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Common cycles and common trends in the stock and oil markets: Evidence from more than 150 years of data*

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ABSTRACT

This paper investigates the role of permanent and transitory shocks, within the framework of common cycles and common trends, in explaining stock and oil prices. We perform a multivariate variance decomposition analysis of monthly data on the West Texas Intermediate (WTI) oil price and the S&P500. The dataset used in the study spans a long period of 150 years and therefore contains a rich history to examine both the short- and long-run comovement properties of oil and stock prices. Given that the oil and stock markets might comove both in the short- and long-run, it is of interest to see the relative impacts of transitory and permanent shocks on both variables. We find that (log) oil price and (log) S&P 500 share a common stochastic trend for our full sample of September 1859 to July 2015, but a common cycle only exists during the post-WW II period. Full and post-WW II samples have quite different common feature estimates in terms of the impact of permanent and transitory shocks as measured by the impulse responses and forecast error variance decompositions. We also find that in the short-run oil is driven mostly by cycles (transitory shocks) and stock market is mostly driven by permanent shocks. But, permanent shocks dominate in the long-run.

1. Introduction

There exists a sizeable large literature that connects movements in oil returns and its volatility with recessions and inflationary episodes in the US economy¹ According to Hamilton (2008), nine of ten recessions in the US since World War II have been preceded by an increase in oil price. In fact, Hamilton (2009) even goes so far as to argue that a large proportion of the recent downturn in the US during the “Great Recession” can also be attributed to the oil price shock of 2007-2008. In the same vein, there is also a large literature that relates to the link between stock prices and economic activity, dating as far back as Mitchell and Bums (1938).² Unlike the empirical literature investigating oil, the impact of stock returns on US recessions is however, mixed, with more recent studies, based on sophisticated econometric techniques, pointing towards its role in predicting economic activity.³ Besides the large in-sample literature (see Footnotes 1 and 2) Stock and Watson (2003), and Rapach and Weber (2004), Kilian and Vigfusson (2011, 2013) provide evidence of the role of oil and the stock market in forecasting output growth and inflation for the US economy. Finally, financial historians, like Ahamed (2009) and Ferguson (2008), have suggested that financial crises are often preceded by bubbles in the asset and commodity markets, which, in turn is vindicated by Phillips and Yu (2011) based on formal tests of bubble detection in real-time.

¹ See for example, Rasche and Tatom (1977), Mork and Hall (1980), Hamilton (1983, 2011), and Hickman et al. (1987), Balke et al., (2002, 2010), Brown and Yücel (2002), Barsky and Kilian (2004), Jones et al. (2004), Kilian (2008a,b, 2009a,b), Elder and Serletis (2010), Nakov and Pescatori (2010), Baumeister and Peersman (2013a,b), Kang and Ratti (2013a, b), Antonakakis et al., (2014a), Bjørnland and Larsen (2015), and Baumeister and Kilian (2015), and references cited therein..

² More recent studies followed, and includes that of Fischer and Merton (1984), Barro (1990), Fama (1981, 1990), Harvey (1989), Stock and Watson (1989), Choi *et al* (1999), Schwert (1990), Estrella and Mishkin (1998), Colombage (2009), Nyberg (2010), Mili *et al* (2012), and Erdogan et al., (2015).

³ Interestingly, Campbell et al (2001) proposes that the variance of stock returns, rather than the returns themselves, have predictive content for output growth. Campbell (2001) finds evidence of high equity price volatility in one quarter to signal low macroeconomic growth in the next.

In addition, following the early works of Chen et al. (1986), Jones and Kaul (1996) and Sadorsky (1999), there exists a huge, and still growing, literature that relates short and long-run movements in oil and stock markets (for a detailed literature review in this regard, see for example, Kilian and Park (2009), Apergis and Miller (2009), Balcilar and Ozdemir (2012), Antonakakis and Filis (2013), Kang and Ratti (2013b), Antonakakis et al., (2014a, b), Broadstock and Filis (2014), Balcilar et al., (2015), Narayan and Gupta (2015), Angelidis et al., (forthcoming), Kang et al., (forthcoming), and references cited therein). While, the early literature primarily treated oil price as exogenous (supply-side shocks); following Kilian's (2009) seminal work which highlighted the endogeneity of oil price movements by relating it to economic activity, the recent studies on the oil and stock market relationship treats both variables as endogenous.

Relating the three (oil and macroeconomic variables, stock market and the economy, and oil and stock markets) strands of literature mentioned above, we can draw the following conclusions: (a) Whether it is based on in-sample or out-of-sample evidence, the importance of the role played by the stock and oil markets for the US economy is, in general, undeniable, and; (b) Oil and stock markets affect each other in both short and long-runs.

Against this backdrop, the objective of this paper is to investigate the role of permanent (i.e., aggregate supply shocks, such as technology shocks) and transitory shocks (namely, aggregate demand shocks, such as those resulting from changes in interest rate, inflation, fiscal policy, taste, velocity, and autonomous investment), within the framework of common cycles and common trends, in explaining stock and oil price movements, with both variables being treated as endogenous. Given that oil and stock prices act as leading indicators for the US economy, it is of paramount importance for a policy maker to determine what types of

shocks drives these two markets. In other words, detecting whether these shocks are temporary or permanent in nature would help in better policy design. Elaborating further on this issue, we can say that, only if temporary shocks are driving the two markets, can a policy maker have a role in affecting oil and stock prices. So for instance, if there are possible persistent bubbles in these two markets, and its collapse is likely to affect the economy negatively due to the leading role played by these two prices, the policy maker can change monetary or fiscal policy to correct for possible adverse effects.

While, applications of the common cycles and common trends methods to stock markets across and within countries can be found in Narayan (2011) and Narayan and Thuraisamy (2013) respectively,⁴ to the best of our knowledge, this is the first study to determine the nature of shocks that drives these two markets simultaneously.⁵ For our purpose, we perform a multivariate variance decomposition analysis of monthly data on the West Texas Intermediate (WTI) oil price and the S&P500 starting in September, 1859 (1859:09) to July, 2015 (2015:07), using Vahid and Engle's (1993) approach to identify common trends and cycles in the context of the multivariate Beveridge and Nelson (1981) decomposition technique.⁶ Another unique feature of our analysis is that sample period runs from the beginning of the modern era of the petroleum industry with the drilling of the first oil well on August 27, 1859 in Titusville, Pennsylvania.

⁴ Narayan (2011) looks at comovements between stock prices of emerging economies: Singapore, Taiwan, and South Korea, while Narayan and Thuraisamy (2013) analyzed comovements between stock prices within the US equity markets (S&P 500, Dow Jones and the NASDAQ).

⁵ Other applications of common cycles and common trends methodology in business cycles (national, local and sectoral), macroeconomic variables, health expenditures, metals and commodities can be found in the papers, such as: Vahid and Engle (1993), Engle and Issler (1995), Issler and Vahid (2001), Narayan (2008), Narayan and Narayan (2008a, b), and Issler et al., (2014).

⁶ Common trends and cycles can also be introduced into the multivariate structural time series model of Harvey (1989) and Koopman et al. (2000).

Note that, a multivariate approach introduces the possibility that trends and cycles may be common among variables. Engle and Kozicki (1993) defines a common feature to exist if a linear combination of the series fails to have the feature even though each of the series individually has the feature. While, cointegration is a common feature, another common feature of interest is the presence of common serial correlation patterns, i.e., common cycles. Issler and Vahid (2001) pointed out that the joint modeling of common-trend and common-cycle restrictions to identify permanent and transitory shocks has a clear advantage over the use of common-trend restrictions only. Understandably, if common-cycle restrictions are correctly imposed, estimates of the dynamic model (traditionally, a vector autoregression (VAR) model) are more precise, and leads to more accurate measurement of the relative importance of permanent and transitory shocks.

