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1 The hydrology of the proglacial zone of a high-Arctic glacier  
2 (Finsterwalderbreen, Svalbard): Sub-surface water fluxes and complete water budget.

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17

18 **Abstract**

19 Proglacial areas receive fluxes of glacial meltwater in addition to their own hydrological  
20 inputs and outputs, while in high latitudes the seasonal development of the active layer also  
21 affects their hydrology. This paper supplements a previous study of the surface and  
22 atmospheric water fluxes in the proglacial area of the Svalbard glacier Finsterwalderbreen  
23 (77° N), by focusing on the sub-surface water fluxes of the active layer, and bringing together  
24 all the components of the proglacial water balance over a complete annual cycle. Particular  
25 attention is given to the transitional zone between the moraine complex and the flat sandur.  
26 Sub-surface water in the moraine complex (sourced mainly from snowmelt, lake drainage and  
27 active-layer thawing), is exchanged with sub-surface water from the sandur (sourced mainly  
28 from glacier-derived snow- and icemelt), across a largely distinct boundary. Hydraulic head  
29 and specific discharge were monitored in a transect of wells spanning this boundary. A  
30 hydraulic gradient from the moraine complex to the sandur is maintained throughout the melt  
31 season, although this is reversed first briefly when glacial runoff floods the sandur, and then  
32 diurnally from mid-melt-season, as peak daily flow in the proglacial channel network drives  
33 sub-surface water in the sandur towards the moraine complex. It is estimated that the active  
34 layer does not freeze up until mid-December at this location, so that sub-surface water flow  
35 may be maintained for months after the cessation of surface runoff. However, the magnitude  
36 of sub-surface flow is very small: the total, annual flux from the moraine complex to the  
37 sandur is 11 mm, compared with 1073 mm of total, annual runoff from the whole catchment  
38 (glacier included). Furthermore, when considering the water balance of the entire proglacial  
39 area, there are unlikely to be significant, seasonal storage changes in the active layer.

40

41 **Key words** proglacial, active layer, hydraulic conductivity, water balance, water budget,  
42 Svalbard.

43 **PACS codes** 92.40.Vq, 92.40.We, 92.40.Zg

44

## 45 1. Introduction

46 Proglacial areas are expanding globally as a consequence of sustained glacier retreat (Zemp  
47 et al., 2008), and can be characterized as highly dynamic fluvial environments (Warburton,  
48 1999). Given the intractability of most proglacial areas, and the complex experimental design  
49 necessary for monitoring multiple hydrological fluxes over sustained periods in such dynamic  
50 environments, it is unsurprising that still very few comprehensive water balance studies are  
51 available for glacierized catchments as a whole, or for proglacial areas in particular. Water  
52 balances for glaciers themselves can be derived from mass-balance data assuming that inter-  
53 annual storage is insignificant (e.g. Hagen et al., 2003), but these shed little light on the  
54 hydrological functioning of catchments, and on the interaction and relative contributions of  
55 different drainage pathways and potential stores. As water and sediment fluxes from glaciers  
56 globally are likely to increase over the coming decades (ACIA, 2004; Meehl et al., 2007) an  
57 enhanced understanding of the hydrological functioning of proglacial areas would be  
58 beneficial: the purpose of this paper is to contribute to this understanding – building on a  
59 previous paper which dealt with surface and atmospheric water fluxes in a proglacial area in  
60 the Norwegian high-Arctic archipelago of Svalbard (Hodgkins et al., 2009) – by analyzing  
61 sub-surface (active-layer) water fluxes and bringing together the complete water balance over  
62 an annual cycle.

63 Studies of sub-surface hydrology in Svalbard have tended to focus on sub-permafrost  
64 groundwater (e.g. Haldorsen et al., 1996; Booji et al., 1998; Haldorsen and Heim, 1999), with  
65 relatively little attention paid to water flow within the active layer. However, results from  
66 several hydrochemical studies suggest that the annual formation of the active layer is  
67 hydrologically significant: observations indicate that the annual formation of the active layer  
68 in Svalbard typically commences following snowpack recession in early June (Herz &  
69 Andreas, 1966; Stäblein, 1971), when mean air temperatures begin to rise consistently above  
70 zero (Hanssen-Bauer et al., 1990). Downward-thawing velocities are initially high, although

71 variations in microtopography and the persistence of patchy snow cover may result in the  
72 development of an irregular permafrost table with thawed troughs and frozen ridges, though  
73 this irregularity tends to even out as the melt season progresses. The potential for sub-surface  
74 water storage and flow in the active layer increases in line with the gradual increase in the  
75 depth of the permafrost table, which constitutes the lower boundary layer for water  
76 movement (Pecher, 1994). Sub-surface flow in the active layer may increasingly contribute to  
77 throughputs of runoff in the proglacial zone as the melt season progresses (Pecher, 1994;  
78 Hodson et al., 1998); this effect may be enhanced following precipitation events, due to the  
79 displacement of sub-surface water by infiltrating precipitation.

80 Available studies indicate that Arctic catchments often exhibit a pattern in which  
81 runoff appears significantly to exceed precipitation (Killingtveit et al., 2003). This can be  
82 attributed to a combination of measurement errors, non-representative locations of  
83 precipitation stations, and net glacial ablation. Førland et al. (1997) considered that  
84 precipitation underestimation for upland areas by coastally-located gauges may fully account  
85 for the discrepancy between precipitation measured at Ny-Ålesund and runoff from the  
86 nearby Bayelva catchment. Groundwater storage has often been regarded as insignificant in  
87 glacierized catchments in Svalbard (e.g. Hagen et al., 2003), usually owing to the presence of  
88 permafrost, although there is little evidence available and groundwater springs are not  
89 unusual (Haldorsen and Heim, 1999). With regards to the active layer itself, the observation  
90 that total evaporation at elevations <50 m above sea level (a.s.l.) in Svalbard may exceed  
91 precipitation by up to about 160% during the summer indicates that water storage there is  
92 often sufficient to maintain the rate of evaporation during dry periods (Harding and Lloyd,  
93 1997).

94

## 95 1.1. Aims

96           The purpose of this paper is to quantify and analyze the sub-surface hydrology of the  
97 proglacial area of a high-Arctic glacier, focusing in general on water fluxes in the active  
98 layer, and in particular on the transitional zone between the moraine complex and the sandur  
99 (see Section 2, ‘Study site description’). Time series of both active layer development and of  
100 hydraulic head in the active layer were acquired by in-situ monitoring over the course of the  
101 1999 melt season, in order to elucidate sub-surface hydraulic gradients and flow paths in the  
102 transitional zone. The saturated hydraulic conductivity of the sediments comprising the active  
103 layer was assessed, in order to enable the time series of hydraulic head to be used to  
104 determine specific discharge at the boundary between the moraine complex and the sandur,  
105 and thus facilitate the calculation of total sub-surface water fluxes to and from the moraine  
106 complex. These fluxes will then be combined with previously-determined surface and  
107 atmospheric fluxes (Hodgkins et al., 2009) to present a comprehensive, annual, proglacial  
108 water balance.

109

## 110 2. Study site description

111           The proglacial zone of Finsterwalderbreen is located at 77° 31′ N, 15° 19′ E in the  
112 Norwegian High Arctic archipelago of Svalbard (Fig. 1). It is part of a catchment situated on  
113 the southern side of Van Keulenfjorden which drains northwards to the sea from a maximum  
114 elevation of 1065 m a.s.l. The catchment is constrained to the east, south and west by high  
115 mountain ridges, and has a total area of 65.7 km<sup>2</sup>, of which 43.5 km<sup>2</sup> is currently glacierized.  
116 The non-glacierized part of the catchment comprises steep, scree-covered mountain slopes,  
117 with the exception of the proglacial zone itself, which consists of a flat sandur (mostly  
118 between 10–20 m a.s.l.) surrounded by a moraine complex (mostly between 20–50 m a.s.l.),  
119 situated between the glacier terminus and the coastline of Van Keulenfjorden (Fig. 1). The  
120 characteristics of the proglacial zone have been described in detail in Hodgkins et al. (2009).

121 Of particular interest for this paper is the transitional zone between the moraine complex and  
122 the sandur: the former consists of a series of compounded ridges (marking the limits of  
123 previous advances) enclosing a hummocky terrain of kames and kettles (many of which  
124 contain small lakes) composed largely of glacial diamicton, interspersed with relict outwash  
125 terraces; the latter is a relatively uniform, low-gradient surface, composed largely of fluvial  
126 sediments, across which glacier meltwater streams braid extensively (Fig. 1). Sub-surface  
127 waters from the moraine complex, sourced mainly from snowmelt, lake drainage and active-  
128 layer thawing, are exchanged with those from the sandur, sourced mainly from glacier-  
129 derived snow- and icemelt, across the largely distinct boundary between the two; this  
130 exchange was the focus of field measurements, described in Section 3.

