 4 shows the effect of cooling rate on microstructural variation at an alloying composition of Cr 9.6%, and Ni 5.2%. Variation of cooling rate from 0.028 to 0.085 (10^6 °C/s), resulted in transformation of microstructure from austenitic-martensitic (γ +*M*) to predominantly martensitic (*M*). However, at lower alloying concentration (below Cr 9.6%, Ni 5.2%), the effect of cooling rate on the final microstructure becomes much more significant, and experimental parameters at this range should be avoided.

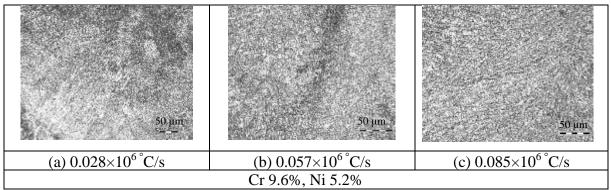
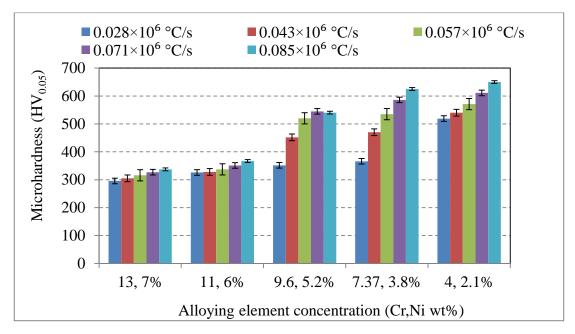
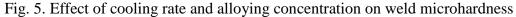


Fig. 4. Effect of cooling rate on the microstructure (a) austenitic-martensitic microstructure, (b) Martensite, (c) Martensite

The hardness measurement results shown in Fig. 5, confirm the observation made with optical microscopy (Table-3). As can be seen from the Fig. 5, increase in cooling rate resulted in

increased hardness values. However, the increase in hardness values at higher alloying level should be attributed to the finer grain structure of the austenite, while at low alloying level it is due to martensitic formation. Also, at higher alloying level, the alloying elements restrict the transition of the austenite phase and the microstructure remained predominantly austenitic-ferritic (γ + δ) irrespective of the cooling rate. The formation of martensite in HCS-SS joint can cause defects such as cracks in fusion zone which can undermine the service performance of the joint [21]. To achieve a weld bead of predominantly austenitic phase, it is essential to maintain higher alloying composition (greater than Cr 11%, Ni 6%) and cooling rate 0.057×10⁶ °C/s. Sample with 25J specific point energy and offset of -0.2 toward SS provided such optimum conditions.





The hardness profile along the middle of the welded joint for cooling rates of 0.028, 0.057, and 0.085×10^{6} °C/s, with a constant alloying composition of (Cr 11%, Ni 6%) is shown in Fig. 6. As can be seen, a significant spike in hardness was observed in the HCS HAZ. The high carbon content along with the formation of martensitic structure (as a result of high cooling rate involved in laser welding) in the HCS HAZ resulted in a spike in hardness at the HCS HAZ. Irrespective of the weld characteristic, the spike in hardness of the HAZ can result in poor joint performance [22].

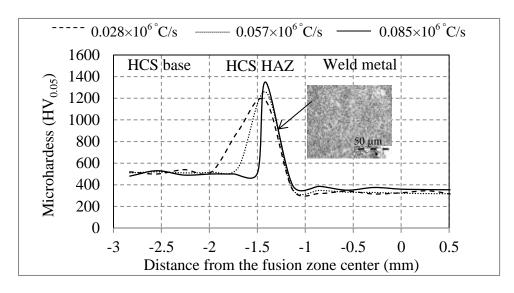


Fig. 6. Micro-hardness profile of the dissimilar weld at various cooling rates (Cr 11%, Ni 6%)

All the samples show similar results, and the spike in the HAZ hardness cannot be controlled just by changing the alloying concentration or fusion zone cooling rate. As noted from the results, laser parameters have very little effect on HAZ cooling rate and subsequent HAZ microstructure. Control of the cooling rate of the HAZ is essential to address the spike in the HCS HAZ, and heat treatment using additional source was identified as one of the method for control of the cooling rate.