Our approach consists of four steps: First, we perform a battery of unit root tests (without and with breaks) on the WTI oil and S&P500 stock prices to establish the integration property of the data series. Second, we investigate the existence of common trends (i.e. co-movement over the long run) by applying the Johansen (1988, 1991) maximum likelihood techniques, and the multivariate cointegration method of Stock and Watson (1988a). Third, we examine the existence of common cycles (i.e. co-movement over the short run), by using the following test statistics: Weak Form (WF) reduced ranked structure test (Hecq et al. 2000, 2002, 2006); Serial Correlation Common Features (SCCF) (Engle and Kozicki, 1993; Vahid and Engle, 1993), and; Polynomial Serial Correlation Common Features (PSCCF) (Cubadda and Hecq, 2001, 2003). Finally, we conduct multivariate variance decomposition and impulse response analyses to examine the relative importance of permanent and transitory innovations in explaining variations in WTI oil and S&P500 stock prices. Note that, though not the primary goal of the paper, but once we identify the common trend and common cycle amongst these

two variables, we are also able to decipher the role played by oil and stock prices in driving these two common features.

Common features estimation approach introduced previously in the literature (e.g., Engle and Kozicki, 1993; Vahid and Engle, 1993; Issler and Vahid, 2001) require that some linear combinations formed from the first differences of the cointegrated $I(1)$ time series be white noise and, hence, the co-movements be contemporaneous. There is indeed a quite strong assumption that does not consider other possible co-cycle structures. Another restrictive feature of the previous approaches is that they require that the short- and long-run comovements be generated from the same common factors. Common features estimation methods used in this paper have three advantages. First, based on the PSCCF (Cubadda and Hecq, 2001, 2003) approach we allow for non-contemporaneous common cyclical movements among the $I(1)$ time series. Second, the WF structure used in the paper (Hecq et al. 2000, 2002, 2006) allows for the presence of short- and long-run comovements that are generated from different factors. A third advantage of our approach compared to the previous approaches is the flexibility to allow for imposing the implied common trends and common features reduced rank structures on the estimated model. Finally, the existence of cointegration as well as the permanent and cyclical components in each series allows one to conduct more accurate long-run forecasts (relative to the traditional VAR models) of the variables in question. One is also to determine the cycle of each series once the permanent component is extracted. Furthermore, the finding of a common stochastic trend between oil prices and stock prices should be the long-run economic growth that will set the growth rate of both the oil and stock prices. The changes in the long-run economic growth rate will induce long-run comovement of both oil and stock market prices. Furthermore, the finding of

cocycling behavior between oil and stock markets indicates to what extent a transitory shock in one market is transmitted to the other market.

The remainder of the paper is organized as follows: Section 2 presents the methodology, with Section 3 discussing the data and the results. Section 4 concludes the paper with policy recommendations.

2. Methodology

The major focus of this study is to examine the short- and long-run comovement of oil and stock prices. The dataset used in the study spans a long period of 150 years and therefore has a quite rich history to examine both the short- and long-run comovement properties of oil and stock prices. There are various channels that may lead to short-run or cyclical comovement and long-run comovement (co-trending) of these series. A large number of papers discussed in the introduction find evidence that increases in oil prices may lead to recessions and falling stock prices, resulting in cocycles. The long-run growth trends in the market value of firms will drive both stock prices and oil prices through resulting economic growth.

Long-run comovement among nonstationary time series require these series to be cointegrated and implies that their long-run tendencies are driven by some common stochastic trends. Common stochastic trends lead to the comovement of the low frequency (permanent) components of the series. The long-run comovement of the oil and stock markets then requires oil and stock price be cointegrated. Long-run comovement is derived by common stochastic trend shared by both the oil and stock prices. The reason behind this common stochastic trend should be the long-run economic growth that will set the growth

rate of both the oil and stock prices. The changes in the long-run economic growth rate will induce long-run comovement of both oil and stock market prices.

However, oil and stock markets might also comove in the short-run. This means that deviations of these series from their long-run common trends also comove leading to cocycling behavior. A large number of papers discussed in Section 1 documented this cocycling behavior based on various econometric methods. The short-run comovement behavior relates to the high frequency (temporary) components of the series and thus usually referred as “cocycles”. The cocycling behavior of oil and stock prices might be due to business cycles, wars, common structural breaks (co-breaks), volatility spillovers, etc. Cocycling behavior between oil and stock markets show to what extent a transitory shock in one market is transmitted to the other market.

2.1. Cointegration and common trends

Both the short- and long-run comovements of economic time series involve various challenges in terms of empirical modeling. The existence of common stochastic trends or cointegration among economic time series is one of the well-known stylized facts. Some stationary linear combinations of the $I(1)$ series do not have the stochastic trend property that each $I(1)$ series has since cointegration vectors annul these stochastic trends. Engle and Kozicki (1993) define this as a “common feature”. A feature is a common feature, if each of the series has the feature but a linear combination of the series fails to have this feature.

Analogous to common stochastic trends, Engle and Kozicki (1993) introduced a notion of serial correlation common features (SCCF). A group of time series will have an SCCF structure, if each series has serial correlation, but a linear combination of the series is serially

uncorrelated or an innovation process with respect to the past information set. Serial correlation signifies a (persistent) cyclical feature in the level of each series, but when the cyclical feature is common to each series, we will be able to find linear combinations of the cyclical component of each series that does not have the cyclical feature.

Our empirical investigation first tests for common-trends and common cycles. Then, we estimate reduced rank regression (RRR) models imposing the common trends and common cycles features. Common trend and cycle components are also estimated. The estimated restricted models are used to decompose both series into their permanent and transitory (PT) components. Finally, we obtain impulse responses (IR) and forecast error variance decompositions (FEVD) of permanent and transitory shocks.

In order to explain the relevant concepts, we focus on the following Wold representation of the vector error correction model (VECM) (Engle and Granger, 1987; Johansen, 1988, 1991):

$$\Delta Y_t = C(L)\varepsilon_t \quad (1)$$

where ε_t is a multivariate Gaussian white noise process with 0 mean and nonsingular covariance matrix Σ , $\varepsilon_t \sim N(0, \Sigma)$ and $C(L) = I_n + \sum_{i=1}^{\infty} C_i L^i$. The VECM (1) can be written as $\Delta Y_t = \Pi Y_{t-1} + \sum_{i=1}^{p-1} \Gamma_i \Delta Y_{t-i} + \varepsilon_t$, where Π has rank $r < n$ and, thus, there exist $n \times r$ matrices α and β such that $\Pi = \alpha\beta'$. Stock and Watson (1988b) show the existence of the well-known common trends representation:

$$Y_t = C(1)\xi_t + C^*(L)\varepsilon_t \quad (2)$$

where $\xi_t = \sum_{s=1}^t \varepsilon_s$, $\varepsilon_0 = 0$ for $i \leq 0$ and $C^*(L) = (1 - L)^{-1}[C(L) - C(1)] = \sum_{i=0}^{\infty} C_i^* L^i$ with $C_i^* = -\sum_{j=i+1}^{\infty} C_j$. Equation (2) is the multivariate Beveridge-Nelson (1981) (BN)

decomposition of Y_t . In this case, a nonsingular matrix Λ exists such that $C(1)\Lambda = [H \ 0_{n \times r}]$, where H is an $n \times k$ matrix with full column rank. Using the matrix Λ we can show that

$$\begin{aligned} Y_t &= H\tilde{\tau}_t + \psi_t \\ &= \tau_t + \psi_t \end{aligned} \tag{3}$$

where $\tau_t = H\tilde{\tau}_t$ and $\tilde{\tau}_t$ are the first k components of $\Lambda^{-1}\xi_t = \Lambda^{-1}\sum_{s=1}^t \varepsilon_s$ and H is an $n \times k$ matrix with full column rank. Equation (3) shows that the linear cointegration combinations are linear combinations of the transitory or cyclical components. This shows the relationship between the multivariate BN decomposition, common trends, and cyclical components arising from a VECM.