131

### 132 3. Methods: Determination of sub-surface water fluxes between the moraine complex 133 and the sandur

#### 134 3.1. Hydraulic head monitoring

135 Hydraulic head was monitored for a total of 36 days, from 19:00 on day 192 (11 July)  
136 to 11:00 on day 227 (15 August). At the start of the monitoring period, five PVC-tube  
137 monitoring wells (Fig. 2) were sited along a gently-sloping transect spanning the transitional  
138 zone, approximately 1 km downstream from the glacier terminus (Fig. 1). The characteristics  
139 of these wells have been described in detail by Cooper et al. (2002), in a study of the  
140 hydrochemistry of waters in the active layer. Following a period of equilibration, Druck  
141 PDCR1830 pressure transducers were used to sample pressure head in each well at 20-s  
142 intervals, and record hourly means (potential error  $\pm 0.1\%$ ). Pressure-head values were  
143 calibrated with a measurement of elevation head derived from field surveying, to give the  
144 record of hydraulic head. No significant net change in the elevation of the sandur due to  
145 aggradation or degradation was detected at the wells transect (with one exception, noted in  
146 Section 4.1). The potential error range for hydraulic head is estimated to be  $\pm 5\%$ . Active

147 layer depth during the monitoring period was measured every 2–6 days by driving a steel  
 148 stake into the ground at each well, until the resistance of the uppermost surface of the  
 149 permafrost was encountered (estimated error range  $\pm 5\%$ ).

150

### 151 3.2. Saturated hydraulic conductivity testing

152 The saturated hydraulic conductivity ( $K_{sat}$ ) of the sediments comprising the active  
 153 layer in the transitional zone is required to determine specific discharge, and hence quantify  
 154 sub-surface water fluxes.  $K_{sat}$  ( $\text{m s}^{-1}$ ) was assessed using falling-head slug tests in the  
 155 monitoring wells (Bouwer and Rice, 1976; Bouwer, 1989) and determined from

$$156 \quad K_{sat} = \frac{R_i^2 \ln(L_r/R_e)}{2L_i} \frac{1}{t} \ln\left(\frac{\psi_0}{\psi_t}\right) \quad (1)$$

157  
 158 where  $R_i$  and  $R_e$  are the internal and external radii of the well tubing respectively (m),  $L_r$  is  
 159 the effective radius over which the increase in pressure head is dissipated (m),  $L_i$  is the length  
 160 of the screened intake through which water can enter (m),  $t$  is the time since  $\psi = \psi_0$  (s),  $\psi$  is  
 161 pressure head in the well (m),  $\psi_0$  is the maximum displacement in pressure head at time  $t = 0$   
 162 (m) and  $\psi_t$  is the displacement in pressure head at  $t = t$  (m) (Bouwer and Rice, 1976). As  $L_r$  is  
 163 unknown, the dimensionless ratio  $\ln(L_r/R_e)$  was estimated from

$$164 \quad \ln\frac{L_r}{R_e} = \left\{ \frac{1.1}{\ln(L_w/R_e)} + \frac{a + b \ln[(L_b - L_w)/R_e]}{L_i/R_e} \right\}^{-1} \quad (2)$$

165  
 166  
 167 where  $L_w$  is the distance from the bottom of the well to the water table (m),  $a$  and  $b$  are  
 168 dimensionless functions of  $L_i/R_e$  and  $L_b$  is the distance from the water table to the upper  
 169 surface of the permafrost (m) (Bouwer, 1989).  $K_{sat}$  values obtained in this way ranged from  
 170  $6.01 \times 10^{-5} \text{ m s}^{-1}$  for sandur sediments to  $4.08 \times 10^{-4} \text{ m s}^{-1}$  for moraine complex sediments.

171

172



173 3.3. Specific discharge and sub-surface water flux calculation

174 Sub-surface water fluxes,  $Q$  ( $\text{m}^3 \text{s}^{-1}$ ) (Fig. 3A), were determined as the product of  
175 mean hourly values of specific discharge ( $\text{m s}^{-1}$ ) at the well situated closest to the boundary  
176 between the moraine complex and the sandur (Well 4) and the cross-sectional area of that  
177 boundary,  $A$  ( $\text{m}^2$ ), using

$$178 \quad Q = \left( K_{\text{sat}} \frac{dH}{dL} \right) A \quad (3)$$

179

180 where  $dH/dL$  is the hydraulic gradient between Wells 4 and 5, determined by dividing the  
181 difference in mean hourly values of hydraulic head by the distance between the wells, and  $A$   
182 is determined by multiplying the saturated layer depth  $L_b$  (m) by the moraine complex-sandur  
183 boundary length (7000 m): given the flat nature of the sandur, it is probably reasonable to  
184 assume that all of the boundary is active concurrently. Hourly values of  $L_b$  were determined  
185 from

$$186 \quad L_b = \psi + (L_a - L_s) \quad (4)$$

187

188 where  $L_a$  is the depth of the active layer (m) (the distance from the ground surface to the  
189 upper surface of the permafrost) and  $L_s$  is the distance from the bottom of the well to the  
190 ground surface (m).

191

192 3.4. Unmonitored sub-surface water fluxes

193 As with the surface and atmospheric water fluxes at Finsterwalderbreen discussed in  
194 Hodgkins et al. (2009), monitoring of hydraulic head and active layer development  
195 commenced some time after the onset of the thaw associated with the 1999 melt season, and  
196 ceased some time before the annual freeze-up. Sub-surface water fluxes during these missed  
197 intervals may have been significant, particularly during the latter period, since the  
198 relationship between decreasing air temperature and refreezing is subject to the zero-curtain

199 effect, whereby the release of latent heat stabilizes the temperature of the active layer at 0 °C  
200 for a prolonged period, delaying the progression of the freezing front (Boike et al., 1998).  
201 However, the development of a robust annual hydrological budget requires these missed  
202 fluxes to be quantified.

203 The first step was to estimate variation in the thickness of the active layer during the  
204 pre-monitoring interval. Monitoring-interval data exhibited an almost perfect linear  
205 relationship between cumulative, positive, hourly air temperature and active layer depth at all  
206 five of the monitoring wells ( $R^2$  values >0.99 in all cases), reflecting the dominance of  
207 conductive heat transfer during the melt season. Active layer development at Well 4 was  
208 therefore predicted using a linear regression model, constructed from all available input terms  
209 for the interval during which active layer depths were monitored, i.e. days 192–227 (11 July–  
210 15 August). The second step was to model the freeze-back of the active layer following the  
211 cessation of monitoring. Freeze-back at Well 4 was again predicted using regression models,  
212 based on significant linear relationships between cumulative, negative, hourly air temperature  
213 and the progression of the downward- and upward-moving freezing fronts in the active layer  
214 at a comparable site in Svalbard during this interval (Roth and Boike, 2001). Daily,  
215 unmonitored, sub-surface water fluxes were then estimated by multiplying values of  
216 estimated  $L_b$  (a linear function of active layer depth, again using input terms from the  
217 monitoring interval – see Equation 4) by the mean value of specific discharge determined  
218 during the period of monitoring. A summary of the regression models is provided in Table 1.

219

## 220 4. Results: Sub-surface water fluxes between the moraine complex and the sandur

### 221 4.1. Temporal variation in hydraulic head and specific discharge

222 The temporal pattern of hydraulic head during the period of monitoring (Fig. 3A) was  
223 characterised by three periods of markedly different behaviour:

224 (1) From day 192–196 (11–15 July), hydraulic-head values in those wells sited in the moraine  
225 complex (Wells 4 and 5) were high and relatively invariable, while values on the sandur  
226 (Well 3) were lower and more variable (Fig. 3A; note that Wells 1 and 2 are excluded from  
227 the figures and discussion, as their behaviour was almost identical to that of Well 3, so they  
228 add no additional insight); a hydraulic gradient was maintained from the moraine complex to  
229 the sandur throughout this period.

230 (2) From day 197–209 (16–28 July), water levels in all of the wells were somewhat higher  
231 and more variable than previously. Peak seasonal values of hydraulic head in all of the wells  
232 were recorded in the interval from day 199–202 (18 July–21 July), when the surface of the  
233 sandur became flooded in response to peak seasonal flow in the proglacial channel network  
234 (Wadham et al., 2001; Hodgkins et al., 2009). During this interval, hydraulic-head values in  
235 Wells 3 and 4 periodically exceeded those in Well 5, reversing the hydraulic gradient from  
236 the moraine complex to the sandur. As the floodwaters subsided, it became apparent that the  
237 surface of the sandur had been eroded between Wells 3 and 4, forming a depression into  
238 which channel waters were able to flow.