A numerical model was developed based on finite element (FEA) formulation, to establish the optimum heat treatment methodology and resulting cooling rate of the HCS HAZ so as to address the martensitic formation. Detailed description of this model is beyond the present scope of this paper, however, the FE model and methodology of simulation is similar to the one discussed by Deng [22, 23]. The sequentially coupled thermal-metallurgical FEA model was [22, 24, 25] solved using ANSYS codes. The dimensions of the work piece considered in numerical analysis is same as described in section 2, and the thermo-physical properties can be noted from Attarha [26] and Lee [27]. In laser welding of HCS, the martensitic transformation of the solid material (HAZ) occurs during the cooling cycle, between 800°C and 500°C ($\nabla t_{8/5}$) [28]. A subroutine was used within the ANSYS code to relate $\nabla t_{8/5}$ of each node, to the martensite fraction obtained from HCS CCT diagrams [22]. A Gaussian heat flux was used to represent the laser beam and convection heat loss was taken into account on all the surfaces. A secondary heat source (as temperature boundary condition) was used in the FEA model to achieve the controlled cooling rate. The secondary heat source maintains the welded joint at 800°C till the end of welding cycle, and cools the joint with a controlled

cooling rate. After initial trials, three set of scenarios where investigated i.e. Case-I: uncontrolled cooling- same as experimentation ($\nabla t_{8/5}=0.1$ sec); Case-II: controlled cooling rate of $\nabla t_{8/5}=40$ sec; Case-III: controlled cooling rate of $\nabla t_{8/5}=140$ sec. The FEM analysis was performed for optimal welding condition, i.e. speed of 5mm/s, laser power of 500W and beam offset of 0.2mm. In-line with the experimental parameter, the laser spot diameter of the beam over the sample surface was maintained at 0.5 mm.

Fig. 7 shows the thermal history of the HAZ for various controlled cooling time ($\nabla t_{8/5}$). Fig. 8a-c shows the contour image of the martensitic fraction obtained for various controlled cooling times of 0.1s, 40s and 140s. The contour image was plotted after the substrate reaches the room temperature. As can be seen from the figure, controlling of the cooling time results in a significant decrease in martensite fraction (from 100% to 20%). The increase in controlled cooling time, promotes the diffusion of carbon atoms out of the crystal structure, resulting in less martensite formation [18].

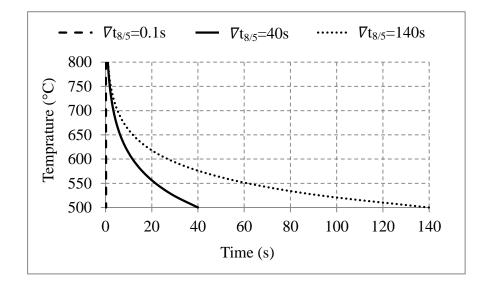
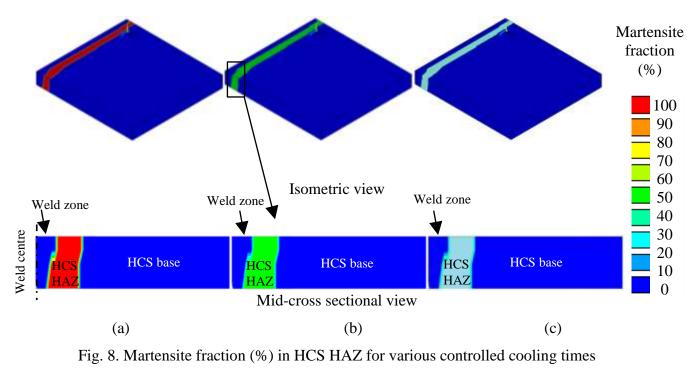