2.2 Common features and common-cycles

We will examine three notions of common cycles which imply that some form of reduced rank restriction can be imposed on the VECM in (1) leading to fewer number of terms in $C^*(L)\varepsilon_t$ and therefore each of the n transitory components in ψ_t can be obtained as a linear combination of less than n cyclical components.

The first of such common cycle notion is the serial correlation common features (SCCF) of Engle and Kozicki (1993) and Vahid and Engle (1993).⁷ The SCCF imposes the reduced rank restrictions on ΔY_t , because they describe the short-run movements of all the terms relating to the ΔY_t given in VECM in Equation (1). A second notion of common cycles that we consider is the polynomial serial correlation common features (PSCCF) of Cubadda and Hecq (2001, 2003). The PSCCF specification does not require contemporaneous synchronization among the cycles in order to reduce to number of cyclical components and allows some cycles to lead or lag the others. The third notion of common cycles is the weak form serial correlation

⁷ Hecq *et al.* (2000, 2002, 2006) also define a similar notion with less restrictive conditions and, therefore, refer the SCCF as the strong form (SF).

common features (WF) of Hecq *et al.* (2000, 2002, 2006). The WF applies to ΔY_t in deviations from the error correction terms $\alpha\beta'Y_{t-1}$, i.e., $\Delta Y_t - \alpha\beta'Y_{t-1}$, so it requires both ΔY_t and $\alpha\beta'Y_{t-1}$ have the same serial correlation structure.

Engle and Kozicki (1993) introduced the notion of SCCF and Vahid and Engle (1993) further generalized and presented statistical inference. The notion of SCCF implies that a vector of serially correlated stationary time series move together in such a way that some linear combinations of these series exists, which are a serially uncorrelated vector of white noise processes. Applied to the VECM in equation (1), the series ΔY_t has SSCF, if there exists an $n \times s$ matrix δ_s such that (1) $\delta_s' \alpha = 0$ and (2) $\delta_s' \Gamma_i = 0$, $i = 1, 2, \dots, p-1$, on the VECM in equation (1).

A drawback of the SCCF is the requirement that the common cycles must be contemporaneously synchronized. In this case, there will be no lead or lag relationship among the common cyclical components. The PSCCF relaxes this assumption and allows common serial correlations among the non-contemporaneous elements.

Introduced by Cubadda and Hecq (2001, 2003), the notion of PSCCF states that the series ΔY_t have s PSCCFs if a first order polynomial $\delta(L) = \delta_p - \delta_1 L$ exists such that (1) $\delta_p' \alpha = 0$, (2) $\delta_p' \Gamma_1 = \delta_1$, and (3) $\delta_p' \Gamma_i = 0$, $i = 2, 3, \dots, p-1$. The PSCCF restrictions imply that $\delta(L)' \psi_t = -\delta_1 C(1) \varepsilon_t$. Therefore, the BN cycles of Y_t , ψ_t , have the same PSCCF, if ΔY_t have the PSCCF structure. In this case, the same PSCCF relationship will cancel the dependence from the past of both ΔY_t and ψ_t .

Two important features of SCCF and PSCCF are: (1) the matrices δ_s and δ_p must lie in the left null space of the loading matrix α containing the adjustment speed coefficients and (2) the long-run dynamics and short-run dynamics are related due to presence of the error-correction terms on the right hand side of the VECM model. Hecq *et al.* (2000, 2002, 2006) introduces a weak form (WF) serial correlation common features notion that relaxes these restrictions.

The WF notion implies the existence of linear combinations of the series $\Delta Y_t - \alpha\beta'Y_{t-1}$ that are white noise. Under the WF notion of Hecq *et al.* (2000, 2002, 2006), there exist an $n \times s$ full column matrix δ_W such that $\delta_W'(\Delta Y_t - \alpha\beta'Y_{t-1}) = \delta_W'\varepsilon_t$. In this case, ΔY_t and $\alpha\beta'Y_{t-1}$ have the same serial correlation pattern, their impulse responses are collinear, and they have similar dynamics. This means that the short- and long-run dynamics of Y_t are unrelated.

2.3. Common features test and inference on permanent-transitory shock decomposition

Testing for cointegration and estimation of cointegration vectors are well established (see, e.g., Johansen, 1996). In this section, we briefly explain the inference in the presence of common features.

Following Johansen (1988, 1991), the maximum likelihood (ML) inference can be based on canonical correlations (CanCor). The likelihood ratio test for the s common feature restrictions is based on the Maximum Likelihood (ML) inference and given in Hecq *et al.* (2000, 2002, 2006) and Cubadda and Hecq (2001, 2003). The ML inference is equivalent to canonical correlations and can be used to determine the s .

Given that the oil and stock markets might comove both in the short- and long-run, it is of interest to see the relative impacts of transitory and permanent shocks on both variables. The analysis might reveal valuable information on what type of shocks drives these variables in the short- and long-run. The information might also help to disentangle the likely sources of transitory and permanent shocks, some of which are common to each variable.

In a VECM framework, the statistical theory for decomposition of variables in the model into permanent and transitory components (the multivariate BN decomposition), and IR and FEVD analysis are well established. Our analysis considers both common stochastic trends and common cycles. Therefore, not only the common stochastic trend restrictions but also common cycles restrictions apply in our case.

Our estimation procedure involves the following steps:

1. Decide the number of cointegration vectors r and estimate the VECM (1) with $p - 1$ order polynomial $\Gamma(L)$.
2. Fix β at estimated values $\hat{\beta}$, determine s and estimate the parameters under common features restrictions.
3. We obtain the estimates of permanent ($\hat{u}_t^P$) and transitory ($\hat{u}_t^T$) shocks and define $\hat{u}_t = (\hat{u}_t^P, \hat{u}_t^T)'$.
4. Obtain a lower block triangular matrix $\hat{M}$ using $V = [\alpha'_\perp \ \alpha' \Sigma^{-1}]'$, e.g., by applying Choleski decomposition to $\hat{\Psi} = \text{cov}(\hat{V} \hat{\varepsilon}_t) = \hat{M} \hat{M}'$, and construct $\hat{\eta}_t = \hat{M}^{-1} \hat{u}_t$. Elements of $\hat{\eta}_t$ are mutually uncorrelated and have unit variances.
5. Transform $\hat{C}(L)$ as $\hat{R}(L) = \hat{C}(L) \hat{V}^{-1} \hat{M}$, which obtains $\Delta Y_t = \hat{R}(L) \hat{\eta}_t$.

The IRs, FEVDs, and PT decompositions can then be obtained from the canned routines available in software packages using $\hat{R}(L)$, with the difference that the Choleski decompositions is applied to $\text{cov}(\hat{V}\hat{\varepsilon}_t)$ rather than to $\text{cov}(\hat{\varepsilon}_t)$.

3. Data and Results

We begin our empirical investigation by examining Figure 1 which plots the (log) of S&P 500 and (log) WTI Crude oil price. Our full sample period extends from September 1859 to July 2015, with the data coming from the Global Financial database. We seasonally adjust the data using the X-13 procedure of the US Census Bureau. We can see that the series move together over time. The spread between the two series increases over time suggesting that the cointegration with a deterministic trend may characterize the series. Along with the tendency of co-movement in the two series, another feature that appears are structural breaks and regime shifts. Short-run changes seem to be harmonized as well.