239 (3) From day 210–227 (29 July–15 August), water levels in Well 3 were elevated in  
240 comparison to interval 1, reflecting the routing of a greater proportion of flow down the  
241 western margin of the sandur following the peak seasonal, proglacial flow. A greater degree  
242 of diurnal variability was recorded in Wells 3 and 4 during interval 3, along with significant  
243 temporal variation in peak daily values of hydraulic head. While peak daily hydraulic-head  
244 values in Well 4 closely tracked the diurnal pattern of flow in the proglacial channel network  
245 with a 1–2 hour delay, those in Well 3 typically exhibited a 10–14 hour delay. Since similar  
246 values of hydraulic head were maintained in Wells 3 and 4 throughout this period, the  
247 temporal variation in peak daily values resulted in the reversal of the hydraulic gradient on  
248 the sandur on a daily basis. However, consistently high values of hydraulic head in Well 5

249 maintained an overall hydraulic gradient from the moraine complex to the sandur throughout  
250 this interval.

251 Time series of specific discharge at Well 4 are presented in Fig. 3B. The pattern of  
252 specific discharge during the period of monitoring was characterised by a trend of fairly  
253 constant discharge (ranging from  $2.10 \times 10^{-7} \text{ m s}^{-1}$  to  $1.64 \times 10^{-6} \text{ m s}^{-1}$ ), punctuated by a short  
254 period of recharge (peak value  $-1.14 \times 10^{-6} \text{ m s}^{-1}$ ), which occurred in response to peak  
255 seasonal flow in the proglacial channel network and reflects the temporary reversal of the  
256 hydraulic gradient. The greater degree of diurnal variability in discharge following the period  
257 of recharge reflects the daily inflow and outflow of channel waters to and from the depression  
258 formed between Wells 3 and 4. High values of peak daily discharge of  $\sim 1.40 \times 10^{-6} \text{ m s}^{-1}$  on  
259 days 221 (9 August) and 226 (14 August) reflect elevated water levels in the moraine  
260 complex following heavy rainfall (Hodgkins et al., 2009: Fig. 2).

261

#### 262 4.2. Daily and cumulative sub-surface water fluxes

263 Active layer depth at each well increased linearly throughout the period of  
264 monitoring, at a rate of  $\sim 0.01 \text{ m d}^{-1}$  (Fig. 4A). Significant spatial variation in active layer  
265 depth was observed on the sandur, reflecting local variations in channel proximity and  
266 thermal erosion. Despite the deepening of the active layer, water levels in the wells sited in  
267 the moraine complex remained relatively constant, resulting in a progressive increase in the  
268 thickness of the saturated layer as the season progressed.

269 Total daily sub-surface water fluxes are presented in Fig. 4B. A total cumulative sub-  
270 surface water flux of  $9.24 \times 10^3 \text{ m}^3$  was discharged from the moraine complex to the sandur  
271 during the 34-day period from days 193–226 (12 July–14 August). Total daily sub-surface  
272 water fluxes were positive throughout this time interval, except for on day 199 (18 July),  
273 when  $2.04 \times 10^2 \text{ m}^3$  was recharged to the moraine complex from the sandur. Very low positive  
274 total daily sub-surface water fluxes during the following 2 days reflect shorter, subsequent

275 periods of recharge. The highest total daily sub-surface water flux was recorded on day 226  
276 (14 August), when  $4.69 \times 10^2 \text{ m}^3$  (about 5% of the total cumulative sub-surface water flux)  
277 was discharged from the moraine complex to the sandur following heavy rainfall.

278 Total sub-surface water fluxes outside the monitoring period were estimated as the  
279 product of the number of missed days of monitoring and the mean daily sub-surface water  
280 flux measured during the period of monitoring ( $2.72 \times 10^2 \text{ m}^3$ ). The number of missed days  
281 was estimated by subtracting the number of days in the period of monitoring (34) from the  
282 number of days during which mean daily air temperatures were consecutively positive: 107  
283 days from 5 June–19 September (Hodgkins et al., 2009: Fig. 2). A cumulative total sub-  
284 surface water flux of  $1.99 \times 10^4 \text{ m}^3$  is therefore estimated to have been discharged from the  
285 moraine complex to the sandur outside the period of monitoring. Adding this missed total to  
286 the monitored total gives a total annual sub-surface water flux of  $2.91 \times 10^4 \text{ m}^3$ , of which  
287 about 32 % was monitored.

288

### 289 4.3. Sub-surface water flux uncertainties

290 Various sources of potential error have been identified concerning the calculation of  
291 sub-surface water fluxes, including those associated with the use of instrumentation, field  
292 techniques and extrapolation in both space and time. Of these potential sources of error, some  
293 are quantifiable and thus susceptible to probabilistic analysis, while others are systematic and  
294 more difficult to constrain. For example, the disturbance associated with digging and then  
295 back-filling holes for the installation of the monitoring wells into the coarse-grained  
296 sediments of the moraine complex probably affected the saturated hydraulic conductivity of  
297 the surrounding sediments, but to what extent is unknown. Furthermore, with regard to  
298 upscaling from specific-discharge estimates at set points on the boundary between the  
299 moraine complex and the sandur to sub-surface water flux estimates for the boundary as a  
300 whole, it is acknowledged that values of saturated hydraulic conductivity probably vary

301 significantly across the moraine complex, and that the depth of the active layer and thickness  
302 of the saturated layer also probably exhibit significant spatial variability.

303 In view of the above, the sub-surface water fluxes must be viewed as first-order  
304 estimates and treated with an appropriate degree of caution, given that it is not possible to  
305 determine realistic error estimates with the data available. However, in order to assess the  
306 robustness of the flux estimates, a sensitivity analysis was conducted, based on Equation 3,  
307 and presented in Table 2. For this analysis, values of the three parameters  $K_{sat}$ ,  $dH/dL$  and  $L_b$   
308 were varied between  $-50\%$  to  $+50\%$  of the measured/modelled values used to determine the  
309 fluxes presented in Section 4.2. The modified values were then used to re-calculate the total  
310 annual sub-surface flux (because of the linear form of the equation, varying any of the three  
311 parameters by the same proportion has an identical numerical outcome). In addition, fluxes  
312 were re-calculated assuming that the length of the hydrologically-active boundary between  
313 the moraine complex and the sandur was either constant (at 7000 m, as assumed for the  
314 fluxes presented in Section 4.2) or varied linearly, between zero and the seasonal maximum  
315 (7000 m) from the start of drainage to 1 July, and from 1 October to end of drainage. From  
316 the results given in Table 2, it seems unlikely that the calculated sub-surface flux is in error  
317 by an order of magnitude, based on errors in measured/modelled saturated hydraulic  
318 conductivity, hydraulic gradient and saturated layer depth. Furthermore, varying the length of  
319 the boundary that is hydrologically active has only a minor effect on the calculated fluxes, as  
320 its impact is greatest when the rate of sub-surface discharge is smallest: early or late in the  
321 melt season, or during the long period of recession flow after the cessation of surface melt.

322

## 323 5. Discussion:

### 324 5.1. The annual, proglacial, sub-surface hydrological regime at Finsterwalderbreen

325 The results presented in Section 4 provide quantitative insights into hydrological  
326 pathways in proglacial areas underlain by permafrost. The annual cycle in proglacial

327 atmospheric and surface water fluxes at Finsterwalderbreen was described in detail in  
328 Hodgkins et al. (2009). We are able here to develop that description with detail of the  
329 variation in sub-surface water fluxes, which are rarely measured in glacierized environments.  
330 This description can be used as a context for understanding both the hydrological functioning  
331 of high-latitude, glacierized catchments and material fluxes from such catchments (e.g.  
332 Wadham et al., 2000; Cooper et al., 2002; Hodgkins et al., 2003).

333         The annual formation of the active layer commences following the recession of the  
334 snowpack, although persistent snow patches may initially delay thawing in some areas.  
335 Active layer formation in the Finsterwalderbreen proglacial area is estimated to have  
336 commenced around 14 June in 1999. As the melt season proceeds, lake levels in the moraine  
337 complex fall in response to the gradual deepening of the active layer and resultant water loss.  
338 Consequently, an increasing proportion of runoff is routed from the moraine complex to the  
339 sandur via sub-surface flow paths, resulting in the gradual disappearance of many ephemeral  
340 surface channels, and a dominant, sub-surface hydraulic gradient from moraine complex to  
341 sandur becomes established.