Fig. 7. Temperature cycle over the HCS HAZ weld for various controlled cooling time $(\nabla t_{8/5}=0.1s, 40s, and 140s)$



(a) $\nabla t_{8/5}=0.1$ s, (b) $\nabla t_{8/5}=40$ s and (c) $\nabla t_{8/5}=140$ s

Direct validation of the numerical simulation results (Case-II and III-with same heat treatment method) was beyond the scope of this study. However, experiments were performed using a stationary laser beam (similar to spot welding-but with varying power levels to follow the trend of the cooling rate in Fig. 7) which gives similar cooling rate at the HCS HAZ ($\nabla t_{8/5}$).

Fig. 9 shows the comparison of martensite fraction obtained from simulation and experimentation (X-ray diffractometer). In agreement with the experimental results, the FEA model predicts the decrease in martensitic fraction with increase in controlled cooling time ($\nabla t_{8/5}$). The decrease in the martensite volume fraction is attributed to the slower cooling rate, which provides sufficient time for the carbon to diffuse out of the crystal structure [29]. As can be seen from the Fig. 10, the optimum HCS HAZ hardness (650HV_{0.05} [18]) was obtained at the heat treatment time of $\nabla t_{8/5}$ =40s. Fig. 10 depicts the hardness profiles and optical microscopic image of the spot weld experimental sample with controlled cooling time

 $(\nabla t_{8/5})$ of 40s. The results of the hardness and optical metallography of heat treated HAZ agrees qualitatively with the FEA model.

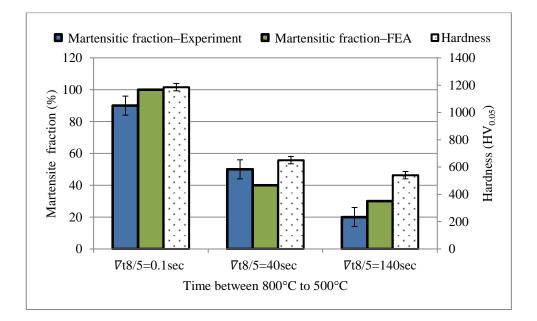


Fig. 9. Calculated and measured martensite fraction (%) in HCS HAZ

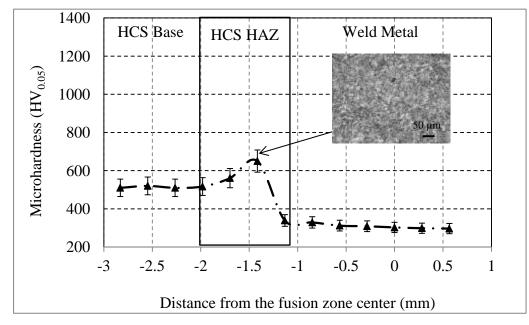


Fig. 10. Microhardness profile and optical micrograph of the HCS zone obtained with controlled cooling rate ($\nabla t_{8/5}$ =40s)

4. Conclusion

An experimental investigation was performed to establish the methodology of controlling the microstructure and mechanical properties of a laser welded joint between high carbon and stainless steel. The results obtained in this work are summarized below:

- This investigation has demonstrated the feasibility of producing a laser welded joint between high carbon steel and austenitic stainless steel that is predominantly homogeneous and of austenitic microstructure.
 - The alloying composition and cooling rate significantly influences the final microstructure of the dissimilar weld zone.
 - At normal laser welding conditions, hard brittle martensitic phase was observed in the HCS HAZ and cannot be controlled by varying the laser processing parameters.
 - The martensitic formation in HCS HAZ can be controlled by using suitable heat treatment methods and the optimal $\nabla t_{8/5}$ cooling time to achieve desirable HCS-SS welded joint was found to be around 40s.
 - FEA analysis can be used to estimate and control the martensitic fraction in laser welding of HCS.

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