We turn next to a discussion of descriptive statistics presented in Table 1 which reports metrics for the log level of S&P 500 and the log WTI oil price as well as log returns of the two series. The average return for the (log) SP500 is 7.8 times higher than the average return for (log) WTI oil price. The WTI return is more volatile than the SP500 return, evidenced by the fact that the coefficient of variation (CV) for WTI returns is 15 times the coefficient of variation (CV) for the SP500 return. Not surprisingly, normality is rejected for both level and return series. Furthermore, returns are negatively skewed, and fat tailed. Both series also exhibit ARCH effects.

Table 2 reports unit root tests, including ADF (Dickey and Fuller, 1981), KPSS (Kwiatkowski et al., 1992), Phillips and Perron (1988), Ng and Perron (2001), DF-GLS

(Elliott et al., 1996), and Zivot and Andrews (2002) structural break in mean and trend. We conduct these tests over our full sample period, September 1859 to July 2015, as well as the post-WW II sample, October 1945 to July 2015 (owing to a structural break found in 1945 discussed later). All tests indicate uniformly that the (log) level of S&P 500 and (log) level of WTI oil price are I(1) series for both sample periods.

Table 3 reports Johansen (1988, 1991) and Stock and Watson (1988a) cointegration tests. Panel A of Table 3 reports information criteria used to select the lag length in the VAR. We use the AIC criteria and select a lag of 6. The information criteria of BIC and HQ select a lag of 2. We believe it is preferred to have a longer lag length than a lag length that is too short. Panel B reports the lambda-max and trace statistics when we allow for a deterministic trend in the cointegrating vector. Results indicate evidence of one cointegrating vector (reported in Panel B). The trend in the cointegrating vector is employed as we discussed the visual inspection of the two series in Figure 1. We also conduct cointegration tests without a trend in the cointegrating vector and find evidence of cointegration as well under that specification. Both tests show that log SP500 and log WTI are cointegrated both in the full sample and the post-WW II sample. Panel C reports result for the Stock and Watson (1988a) cointegration tests. The results support the Johansen tests in finding evidence of one cointegrating vector.

We also conducted three parameter constancy test based on the recursive estimation of the vector error correction model (VECM). Recursive estimation is performed over the Jul. 1861-Jul. 2015 period with the initial estimation period of Sep. 1859-Jul 1861. The likelihood ratio parameter constancy tests reported in Figure 2 are (a) max test of VECM parameter constancy (difference between $\beta^{(T)}$ and $\beta^{(t)}$), (b) β equals ‘known β ’ (i.e., $\beta^{(t)} \in \text{span } \beta$), and (c) log-likelihood constancy test. For each tests we report two test types, the X_t -Form and

the R_t -Form. The X_t -Form tests re-estimates all parameters in the model while the R_t -Form re-estimates only the long-run parameters. The tests are scaled by the critical value so that the critical value for comparison is 1. The max parameter constancy test results reported in Figure 2(a) do not reject the parameter constancy, ignoring the initial sample periods for which the recursive estimates might have not converged. The R_t -Form tests reach a maximum around the WW II period while the X_t -Form tests reaches a maximum in 1973. We further check whether the constancy can be supported for β equals ‘known β ’, which tests whether $\beta^{(t)} \in \text{span } \beta$. This statistic tests for constancy of the space spanned by β . The results presented in Figure 2(b) for testing β equals ‘known β ’ indicate that the constancy is rejected before 1920 by the X_t -Form tests and mostly between 1959-1933 and 1960-1974 periods by the R_t -Form tests. The log likelihood constancy tests reported in Figure 2(c) indicate that a structural break is most likely to have occurred in 1945. Overall, we obtain some evidence that a structural break most likely to occur around WW II. Figure 2(d) additionally reports the recursive log likelihood estimates scaled by the number of observations in the estimation window. The evidence presented in Figures 2(a)-(d) show that although the particular VECM parameter estimates seem stable, the space spanned by the parameters do not look constant over the sample period, which is evidenced by the log likelihood constancy test. The scaled log likelihood estimates in Figure 2(d) illustrate the possible economic reasons behind the existence of the structural break at the end of WW II. The log likelihood estimates decline significantly beginning at the Great Crash and this decline continues until early 1940s. Then, it starts rising back until 1980s, but it never reaches the level right before 1930. This is probably due to two important forces. First, the Great Crash caused a large decrease in the stock prices, but its effect on the oil prices was milder and come later. Second, in the post-WW II era oil prices had significant government regulation. In the US, the oil prices were regulated for periods Jun. 1947-Jun. 1963 and Apr.

73-Jun. 1981. The imposition and lift of the oil price controls caused a faster growth for stock prices compared to the oil prices during 1945-1981. There were also significant upward oil price jumps in 1971 and 1978. These events worsened the fit of the model during this period leading to breaks in the long-run and short dynamics.

Because of the structural break around 1945 we also report cointegration tests on a post-WW II sample period, October 1945 to July 2015, in Table 4. For this sample period we employ a lag length of 2 in the VAR and find that both the Johansen and Stock and Watson (1988a) tests indicate evidence of one cointegrating vector. The cointegrating vector for the full sample and the post-WW II period are different reflecting the finding of a structural break. The results for the post-WW II and full sample period differ due to two reasons. First, the long-run parameter estimates across two samples vary up to a sign change, implying a reversal of the impact of oil. The VECM estimates reported in Table 5 show that the impact of stock price on the oil price is 0.6936 in the full sample while it is -1.5095 in the post-WW II sample. Moreover, the trend term in the cointegration relationship also has a sign reversal across the two samples, a change from an insignificant -0.0002 to a highly significant (at 1% level) 0.0136. This may be due increased oil dependence and negative impact of oil on the economy due to fast growth after WW II. The second reason is related to the change in the cointegration structure between oil and stock markets. In the post-WW II period cointegration required a positive significant trend. The existence of a trend in the cointegration specification is similar to a Hicks neutral technological change in a production function. We interpret this unexplained growth effect as arising from the increased GDP growth rate in the post-WW II period, which probably resulted in a faster growth for oil demand particularly enhanced by the end of the oil price regulation in first in Jun. 1957 and second time later in Feb, 1981. Table 5 also show that the adjustment to equilibrium varies significantly in the

post-WW II sample. The full sample estimates show that the oil prices are weakly endogenous while stock price are weakly exogenous, indicating that it is oil prices do the adjusting back to long-run equilibrium after deviations from the long-run occur. For the post-WW II, estimates indicate that both oil and stock prices are weakly endogenous. This result combined with the existence of a significant trend in the cointegration equation in the post-WW II period, i.e., the unexplained growth, indicate that both the oil and stock prices are driven by other factors in the post-WW II era, most likely by the stronger GDP growth in this period.