342         Peak seasonal flow in the proglacial, surface channel network tends to occur in mid-  
343 to-late July in this location, in response to high rates of ablation on the lower reaches of the  
344 main glacier; it may be accompanied by subglacial outburst floods, submerging the sandur for  
345 several days at a time (Wadham et al., 2001). The impact of such events on sub-surface flow  
346 is significant, since the dominant hydraulic gradient from the moraine complex to the sandur  
347 is temporarily reversed, allowing floodwaters from the proglacial channel network to  
348 recharge sub-surface water levels in the active layer at the boundary zone of the moraine  
349 complex. During preceding and succeeding periods of lower flow, the hydraulic gradient is  
350 maintained from the moraine complex to the sandur, although the gradient beneath the sandur  
351 itself is reversed diurnally, in response to diurnal flow variations in the proglacial channel  
352 network. The rate of sub-surface discharge from the moraine complex increases as the melt

353 season proceeds, reflecting the progressive deepening of the active layer and the supply of  
354 water from the interior of the moraine complex. A degree of flushing occurs following  
355 periods of rainfall, as infiltrating precipitation displaces water stored in the active layer.

356 The refreezing of the active layer commences in early-to-mid October, as two  
357 freezing waves begin to advance: one from the ground surface and one from the permafrost  
358 table (Marlin et al., 1993). However, complete refreezing may take 6–8 weeks, since the  
359 release of latent heat upon freezing offsets the initial drop in temperature (French, 2007). This  
360 temporal pattern appears to be typical for high-latitude, permafrost-influenced catchments.  
361 For instance, Humlum (1998) found that seasonal maximum thaw depth in the active layer  
362 was reached in late September at Qeqertarsuaq, Greenland (69° 15' N, mean annual air  
363 temperature –5.1° C) and that the closure of the active layer occurred between late December  
364 and late January. In the somewhat more northerly Finsterwalderbeen proglacial area, closure  
365 is estimated to have occurred around 11 December in 1999 (Fig. 4A).

366

## 367 5.2. The complete (atmospheric, surface and sub-surface) annual proglacial 368 hydrological budget at Finsterwalderbeen

369 The results presented in this paper, in combination with those presented in Hodgkins  
370 et al. (2009), also enable the complete, annual hydrological budget of the proglacial zone to  
371 be determined. This allows the relative importance of the various hydrological pathways in  
372 the proglacial zone to be identified. The annual, steady-state hydrological budget of the  
373 proglacial zone may be represented by the simple water-balance model

374

$$375 \quad W_{PZ} = W_P + W_R - W_E - W_{SSS} - W_{SR} \pm \Delta W_S \quad (5)$$

376

377 where  $W_{PZ}$  is the net proglacial water flux,  $W_P$  is the precipitation water flux,  $W_R$  is the  
378 channel recharge water flux (active-layer discharge from the sandur to the moraine complex),



379  $W_E$  is the evaporation water flux,  $W_{SSS}$  is the sub-surface seepage water flux (active-layer  
380 discharge from the moraine complex to the sandur),  $W_{SR}$  is the surface runoff water flux  
381 (mainly snowmelt and lake drainage from the moraine complex) and  $\Delta W_S$  is the change in  
382 water storage. A schematic of this model is presented in Fig. 5, with the addition of both  
383 glacial runoff, which effectively constitutes a proglacial throughput, and bulk runoff, which is  
384 the sum of glacial runoff and the net proglacial water flux. Specific values of the water  
385 balance terms are also given in Table 3. In both cases, the water fluxes given are annual  
386 totals, derived from the data presented in this paper and in Hodgkins et al. (2009), with the  
387 exception of the value for surface runoff from the moraine complex, which was determined  
388 by balance, assuming zero change in water storage.

389 In the year studied, precipitation exceeded evaporation by a little over 80%, though  
390 during the summer season, the evaporation rate was almost five times that of precipitation.  
391 Runoff was simply determined here as precipitation minus evaporation, as monitoring the  
392 extensive network of small, surface streams draining the moraine complex was not a feasible  
393 task. The value of runoff ( $104 \text{ mm a}^{-1}$ ) is small compared to other Svalbard values given by  
394 Killingtveit et al. (2003), though this can be explained by the inclusion of glacial runoff in  
395 those other values. However, assuming no significant storage changes, the water budget  
396 balances without any obvious difficulties or anomalies, so there is no indication of an  
397 apparent precipitation deficit, as identified at some other Arctic catchments: again, this may  
398 be partly attributable to the separation of glacial water fluxes from specifically proglacial  
399 ones in this study. Killingtveit et al. (2003) considered the main uncertainties in high-latitude  
400 water balances to be: (1) the distribution of precipitation, and (2) the rate of evaporation.  
401 Regarding (1), the Finsterwalderbreen proglacial area has a limited elevation range (10–50 m  
402 a.s.l., the maximum being moraine crests of limited spatial extent), so minimal extrapolation  
403 is required, but the hummocky topography of the moraine complex contributes to the  
404 relatively large uncertainty in winter precipitation, in particular; this is reflected in the large,

405 proportional error term for the precipitation flux in Fig. 5. Regarding (2), the modelled rate of  
406 evaporation from the proglacial area of Finsterwalderbreen ( $141 \text{ mm a}^{-1}$ ) compares  
407 favourably with other estimates from non-glacierized (and the non-glacierized parts of  
408 glacierized) Svalbard catchments, which are in the range  $51\text{--}200 \text{ mm a}^{-1}$  (Jania and Pulina,  
409 1994; Killingtonveit et al., 1994; Bruland, 2001; Mercier, 2001). Killingtonveit et al. (2003)  
410 determined average annual evaporation (as a function of air temperature, based on  
411 evaporation pan measurements at Ny-Ålesund) for glacier-free areas at three locations in  
412 Svalbard to be about  $80 \text{ mm a}^{-1}$ .

413 The notable exclusion from the water-balance model is the contribution to total, annual  
414 glacial runoff by over-winter subglacial drainage. However, a reliable estimate for this value  
415 may be derived by calculating the water-equivalent volume of the proglacial icing, which  
416 typically accumulates over an area of about  $0.3 \text{ km}^2$ . Previous coring investigations have  
417 revealed that the icing typically has a mean thickness of  $1.5 \text{ m}$  (Wadham et al., 2000).  
418 Assuming an ice density of  $900 \text{ kg m}^{-3}$ , a water-equivalent volume of about  $4.05 \times 10^5 \text{ m}^3$  of  
419 winter subglacial drainage is implied. This estimate equates to  $<1\%$  of average annual glacial  
420 runoff and is therefore unlikely to be a significant source of error through its contribution to  
421 storage changes. Neither is there any indication of significant changes in active-layer water  
422 storage; the magnitude of the sub-surface water flux is an order of magnitude smaller than the  
423 atmospheric and surface fluxes, and fully two orders of magnitude smaller than the bulk  
424 catchment runoff (Table 3).

425

## 426 6. Conclusions

427 Understanding the water balance of glacierized catchments is important both for furthering  
428 scientific understanding of the hydrological functioning of snow- and ice-fed systems at a  
429 time of rapid environmental change, and for the management of snow- and ice-derived water  
430 resources of the world's major mountain chains, likewise in the context of change (Barnett et

431 al., 2005; Bates et al., 2008). Even in high latitudes, remote from centres of population,  
432 changes in the storage and release of freshwater may have important implications for the  
433 functioning of aquatic ecosystems, ocean currents and ice-sheet stability (Das et al., 2008;  
434 Hanna et al., 2008; Mernild et al., 2008; Milner et al., 2009; Schofield et al., 2010).

435 This contribution has demonstrated that active-layer depth, hydraulic head and specific  
436 discharge may be successfully monitored as part of a water balance study in permafrost-  
437 influenced catchments. There are a range of practical limitations necessarily associated with  
438 monitoring sub-surface processes in remote and relatively intractable areas such as the  
439 Finsterwalderbreen catchment in Svalbard, but some aspects of the environment compensate  
440 for these: for instance, the air temperature-active-layer depth relationship is very linear,  
441 allowing early-season thawing and late-season freezing to be modelled quite  
442 straightforwardly. The active layer itself responds quite sensitively to forcing from proglacial  
443 surface hydrology, with diurnal reversals of the hydraulic gradient between the moraine  
444 complex and the sandur taking place from the mid-melt-season onwards, and clear flux peaks  
445 related to rainfall.