Figure 3 (for the full sample period) plots permanent components of both (log) S&P500 and (log) WTI oil price as well as the common trend and common cycle series. The upper panel reports the permanent components (in dashed lines) and the actual series (in solid lines). The lower panel shows the common cycle and common trend components of the two series. Figure 4 reports comparable results for the post-WW II period. From the figures we can see that the stock market is driven primarily by the long-run stochastic trend, as actual stock price closely follows the permanent component (see Figures 2(b), 3(b)). The common trend component is mostly driven by the changes in the stock price (see Figures 2(d), 3(d)). It is the oil price that deviates mostly from this long-run common trend. However, this deviation feeds back to the system as the cycle is common during the post-WW II model. So, the deviation of oil price should impact the stock market in the short-run as well. This impact is quite large in the short-run (44% at step 1, see Table 8). Notice that the post-WW II results in Figure 4 are quite different from the full sample results in Figure 3. For the full sample a common cycle is not found and the permanent shock dominates (see Table 7). Figures 2(b) and 3(b) show that the stock price is always close to its permanent component, while the oil price significantly deviates from its permanent component in several periods. So the common

cycle is driven by the oil price deviating from the long-run trend. These dynamics might relate to the different dynamics in the oil and stock markets. Oil price had a regulation period as well as major demand boom in the post WW II period. The oil price has grown quite smoothly during 1900-1973 while the stock market was the most volatile during this period. Moreover, the oil price growth was less smoother than the stock market growth before 1900s and after 1973.

Figure 5 reports (for the full sample) impulse response functions for a one standard deviations to a permanent shock for the level of S&P 500 and the level of oil price (panel a and b) and for S&P 500 returns and oil returns (panel c and d). Figure 6 reports impulse responses to a transitory shock for the full period. We see a positive and significant response to permanent shocks from both (log) S&P 500 and (log) oil price. The stock market responds faster and its response is relatively higher than the response of the oil market. For the full sample, the responses of oil and stock price to transitory shocks are asymmetric. Oil responds negatively and significantly, while stock price responds positively but insignificantly. Initial response of oil is very large and negative with some undershooting.

Figure 7 and Figure 8 report comparable results to Figure 5 and Figure 6. In the post-WW II sample, responses to permanent shocks are quite different for the stock market than in the full sample period. The response of oil price in the post-WW II period is negative and significant. The response of oil price in the full sample and post-WW II samples are similar. It is the response of stock market that is largely affected by the structural break. The responses of both oil and stock markets to transitory shocks in the post-WW II sample (Figure 8) vary significantly compared to the full sample model. First, the response of oil price now becomes positive and exponentially decaying as well as the response of the stock market. In the post-

WW II period we see more changes for oil price's response to transitory shocks. The stock market's response also becomes larger and significant in the post-WWW II sample.

Agents that are interesting in forecasting oil prices over long-periods of time will find these results useful. It has been shown that when variables are cointegrated and there is one common stochastic trend then long-run forecasts can be improved by incorporating the error correction term yield a vector error correction model. Such a model has been shown to have greater forecast accuracy relative to a standard vector error correction model.

Table 6 reports three common cyclical features tests: i) Weak Form (WF) reduced rank structure (Hecq et al. 2000, 2002, 2006); ii) Serial Correlation Common Features (SCCF) (Engle and Kozicki, 1993; Vahid and Engle, 1993), and iii) Polynomial Serial Correlation Common Features (PSCCF) (Cubadda and Hecq, 2001, 2003). Panel A reports the full sample results while Panel B reports post-WW II result. In the full sample, no common cyclical features are found. In the post-WW II sample, WF and SSCF cases indicate a common cyclical feature. AIC, BIC and HQ information criteria all favor the SSCF specification.

Table 7 reports the forecast error variance decomposition for the full sample model for both the oil price and stock price series while the decomposition separates the variance into percentages accounted for by a shock in the common permanent component and a shock in the transitory (cyclical) component. The decomposition is based on the SCCF specification. This table is reported only for comparison purposes only, as we do not find a common cycle in the full sample (see Table 6 discussion). Therefore, the transitory shock should not be assumed as common. In the short-run 98% of the variance of the oil price is due to transitory

shocks, declines to 82% in 60 months. Almost all of the variance (99% in 1 to 3 months and 100% afterwards) of the stock price is due to permanent shocks.

Table 8 reports the forecast error variance decomposition for the post-WW II model for the oil price and stock price series. The decomposition splits the variance into percentages accounted for by a shock in the common permanent component and a shock in the common transitory (cyclical) component. The decomposition is based on the SCCF specification. Both the permanent and transitory shocks are common shocks. In the short-run 56% of the variance of the oil price is due to transitory shocks, this falls to 21% in 60 months. So, permanent shocks eventually dominate in the long-run and the impact of transitory shocks die off. In the short-run 44% of the variance of the stock price is due to transitory shocks, this falls to 12% in 60 months. So, permanent shocks eventually dominate in the long-run and the impact of transitory shocks die off. Transitory shocks account for almost half of the variance for both SP500 and WTI in the short-run, implying that common cyclical fluctuations play a significant role in the short-run but the common permanent shock dominate in the long-run.

4. Conclusion

The role played by the stock and oil markets in the US economy is an important area of inquiry. It is important for policy makers to determine what types of shocks drives these two markets. Ascertaining whether shocks are temporary (e.g. aggregate demand shocks) or permanent in nature (aggregate supply shocks), helps in better formulate policy. This paper investigates the role of permanent and transitory shocks, within the framework of common cycles and common trends, in explaining stock and oil prices. This is the first study to determine the nature of shocks that drives these two markets simultaneously. We perform a multivariate variance decomposition analysis of monthly data on the West Texas

Intermediate (WTI) oil price and the S&P500. The dataset used in the study spans a long period of 150 years and therefore contains a rich history to examine both the short- and long-run comovement properties of the oil and stock prices. We examine the short- and long-run comovement of oil and stock prices.

This paper centers around two important themes: (a) existence of common stochastic trend (common long-run relation) (b) existence of a common features (i.e. comovement of short run, transitory components). We present decomposition of each series into the independent permanent and transitory components, impulse responses and forecast error variance decompositions in the presence of both common stochastic trends and common cycles. Stock prices and oil prices may commove in the long-run as well as in the short-run.

We employ the Vahid and Engle's (1993) approach to identify common trends and cycles in the context of the multivariate Beveridge and Nelson (1981) decomposition technique. If common-cycle restrictions are correctly imposed, estimates of the dynamic model (a vector autoregression model) are more precise, and leads to more accurate measurement of the relative importance of permanent and transitory shocks. Given that the oil and stock markets might comove both in the short- and long-run, it is of interest to see the relative impacts of transitory and permanent shocks on both variables. The analysis might reveal valuable information on what type of shocks drives these variables in the short- and long-run. The information might also help to disentangle the likely sources of transitory and permanent shocks, some of which are common to each variable. Our analysis considers both the common stochastic trends and common cycles in the bivariate model of oil and stock prices. Therefore, not only the common stochastic trend restrictions but also common cycle restrictions apply in our case. We present decomposition of each series into the independent

permanent and transitory components, impulse responses, forecast error variance decomposition, in the presence of both common stochastic trends and common cycles. Our analysis reveals that there is a structural break in 1945 in the long-run linkage between log stock price and log oil prices.