446 The results obtained are consistent with previous water balance studies from Svalbard,  
447 though this contribution is distinctive in quantifying active-layer fluxes, although the total  
448 annual flux from the moraine complex to the sandur, at 11 mm, is very small compared to the  
449 total annual catchment runoff, at 1073 mm. While the total water balance was determined  
450 assuming no significant changes in any plausible stores, the consistency of the various  
451 measured or estimated values for the balance components suggests there are unlikely to be  
452 significant gains from or losses to storage in the active layer. Uncertainties in the sub-surface  
453 variables are difficult to quantify, although given the small magnitude of the annual totals, are  
454 unlikely to have an important effect on the water balance calculation. Probably the principal  
455 source of uncertainty is the representativeness of the location used for well monitoring: this is  
456 essentially a matter of judgement. In any case, it is clear that throughputs from the adjacent

457 glacier – 1697 mm of runoff in the season studied (Hodgkins et al., 2009) – dominate the  
458 proglacial area hydrologically, underlining the important role of glacially-derived water  
459 fluxes in this high-latitude region.  
460

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469

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572

573 Figure captions

574

575 Fig. 1. Location of the study site within the Svalbard archipelago (inset) and configuration of  
576 the Finsterwalderbreen proglacial area (main). The limits of the moraine complex are shown  
577 with a solid white line; the part of the moraine complex that drains to the sandur is delimited  
578 by the long-dashed line; the boundary between the moraine complex and sandur is shown by  
579 the short-dashed line. WT marks the position of the wells transect, along which five wells are  
580 located (Fig. 2A). Aerial photograph acquired by UK Natural Environment Research Council  
581 Airborne Research and Survey Facility in 2003.

582

583 Fig. 2. (A) Detail map of the wells transect, located in Fig. 1. Wells 1 and 2 behave so  
584 similarly to Well 3 that their data are excluded from subsequent figures, for clarity. (B)  
585 Example of a monitoring well, comprising a pair of rigid, plastic tubes, the bottoms of which  
586 are sealed; the buried length of each tube features a screened intake into which sub-surface  
587 waters can flow. One tube was used for water sampling for hydrochemical studies (Cooper et  
588 al., 2002), while the monitoring instruments described in the text are secured at the bottom of  
589 the other tube: further details are given in Cooper et al. (2002).

590

591 Fig. 3. Temporal variation in (A) hydraulic head and (B) specific discharge during the period  
592 of monitoring. Well 4 is in the transitional zone between the moraine complex and the  
593 sandur; Well 5 is representative of the former, Well 3 of the latter. Note that positive values  
594 indicate discharge from the moraine complex to the sandur and negative values indicate  
595 recharge from the sandur to the moraine complex.

596

597 Fig. 4. Proglacial active layer depth/thickness (A) and daily sub-surface water flux between  
598 the moraine complex and sandur (B). Note that positive values indicate discharge from the

599 moraine complex to the sandur and negative values indicate recharge in the opposite  
600 direction.

601

602 Fig. 5. Schematic representation of the complete, annual water budget for the  
603 Finsterwalderbreen proglacial area. Blue arrows represent inputs, red arrows represent  
604 outputs, and other arrows represent internal transfers; broken lines represent minor multi-  
605 directional, stores/exchanges that cannot be quantified from the data available. All of the  
606 water fluxes presented in the figure are given in  $\text{m}^3$ , with estimates of probable error, except  
607 for channel recharge, active-layer discharge and surface runoff, for which it is not possible to  
608 determine realistic error estimates with the data available: these fluxes must therefore be  
609 viewed as first-order estimates. The determination of errors in all other water fluxes are  
610 described in detail in Hodgkins et al. (2009), with additional estimates as follows: (1) the  
611 error for the precipitation water flux is an average of probable errors previously determined  
612 for the rainfall and snowpack water-equivalent fluxes, weighted by proportion of total  
613 precipitation; (2) the probable error for the glacial runoff water flux is an average, weighted  
614 in proportion to overall contribution, of probable errors from the Terminus East and West  
615 gauging stations (average-weighted by time, as these errors varied temporally: Hodgkins et  
616 al., 2009) and the supraglacial water flux determined from ablation measurements.

Figure 1 (black/white)  
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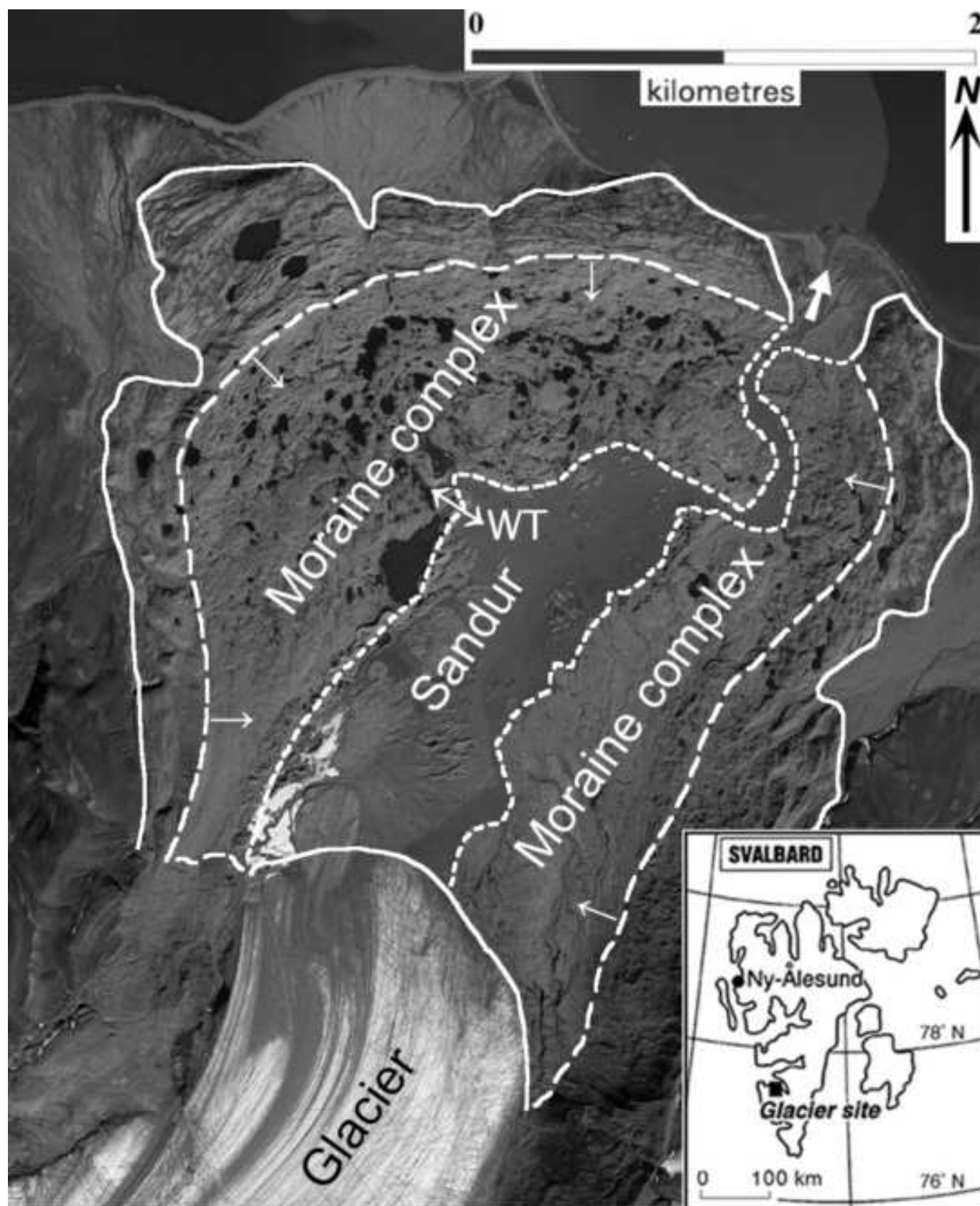




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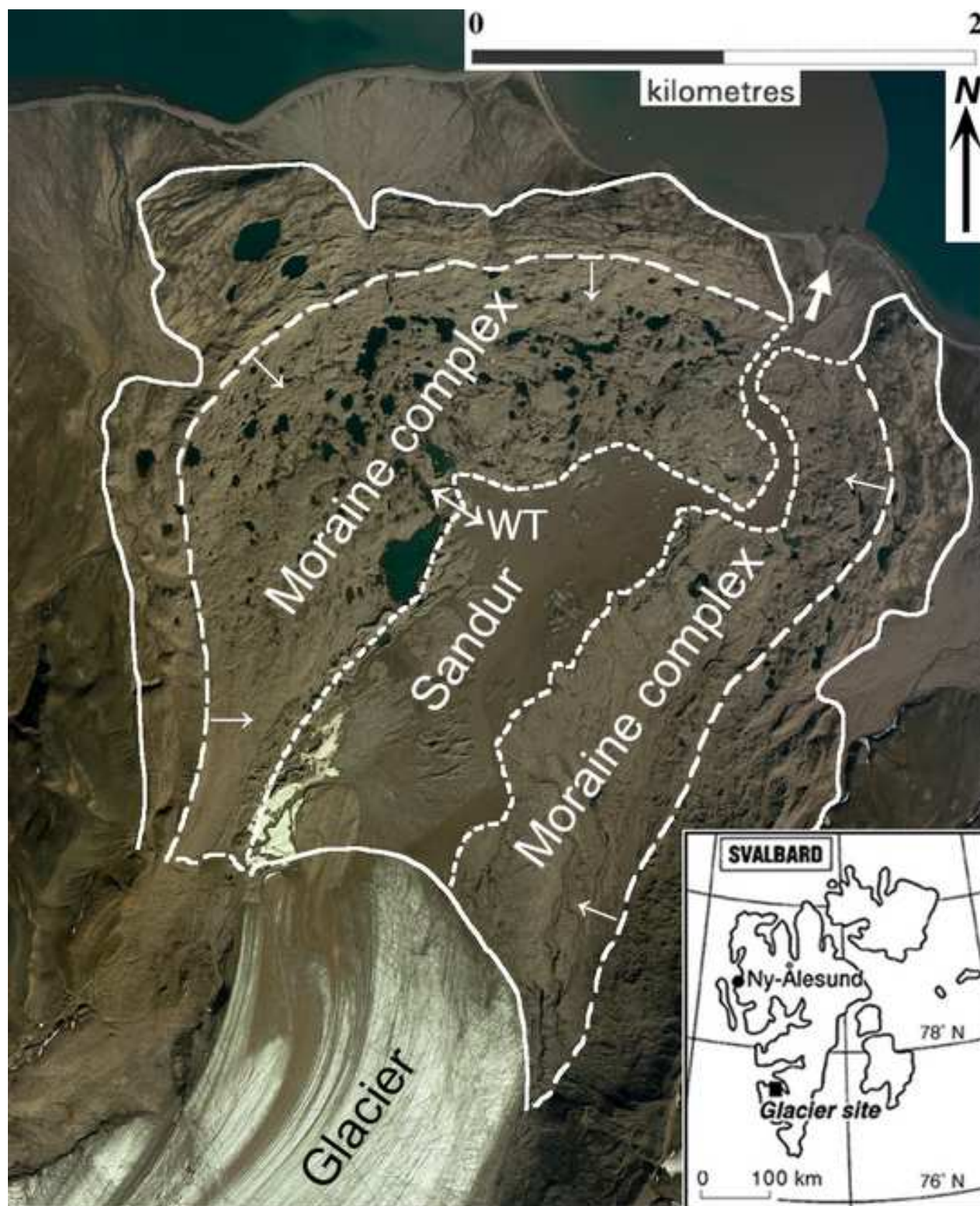




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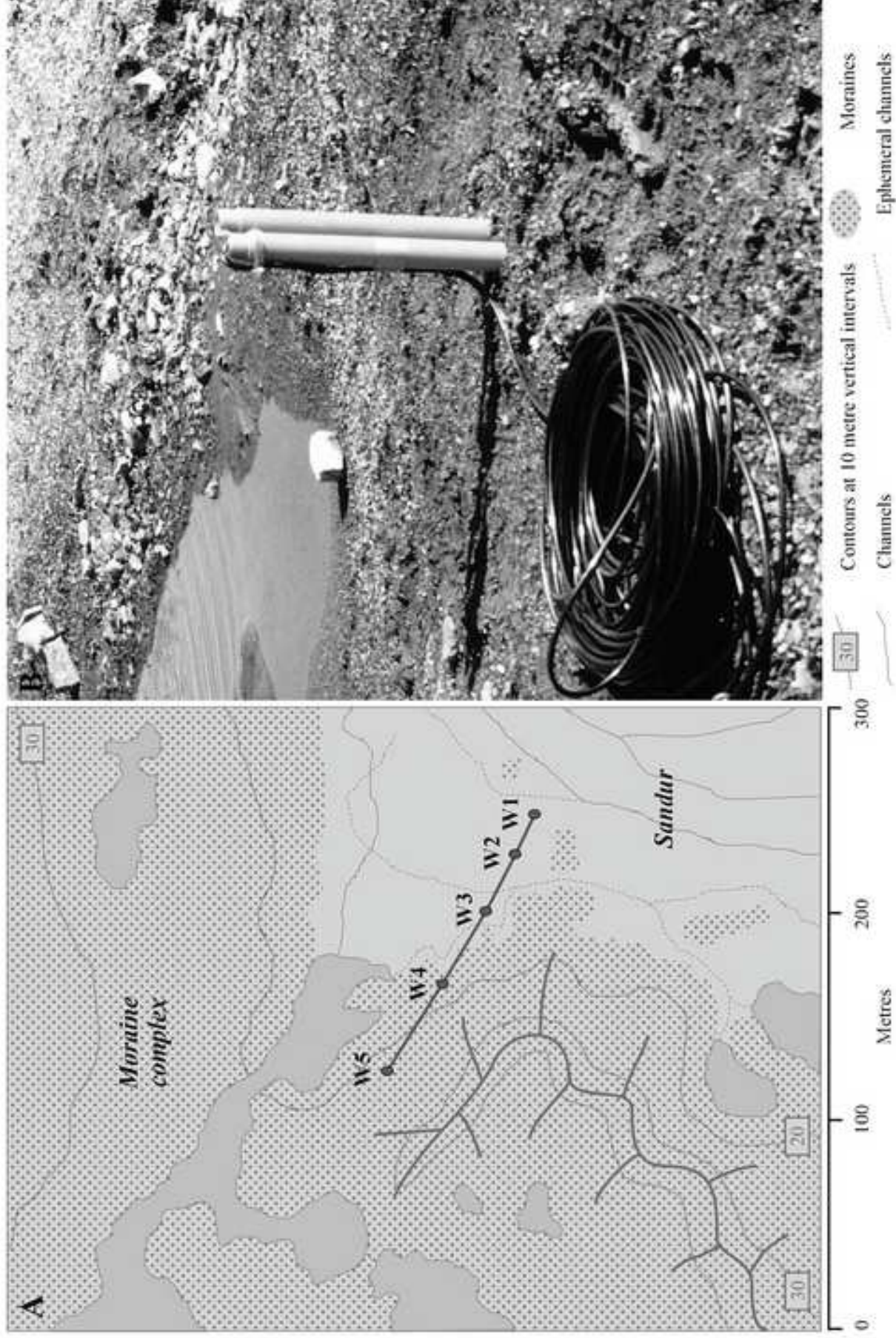




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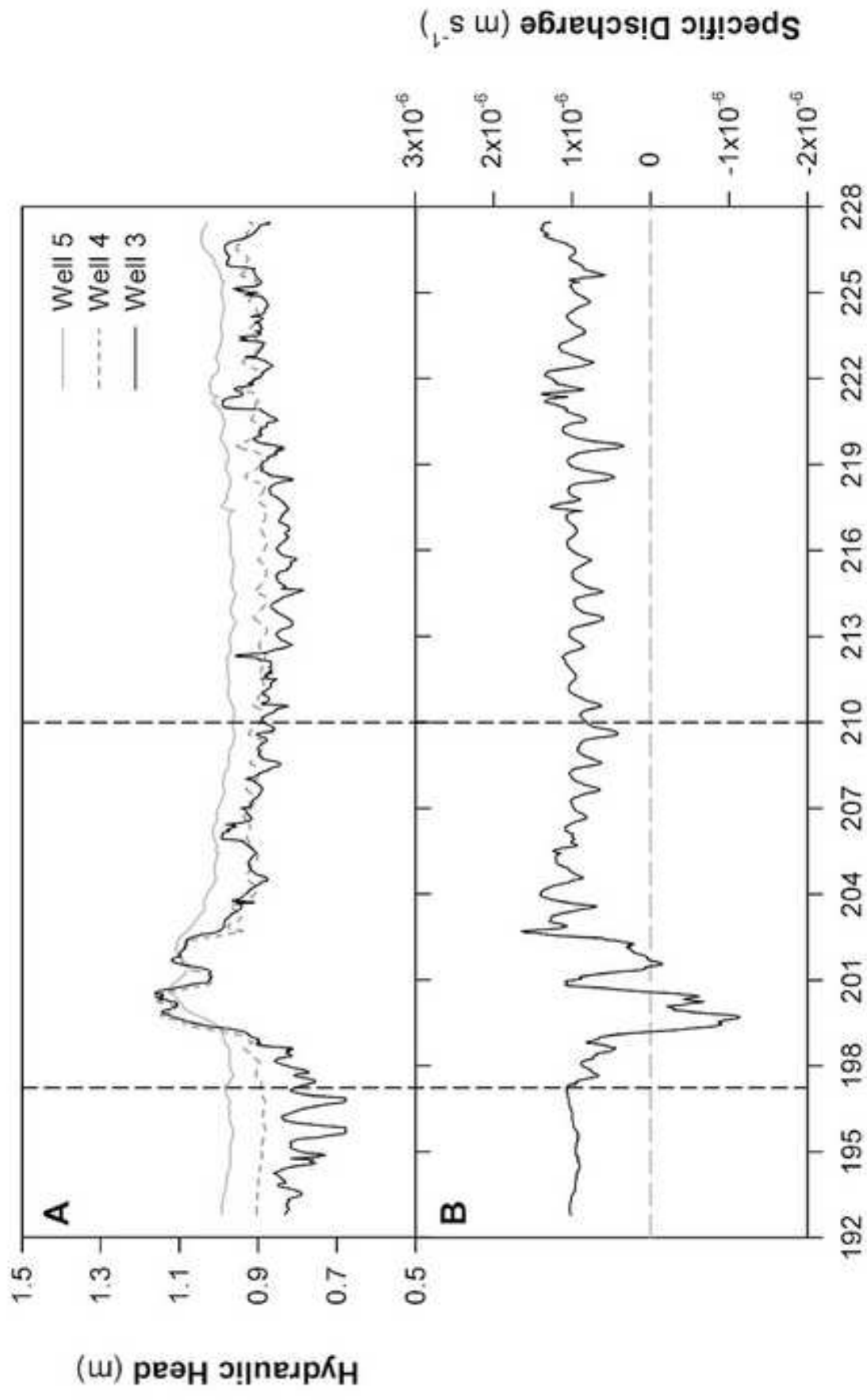