For the post WW II period we find that the common trend component is driven primarily by the changes in the stock price. It is the oil price that deviates mostly from this long-run common trend. However, this deviation feeds back to the system as the cycle is common in the post-WW II model. Thus, both the oil and stock prices behave weakly endogenously in the post-WW II model as shown in Table 5. We do not find a common cycle during the post-WW II period. The deviation of oil price should impact the stock market in the short-run as well. This impact is quite large in the short-run. The results for the full sample estimates are quite different from the post-WW II results. The results indicate that a common cycle is not found and most things are driven by permanent shocks. We find that the stock price is always close to its permanent component, while the oil price significantly deviates from its permanent component in several periods. So the common cycle is driven by the oil price deviating from the long-run trend. During the post-WW II sample, responses to permanent shocks are quite different for the stock market than in the full sample period. The response of oil price in the post-WW II period is negative and significant. The response of oil price in the full sample and post-WW II samples are similar. It is the response of stock market that is largely affected by the structural break. The responses of both oil and stock markets to transitory shocks in the post-WW II sample vary significantly compared to the full sample model. During the full sample period the response of oil price now becomes positive and exponentially decaying as well as the response of the stock market. In the post-WW II period we see more changes for oil price's response to transitory shocks. The stock market's

response also becomes larger and significant in the post-WWW II sample. In the post-WW II sample, the WF and SSCF cases indicate a common cyclical feature. AIC, BIC and HQ information criteria all favor the SSCF specification. The forecast error variance decomposition is based on the SSCF specification. For the full sample we find that in the short-run 98% of the variance of the oil price is due to transitory shocks, declines to 82% in 60 months. Almost all of the variance (99% in 1 to 3 months and 100% afterwards) of the stock price is due to permanent shocks. For the post-WW II period we find both the permanent and transitory shocks are common shocks. In the short-run 56% of the variance of the oil price is due to transitory shocks, this falls to 21% in 60 months. Permanent shocks eventually dominate in the long-run and the impact of transitory shocks die out. In the short-run 44% of the variance of the stock price is due to transitory shocks, this falls to 12% in 60 months. Transitory shocks account for almost half of the variance for both (log) SP500 and (log) WTI in the short-run, implying that common cyclical fluctuations play a significant role in the short-run but the common permanent shock dominate in the long-run. The importance of both the permanent and transitory components in explaining the movements in both series (answered by the IRFs and FEVDs) show interestingly that in the short-run oil is driven mostly by cycles (transitory shocks) while the stock market is mostly driven by permanent shocks. But, permanent shocks dominate in the long-run. From the perspective of a policy maker this implies that policy decisions cannot affect the stock market either in short and long-runs, given that it is primarily driven by permanent productivity shocks. However, if there are bubbles in the oil market in the short-run, the policy maker can change interest rates or fiscal decisions to prevent its collapse, and the associated adverse effect on the macroeconomy. In the longer-run, policy decisions cannot affect the oil market just like the stock market. To put it alternatively, changes in policy to correct for possible bubbles in the

stock market is likely to be a futile exercise, but not so for the oil market, at least in the short-run.

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Table 1: Descriptive statistics.

	SP500	WTI
<u>Panel A: log levels</u>		
Mean	3.381	1.435
SD	1.947	1.343
CV	0.352	-2.303
Min	7.653	4.897
Max	0.732	0.707
Skewness	-0.726	-0.278
Kurtosis	208.434***	162.122***
JB	1865.708***	1860.730***
Q(1)	7417.626***	7320.441***
Q(4)	1866.888***	1841.264***
ARCH(1)	1863.956***	1844.030***
ARCH(4)		
<u>Panel B: log returns</u>		
Mean	0.0039	0.0005
SD	0.0476	0.0904
CV	-0.3563	-0.6931
Min	0.3524	0.7985
Max	-0.5286	-0.2482
Skewness	8.6242	13.024
Kurtosis	5899.1800***	13270.6490***
JB	25.1111***	277.6604***
Q(1)	34.0404***	324.3194***
Q(4)	93.6588***	201.6846***
ARCH(1)	230.4339***	299.5312***
ARCH(4)	0.0039	0.0005
N	1,871	1,871

Note: The table gives the descriptive statistics for Standard and Poor's S&P 500 Stock Market Index (SP500), and West Texas Intermediate spot crude oil price (WTI). All values are in natural logarithms in Panel A. Panel B gives the descriptive statistics for log returns. The sample period covers Sep. 1859-Jul. 2015 with $n=1871$ observations. S.D. and C.V. denote standard deviation and coefficient of variation, respectively. In addition to the mean, standard deviation (S.D.), minimum (min), maximum (max), skewness, and kurtosis statistics, the table reports the Jarque-Berra normality test (JB), the Ljung-Box first [$Q(1)$] and the fourth [$Q(4)$] autocorrelation tests, and the first [ARCH(1)] and the fourth [ARCH(4)] order Lagrange multiplier (LM) tests for the autoregressive conditional heteroskedasticity (ARCH). ***, ** and * represent significance at the 1%, 5%, and 10% levels, respectively.

Table 2: Unit root tests.

	LnSP500	LnWTI	LnSP500	LnWTI
	Full Sample: Sep. 1859 – Jul. 2015		Post-WW II Sample: Oct. 1945 – Jul. 2015	
<i>Panel A: Unit-root tests in levels</i>				
ADF	-1.3728 [21]	-2.1747 [25]	-2.5357 [6]	-2.2465 [21]
Z_α	-5.1710 [1]	-4.4679 [1]	-9.9881 [1]	-12.1280 [1]
MZ_α	-5.1669 [1]	-4.4660 [1]	-9.9389 [1]	12.1060 [1]
MZ_t	-1.4641 [1]	-2.1236 [1]	-2.2289 [1]	-2.4485 [1]
DF-GLS	-1.4620 [1]	-1.4326 [1]	-2.2335 [1]	-2.4313 [1]
KPSS	0.8678*** [1]	4.5657*** [1]	2.7545*** [1]	1.9687*** [1]
Zivot-Andrews	-5.4187** [18]	-4.1562 [37]	-3.3566 [18]	-4.3794 [1]
<i>Panel B: Unit-root test in first differences</i>				
ADF	-10.1480*** [19]	-12.8360*** [23]	-27.6870*** [0]	-20.353*** [0]
Z_α	-512.3800*** [9]	-2.5211E+05*** [14]	-485.6600*** [1]	-541.0000*** [1]
MZ_α	-43.609*** [9]	-2.5176E+05*** [14]	-274.3300*** [1]	-356.6600*** [1]
MZ_t	-4.6549*** [9]	-354.7900*** [14]	-11.71100*** [1]	-13.2920*** [11]
DF-GLS	-6.9010*** [9]	-12.4930*** [14]	-14.5670*** [1]	-16.2530*** [11]
KPSS	0.9608 [9]	0.0951 [14]	0.0515 [1]	0.0697 [1]

Note: Panel A reports unit roots tests for the log levels of the series with a constant and a linear trend in the test equation. Panel B report unit root test for the first differences of the log series with only a constant in the test equation. ADF is the augmented Dickey-Fuller (Dickey and Fuller, 1979) test, Z_α is the Phillips-Perron Z_α unit root test (Phillips and Perron, 1988), MZ_α and MZ_t are the modified Phillips-Perron tests of Perron and Ng (1996), DF-GLS is the augmented Dickey Fuller test of Elliot *et al.* (1996) with generalized least squares (GLS) detrending, KPSS is the Kwiatkowski *et al.* (1992) stationarity test, and Zivot-Andrews is the endogenous structural break unit root test of Zivot and Andrews (1992) with breaks in both the intercept and linear trend. Z_α , MZ_α , and MZ_t tests are based on GLS detrending. For the ADF unit root statistic the lag order is selected by sequentially testing the significance of the last lag at 10% significance level. The bandwidth or the lag order for the MZ_α , MZ_t , DF-GLS, and KPSS tests are select using the modified Bayesian Information Criterion (BIC)-based data dependent method of Ng and Perron (2001). ***, ** and * represent significance at the 1%, 5%, and 10% levels, respectively.

Table 3: Multivariate cointegration tests for the full sample: Sep.1859-Jul. 2015.