Figure 4  
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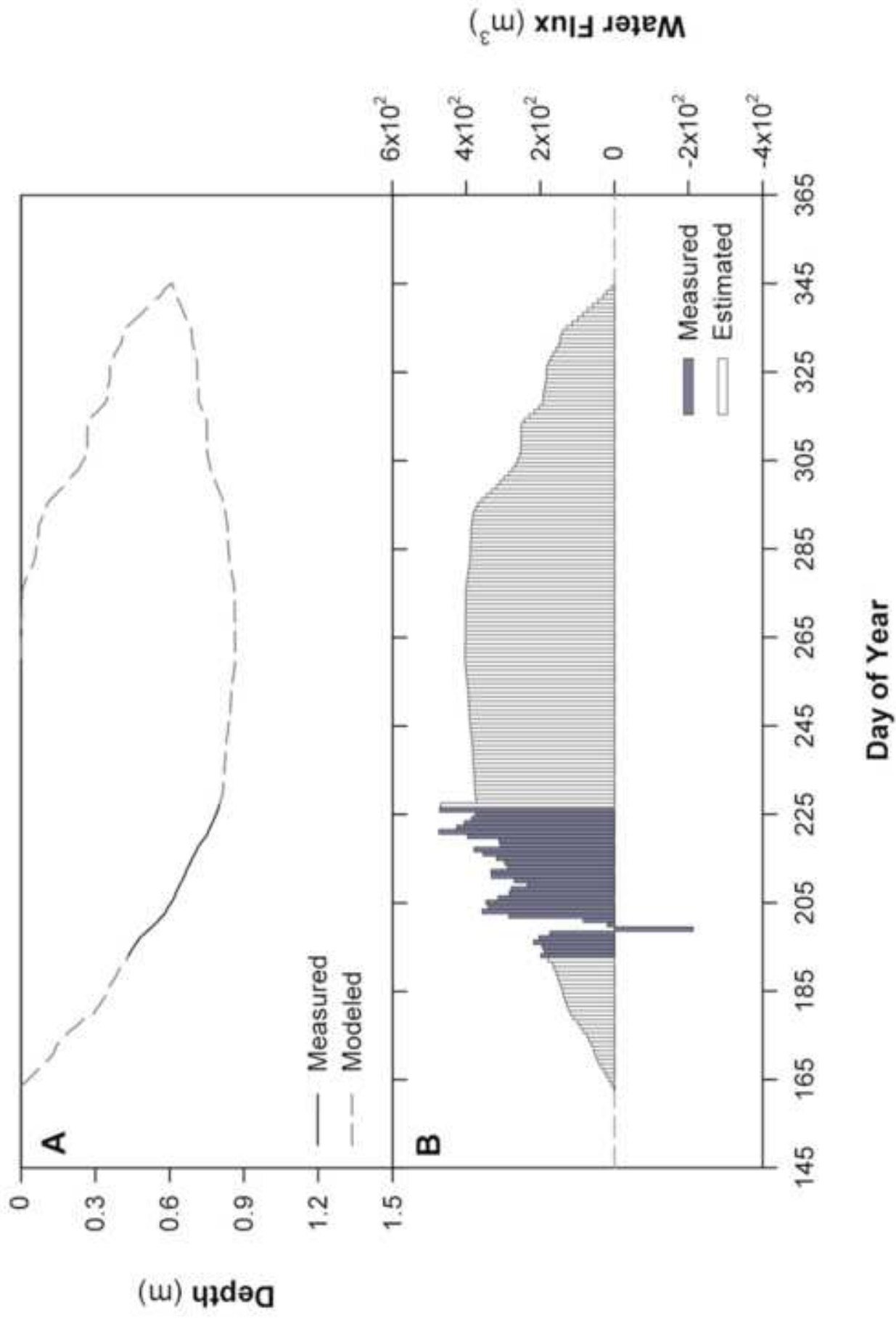


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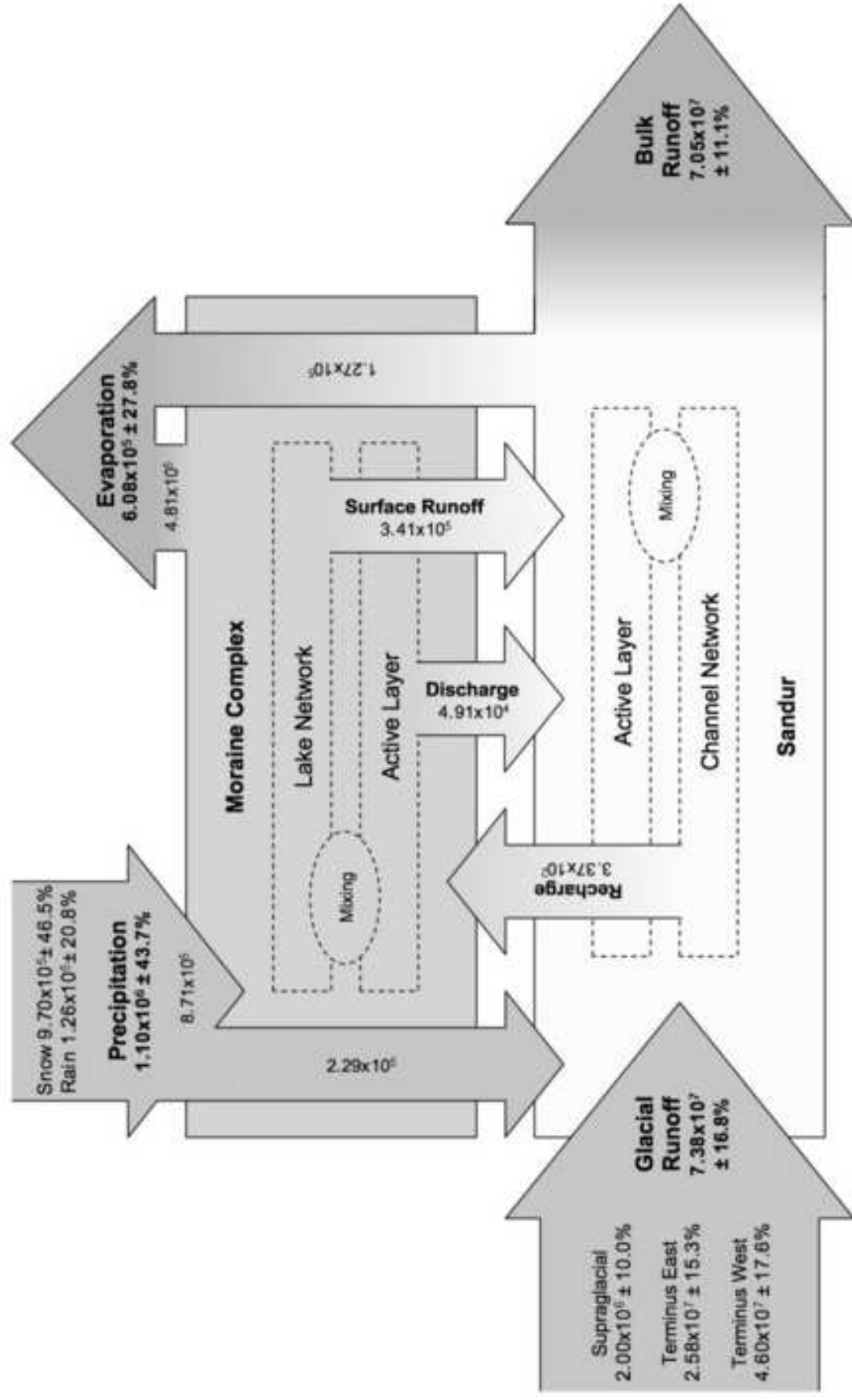
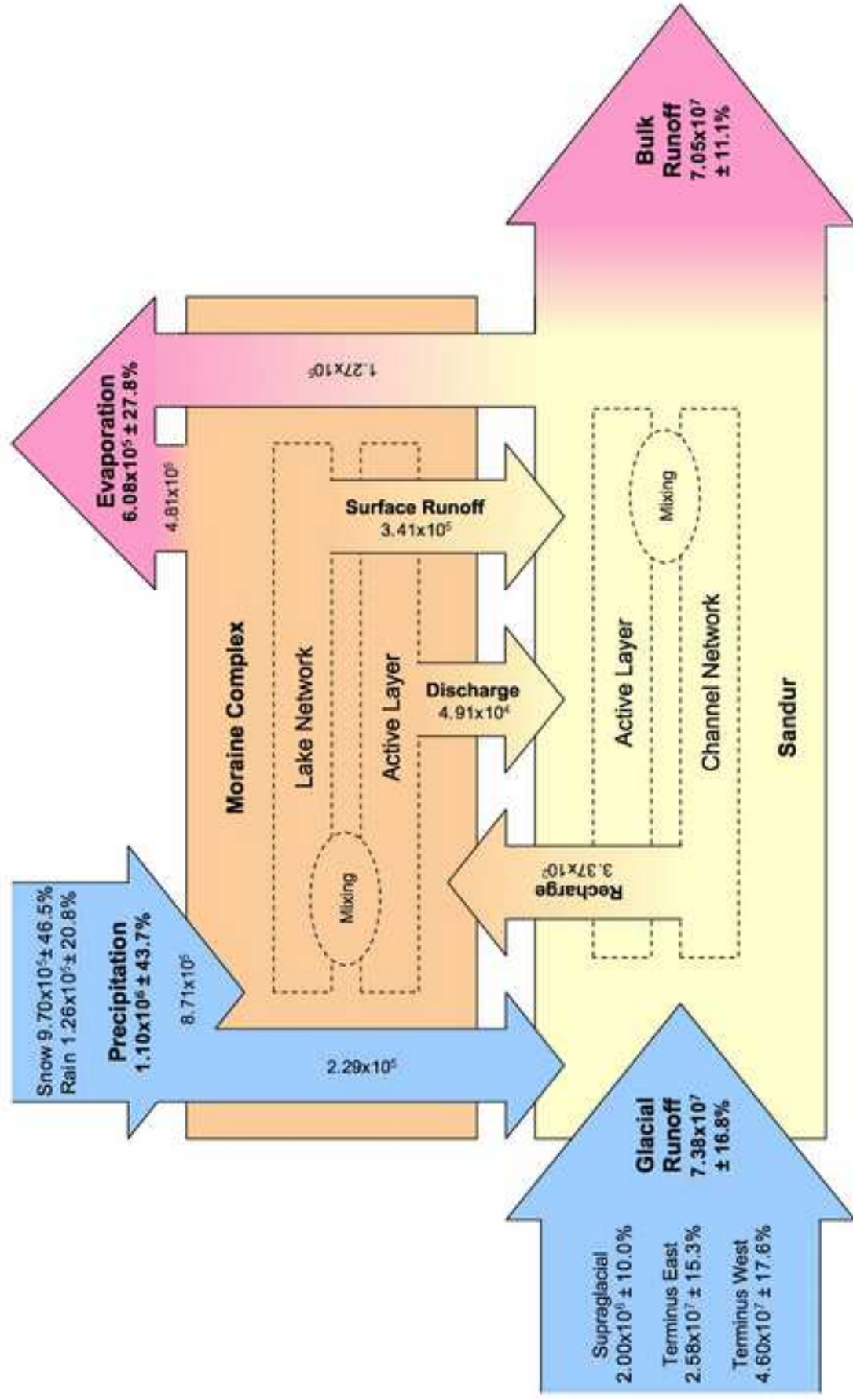


Figure 5 (colour)  
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## Tables

Table 1: Linear regression models used to predict active- and saturated-layer depths ( $L_a$  and  $L_b$  respectively) during unmonitored intervals at the start and end of the 1999 melt season. All coefficients are significant at  $p < 0.05$ .  $T_a$  is hourly air temperature, positive or negative.

Independent variable	Dependent variable	Slope	Intercept	$R^2$	When applied
$L_a$	$L_b$	1.047	-0.134	0.981 ( $n = 690$ )	For duration of active layer formation
$\sum T_a^+$	$L_a$	0.012	-0.380	1.000 ( $n = 2$ )	During active-layer thawing
$\sum T_a^-$	$L_a$	$-2.624 \times 10^{-4}$	0.000	0.837 ( $n = 5$ )	During active-layer freezing (surface-down)
$\sum T_a^-$	$L_a$	$1.111 \times 10^{-4}$	1.179	0.635 ( $n = 3$ )	During active-layer freezing (bottom-up)

Table 2: Sensitivity analysis of sub-surface water flux using equation 3, for the entire period of sub-surface flow (monitored and modelled fluxes, from June to December).

	Constant boundary	Variable boundary
<i>Results using parameter values given in text</i>		
Total annual flux	$4.91 \times 10^4 \text{ m}^3$	$4.19 \times 10^4 \text{ m}^3$
Mean annual discharge	$3.12 \pm 1.56 \times 10^{-3} \text{ m}^3 \text{ s}^{-1}$	$2.66 \pm 1.77 \times 10^{-3} \text{ m}^3 \text{ s}^{-1}$
<i>Corresponding results with any of <math>K_{sat}</math>, <math>dH/dL</math> or <math>L_b</math> modified by stated percentage</i>		
+50%	$7.36 \times 10^4 \text{ m}^3$ $4.68 \pm 2.34 \times 10^{-3} \text{ m}^3 \text{ s}^{-1}$	$6.29 \times 10^4 \text{ m}^3$ $4.00 \pm 2.66 \times 10^{-3} \text{ m}^3 \text{ s}^{-1}$
+30%	$6.38 \times 10^4 \text{ m}^3$ $4.06 \pm 2.02 \times 10^{-3} \text{ m}^3 \text{ s}^{-1}$	$5.45 \times 10^4 \text{ m}^3$ $3.46 \pm 2.31 \times 10^{-3} \text{ m}^3 \text{ s}^{-1}$
+20%	$5.89 \times 10^4 \text{ m}^3$ $3.75 \pm 1.87 \times 10^{-3} \text{ m}^3 \text{ s}^{-1}$	$5.03 \times 10^4 \text{ m}^3$ $3.20 \pm 2.13 \times 10^{-3} \text{ m}^3 \text{ s}^{-1}$
-20%	$3.93 \times 10^4 \text{ m}^3$ $2.50 \pm 1.25 \times 10^{-3} \text{ m}^3 \text{ s}^{-1}$	$3.35 \times 10^4 \text{ m}^3$ $2.13 \pm 1.42 \times 10^{-3} \text{ m}^3 \text{ s}^{-1}$
-30%	$3.44 \times 10^4 \text{ m}^3$ $2.19 \pm 1.09 \times 10^{-3} \text{ m}^3 \text{ s}^{-1}$	$2.93 \times 10^4 \text{ m}^3$ $1.87 \pm 1.24 \times 10^{-3} \text{ m}^3 \text{ s}^{-1}$
-50%	$2.45 \times 10^4 \text{ m}^3$ $1.56 \pm 0.78 \times 10^{-3} \text{ m}^3 \text{ s}^{-1}$	$2.10 \times 10^4 \text{ m}^3$ $1.33 \pm 0.89 \times 10^{-3} \text{ m}^3 \text{ s}^{-1}$

Table 3: Finsterwalderbreen proglacial area annual water balance, 1999: summary.

Component	Value
Precipitation (winter)	226 mm
Precipitation (summer)	29 mm
Precipitation (total)	256 mm
Evaporation	141 mm
Precipitation - evaporation	115 mm
Surface runoff	104 mm (inferred)
Sub-surface discharge from moraine complex to sandur	11 mm
Sub-surface recharge from sandur to moraine complex	0.1 mm
Glacial runoff	1697 mm (43.5 km <sup>2</sup> glacierized area)
Bulk catchment runoff	1073 mm (65.7 km <sup>2</sup> total catchment area)