<i>Panel A: VAR order-selection criteria</i>								
Lag (p)	1	2	3	4	5	6	7	8
AIC	-5.2390	-5.4119	-5.4095	-5.4120	-5.4109	-5.4150	-5.4129	-5.4141
HQ	-5.2212	-5.3822	-5.3679	-5.3585	-5.3455	-5.3377	-5.3238	-5.3130
BIC	-5.2324	-5.4010	-5.3942	-5.3922	-5.3868	-5.3865	-5.3801	-5.3768
<i>Panel B: Johansen cointegration tests</i>								
Eigenvalues	0.0175	0.0019						
H_0	λ_{trace}	Critical values			Cointegration vector			
		1%	5%	10%	LOIL	LSP	Trend	
$r \leq 1$	3.4905	16.5539	12.5180	10.6664	1.4989	-1.0396	0.0003	
$r = 0$	36.3757***	31.1539	25.8721	23.3423	-0.1685	1.4667	-0.0056	
H_0	λ_{max}				Loadings			
		1%	5%	10%	LOIL	LSP		
$r = 1$	3.4905	16.5539	12.5180	10.6664	-0.0108	0.0008		
$r = 0$	32.8852***	23.9753	19.3870	17.2341	-0.0007	-0.0020		
<i>Panel C: Stock-Watson cointegration test</i>								
$H_0: q(k, k-r)$	Statistic	Critical values for $q(2,1)$						
$q(2,0)$	-5.1557	1%	-38.539					
$q(2,1)$	-48.6600***	5%	-30.369					
		10%	-26.501					

Note: Table reports selection criteria and multivariate cointegration tests for the VAR(p) model of variables LSP, and LOIL. Panel A reports the AIC, BIC, and Hannan-Quinn (HQ) information criteria. The VAR order is selected based on minimum AIC and is 6. Panel B reports maximal eigenvalue (λ_{max}) and trace (λ_{trace}) cointegration order tests of Johansen (1988, 1991) with a restricted trend specification. Non-rejection of $r=0$ for the Johansen tests implies no cointegration. Panel C reports the multivariate cointegration test of Stock and Watson (1988a). Under the null $q(k, k-r)$ of Stock-Watson cointegration test, k common stochastic trend is tested against $k-r$ common stochastic trend (or r cointegration relationship). Rejection of $q(2,1)$ for the Stock-Watson test implies cointegration. Numbers in bold are the minimum information criterion values. ***, ** and * represent significance at the 1%, 5%, and 10% levels, respectively.

Table 4: Multivariate cointegration tests for the post-WW II sample: Oct. 1945-Jul. 2015.

<i>Panel A: VAR order-selection criteria</i>								
Lag (p)	1	2	3	4	5	6	7	8
AIC	-6.2154	-6.3274	-6.3248	-6.3209	-6.3221	-6.3212	-6.3213	-6.3194
HQ	-6.1813	-6.2704	-6.2450	-6.2183	-6.1967	-6.1730	-6.1503	-6.1256
BIC	-6.2023	-6.3056	-6.2942	-6.2815	-6.2740	-6.2643	-6.2557	-6.2451
<i>Panel B: Johansen cointegration tests</i>								
Eigenvalues	0.0235	0.0042						
H_0	λ_{trace}	Critical values			Cointegration vector			
		1%	5%	10%	LOIL	LSP	Trend	
$r \leq 1$	3.5043	16.5539	12.5180	10.6664	-2.8381	-4.2907	0.0386	
$r = 0$	23.3639*	31.1539	25.8721	23.3423	-0.9193	2.3233	-0.0095	
H_0	λ_{max}				Loadings			
		1%	5%	10%	LOIL	LSP		
$r = 1$	3.5043	16.5539	12.5180	10.6664	0.0069	0.0042		
$r = 0$	19.8596**	23.9753	19.3870	17.2341	0.0024	-0.0021		
<i>Panel C: Stock-Watson cointegration test</i>								
$H_0: q(k, k-r)$	Statistic	Critical values for $q(2,1)$						
$q(2,0)$	-7.2332	1%	-38.539					
$q(2,1)$	-39.263***	5%	-30.369					
		10%	-26.501					

Note: Table reports selection criteria and multivariate cointegration tests for the VAR(p) model of variables LSP, and LOIL. Panel A reports the AIC, BIC, and Hannan-Quinn (HQ) information criteria. The VAR order is selected as 2 by all information criteria. Panel B reports maximal eigenvalue (λ_{max}) and trace (λ_{trace}) cointegration order tests of Johansen (1988, 1991) with a restricted trend specification. Non-rejection of $r=0$ for the Johansen tests implies no cointegration. Panel C reports the multivariate cointegration test of Stock and Watson (1988a). Under the null $q(k, k-r)$ of Stock-Watson cointegration test, k common stochastic trend is tested against $k-r$ common stochastic trend (or r cointegration relationship). Rejection of $q(2,1)$ for the Stock-Watson test implies cointegration. Numbers in bold are the minimum information criterion values. ***, ** and * represent significance at the 1%, 5%, and 10% levels, respectively.

Table 5: Estimates of the vector error correction models.

	Full sample: Sep.1859-Jul. 2015		Post-WW II sample: Oct. 1945-Jul	
	<i>OIL Equation</i>	<i>SP Equation</i>	<i>OIL Equation</i>	<i>SP Equation</i>
Normalized cointegration parameters				
LOIL	1.0000		1.0000	
LSP	-0.6936*** (0.1839)		1.5095*** (0.2821)	
Trend	0.0002 (0.0007)		-0.0136*** (0.0017)	
Constant	0.7336*** (0.0000)		9.4022*** (0.0000)	
Error correction parameters				
ΔECT_{t-1}	-0.0162*** (0.0029)	0.0013 (0.0016)	-0.0195*** (0.0057)	-0.0115*** (0.0041)
Short-run parameters				
$\Delta LOIL_{t-1}$	0.3892*** (0.0231)	-0.0047 (0.0131)	0.3422*** (0.0327)	-0.0160 (0.0234)
$\Delta LOIL_{t-2}$	-0.0259 (0.0248)	0.0162 (0.0141)	0.0224 (0.0483)	0.0515 (0.0345)
$\Delta LOIL_{t-3}$	0.0500** (0.0247)	0.0005 (0.0141)		
$\Delta LOIL_{t-4}$	-0.0299 (0.0248)	-0.0051 (0.0141)		
$\Delta LOIL_{t-5}$	0.0104 (0.0231)	0.0056 (0.0131)		
ΔLSP_{t-1}	0.0499 (0.0408)	0.1176*** (0.0232)		
ΔLSP_{t-2}	0.0220 (0.0410)	-0.0103 (0.0233)		
ΔLSP_{t-3}	0.0635 (0.0409)	-0.0619*** (0.0233)		
ΔLSP_{t-4}	-0.0312 (0.0410)	0.0405* (0.0233)		
ΔLSP_{t-5}	0.0829** (0.0408)	0.0798 (0.0232)		
Constant	-0.0004 (0.0019)	0.0033*** (0.0011)	0.0022 (0.0020)	0.0056 (0.0015)
log L	5070.3940		2673.81	
AIC	-5.4085		-6.3600	
BIC	-5.3284		-6.2900	

Note: Table reports the tests estimates of the vector error correction models for the full sample and post-WW II sample periods. Standard error of the estimates are reported in parentheses. In addition to the log likelihood (log L), the table reports the Akaike Information Criterion (AIC) and the Bayesian Information Criterion (BIC). ***, ** and * represent significance at the 1%, 5%, and 10% levels, respectively.

Table 6: Common cyclical features tests using reduced rank regression.

Panel A: Full Sample, Sep. 1859 – Jul. 2015								
Model	H_0	$\hat{\lambda}$	χ^2	$\log L$	p -value	AIC	HQ	BIC
(i) WF								
	$s \geq 1$	0.0269	50.8264***	10337.60	> 0.0001	-11.072	-11.058	-11.033
	$s \geq 2$	0.1579	371.3850***	10177.30	> 0.0001	-10.912	-10.910	-10.906
(ii) SCCF								
	$s \geq 1$	0.0273	51.7097***	10337.20	> 0.0001	-11.073	-11.059	-11.037
	$s \geq 2$	0.1695	398.0150***	10164.00	> 0.0001	-10.900	-10.900	-10.900
(iii) PSCCF								
	$s \geq 1$	0.0134	25.1295***	10350.50	0.0015	-11.085	-11.069	-11.043
	$s \geq 2$	0.0242	70.8467***	10327.60	> 0.0001	-11.071	-11.067	-11.059
Panel B: Post-WW II Sample, Oct. 1945 – Jul. 2015								
Model	H_0	$\hat{\lambda}$	χ^2	$\log L$	p -value	AIC	HQ	BIC
(i) WF								
	$s \geq 1$	0.0027	2.2253	5037.30	0.1358	-11.922	-11.918	-11.911
	$s \geq 2$	0.1164	105.7250***	4985.55	> 0.0001	-12.039	-12.028	-12.011
(ii) SCCF								
	$s \geq 1$	0.0071	5.9435*	5037.67	0.0512	-12.042	-12.034	-12.020
	$s \geq 2$	0.1304	122.7210***	4979.28	> 0.0001	-11.912	-11.912	-11.912
(iii) PSCCF								
	$s \geq 1$	0.0033	2.7955	5034.29	0.2472	-12.039	-12.022	-11.994
	$s \geq 2$	0.0302	28.4194***	5021.47	0.0001	-12.018	-12.009	-11.995

Note: Table reports the tests for s common cyclical features for three types of models (restrictions): (i) Weak Form (WF) reduced rank structure (Hecq et al. 2000, 2002, 2006), (ii) Serial Correlation Common Features (SCCF) (Engle and Kozicki, 1993; Vahid and Engle, 1993), and (iii) Polynomial Serial Correlation Common Features (PSCCF) (Cubadda and Hecq, 2001, 2003). All these restrictions lead to likelihood ratio tests, which distributed as χ^2 with degrees of freedom equal to number of restrictions. In the table $\hat{\lambda}$ are the eigenvalues form canonical correlation problems relating to the three types of restrictions, $\log L$ is the log likelihood of the model under the specification, and p -value is for the χ^2 test given in the fourth column. AIC, BIC, and HQ are the Akaike, Bayesian, and Hannan-Quinn information criterion, respectively. Numbers in bold are the minimum information criterion values. ***, ** and * represent significance at the 1%, 5%, and 10% levels, respectively, and ">" means "less than" the following it.

Table 7: Forecast Error Variance Decomposition for the full sample common features model: Sep. 1859-Jul. 2015.

Variance Decomposition of LOIL			Variance Decomposition of LSP	
Variance due to:				
Step	Permanent shock	Transitory shock	Permanent shock	Transitory shock
1	0.02	0.98	0.99	0.01
2	0.02	0.98	0.99	0.01
3	0.03	0.97	0.99	0.01
4	0.03	0.97	1.00	0.00
5	0.04	0.96	1.00	0.00
6	0.04	0.96	1.00	0.00
7	0.05	0.95	1.00	0.00
8	0.05	0.95	1.00	0.00
9	0.05	0.95	1.00	0.00
10	0.06	0.94	1.00	0.00
11	0.06	0.94	1.00	0.00
12	0.06	0.94	1.00	0.00
13	0.06	0.94	1.00	0.00
14	0.07	0.93	1.00	0.00
15	0.07	0.93	1.00	0.00
16	0.07	0.93	1.00	0.00
17	0.07	0.93	1.00	0.00
18	0.08	0.92	1.00	0.00
19	0.08	0.92	1.00	0.00
20	0.08	0.92	1.00	0.00
30	0.10	0.90	1.00	0.00
40	0.13	0.87	1.00	0.00
50	0.15	0.85	1.00	0.00
60	0.18	0.82	1.00	0.00

Note: The decomposition is based on the SSCF model, which selected jointly by all information criteria.

Table 8: Forecast Error Variance Decomposition for the post-WW II common features model: Oct. 1945-Jul. 2015.

Variance Decomposition of LOIL			Variance Decomposition of LSP	
Variance due to:				
Step	Permanent shock	Transitory shock	Permanent shock	Transitory shock
1	0.44	0.56	0.56	0.44
2	0.45	0.55	0.59	0.41
3	0.46	0.54	0.59	0.41
4	0.47	0.53	0.59	0.41
5	0.48	0.52	0.59	0.41
6	0.49	0.51	0.60	0.40
7	0.50	0.50	0.60	0.40
8	0.51	0.49	0.61	0.39
9	0.52	0.48	0.62	0.38
10	0.53	0.47	0.63	0.37
11	0.54	0.46	0.64	0.36
12	0.54	0.46	0.65	0.35
13	0.55	0.45	0.66	0.34
14	0.56	0.44	0.67	0.33
15	0.57	0.43	0.68	0.32
16	0.58	0.42	0.69	0.31
17	0.59	0.41	0.69	0.31
18	0.60	0.40	0.70	0.30
19	0.60	0.40	0.71	0.29
20	0.61	0.39	0.72	0.28
30	0.68	0.32	0.78	0.22
40	0.73	0.27	0.83	0.17
50	0.76	0.24	0.86	0.14
60	0.79	0.21	0.88	0.12

Note: The decomposition is based on the SSCF model, which selected jointly by all information criteria.

Figure 1: Natural Logarithms of SP500 and WTI: Sept.1859-Jul. 2015

Figure 2: Constancy tests for the log likelihood of the VECM model

Note: Figure reports recursive constancy tests for (a) VECM parameters (difference between $\beta^{(T)}$ and $\beta^{(t)}$), (b) β equals 'known β ' ($\beta^{(t)} \in \text{span } \beta$), (c) log-likelihood. The X_t -Form tests re-estimates all parameters in the model while the R_t -form re-estimates only the long-run parameters. The tests are scaled by the critical value so that the critical for comparison is 1. Part (d) of the figure additionally reports the recursive log likelihood estimates scaled by the number of observations in the estimation window. Recursive estimation is performed over the Jul. 1861-Jul.2015 period with the initial estimation period Sep. 1859-Jul 1861 (23 observations).

Figure 3: Estimates of the common features for the full sample: Sep. 1859-Jul. 2015.

Note: The decomposition is based on the SSCF model, which selected jointly by all information criteria.

Figure 4: Estimates of the common features for the post-WW II sample: Oct. 1945-Jul. 2015.

Note: The decomposition is based on the SSCF model, which selected jointly by all information criteria.

Figure 5: Impulse responses to a permanent shock for the full sample: Sep. 1859-Jul. 2015.

Note: The figure gives the impulse responses to a 1 standard deviation shock in the permanent component. The impulse responses are obtained the SSCF model, which selected jointly by all information criteria. The horizontal axis represents the steps in months. The solid line denotes the impulse response, while shaded region around the impulse response line represent the 68% (± 1 standard deviation) confidence interval.

Figure 6: Impulse responses to a transitory shock for the full sample: Sep. 1859-Jul. 2015.

Note: The figure gives the impulse responses to a 1 standard deviation shock in the transitory component. The impulse responses are obtained the SSCF model, which selected jointly by all information criteria. The horizontal axis represents the steps in months. The solid line denotes the impulse response, while shaded region around the impulse response line represent the 68% (± 1 standard deviation) confidence interval.

Figure 7: Impulse responses to a permanent shock for the post-WW II: Oct. 1945-Jul. 2015.

Note: See Note to Figure 5.

Figure 8: Impulse responses to a transitory shock for the post-WW II: Oct. 1945-Jul. 2015.

Note: See Note to Figure 6.