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HYDRAULIC ACTUATION TECHNOLOGY FOR FULL- AND SEMI-ACTIVE RAILWAY SUSPENSIONS

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HYDRAULIC ACTUATION TECHNOLOGY FOR FULL- AND SEMI-ACTIVE RAILWAY SUSPENSIONS

Abstract

The paper describes a simulation study that provides a comprehensive comparison between full-active and semi-active suspensions for improving the vertical ride quality on railway vehicles. It includes an assessment of the ride quality benefits that can theoretically be achieved with idealised devices, and also examines the impact of real devices based upon hydraulic actuation technology.

Keywords: Mechatronics, active suspension, actuator, secondary suspension, railway vehicle, simulation

1. INTRODUCTION

In the last two decades, much research has been completed in order to improve ride quality on railway vehicles. An overall summary of the possibilities of using active suspensions for railway vehicles is included in [1], and it is generally accepted that such concepts applied to the secondary suspension system offer significant improvements in ride quality, including the effects of different actuator technologies – see for example [2, 3]. Tilting trains, which are an example of active suspension technology, represent what is nowadays a standard railway technology which is offered and supplied by all major rail vehicle manufacturers in high-speed trains and for regional applications [1]. However a broader use of active secondary suspensions has been very limited. This is largely because a higher level of passenger comfort is not strongly cost beneficial, and since semi-active devices are cheaper and simpler a number of workers have investigated the use of these both theoretically and via experiment (see for example [4, 5]).

Full-active and semi-active approaches have a significant difference. A full-active approach includes a fully-controllable force actuator that includes a power supply, whereas the

semi-active concept utilises a suspension component with a controllable characteristic. The energy flow of a semi-active suspension is controlled but not augmented, and furthermore the energy flow's direction is limited to one direction. More precisely, it is only possible to dissipate energy but not inject it (although with an accumulator it is possible to partly utilize the energy stored [6]), and this behaviour results in a fundamentally nonlinear concept which offers less improvement compared with full-active. In principle any passive component whose characteristics can be changed electrically would comprise a semi-active device, but in practice a semi-active actuator is usually a conventional damper with the ability of variable damping by using electro hydraulic or electro-rheological fluid devices. On the other side, full-active actuators mostly use electro-hydraulic, pneumatic or electro-mechanical technology. Electro- and magneto-rheological fluids have also been studied for semi-active devices, but at present these are not appropriate for the actuation required for full-active suspensions.

The papers referenced above [1-5] are examples of many studies of both full-active and semi-active suspensions for improving the ride quality on railway vehicles, but none has properly compared their relative performance using a consistent set of

Fig 1 Assessment framework

criteria. It has also not been possible to define what can theoretically be achieved with idealised devices compared with real active and semi-active hydraulic actuation. This paper provides a consistent comparative assessment for a vertical suspension system based upon a “side-view” suspension model for a four-axle vehicle focussed upon the comparisons as indicated by Fig 1. The passive v. semi-active v. full-active comparison identifies the conceptual benefits of active control, and provides an aspirational basis for possible developments in actuator technology for

active suspensions, including the fundamental limitations of semi-active compared with active solutions. The ideal v. real comparison, in this paper for a single technology, **moderates** expectations of what is achievable in practice and perhaps **guides** technology improvements.

2. MODELLING AND ASSESSMENT

This section describes the simulation models for the vehicle suspension and the full- and semi-active devices used in the study, and also explains the requirements and approach used for assessment.

2.1 Sideview vehicle model

The simulation studies are undertaken using a passive side-view model that includes four axles, two bogies and primary and secondary vertical suspensions shown by Fig. 2. Typical parameters for a modern high-speed train with an airspring suspension are used [7] (**notation, equations and values are listed in** the Appendix). Note that, for both the full- and semi-active solutions, the surge reservoir and orifice damping represented by k_{SecD} and c_{Sec} are omitted since damping is then provided through active control. ~~The corresponding equations are not included here because they have been adequately described by many papers.~~

Fig 2 Side view model of railway vehicle

2.2 Full and semi-active device models

The actuators are fitted in parallel with the secondary suspension as indicated in Fig 2, and their modelling requires different approaches for each of the four options. The ideal full-active actuator is simply a perfect force actuator that generates the commanded force irrespective of the movements across it and with no time delay. It can produce bi-directional force when the actuator is moving in both directions, i.e. it can operate in all four quadrants of the force-velocity graph, although a real actuator will of course be subject to dynamic constraints relating to how quickly it can transition from one quadrant to another.

However even the ideal semi-active damper is a non-linear device with a force/velocity coefficient that can be varied instantly up to a maximum defined value – more discussion of this is given below. However this is not true for the semi-active device, and Figure 3 provides a generalised characteristic which illustrates that it is constrained to operate in a relatively small area of the graph. Not only is operation in the upper left and lower right quadrants completely impossible, but also the minimum and maximum damping rates provide a limitation in the other

two quadrants. This type of characteristic emphasises the fundamentally non-linear nature of all semi-active suspensions.

Fig 3 Semi-active damper Force-Velocity characteristic

For the “real” actuator a well-established model [described by Neal \[8\]](#) is depicted in Fig. 4. The equations that are used to represent the compressibility of the oil in the cylinder and the nonlinear flow/pressure relationship associated with the servo-valve are given in the Appendix, [also](#) based upon [Neal’s](#) well-established approach. The corresponding linearised block diagram model is given by Figure 5, which includes a no flow pressure gain K_c and a transfer function to allow for the valve dynamic response.

Fig 4 Real hydraulic actuator scheme

Fig 5 Real hydraulic actuator linearised block diagram

The “real” semi-active device is a relatively straightforward adaptation of the full-active hydraulic model, but without the hydraulic power supply, as shown in Fig 6. The valve is then a simple variable device connected between the two sides of the actuator. Although in principle it is possible to account for the different effective areas by shaping the opening characteristics of the valves, for this study a “through-rod” actuator has been assumed so that, unlike the full-active actuator, the flows are equalised. The same flow/pressure relationship as the full actuator is used.

Fig 6 Semi-active damper scheme

By means of simulations with the ideal full active suspension it was possible to undertake an

“outline design”, and this defined actuator force and velocity requirements of 15kN and 0.4 m/s respectively. A supply pressure of 210 bar was assumed, and these values enabled the calculation of other parameters, e.g. the area of the piston, and to choose an appropriate cylinder and valve. Parameter values based upon this outline hydraulic design process are listed in the Appendix.

2.3 Performance assessment approach

The secondary suspension of a railway vehicle has to cope with deterministic and stochastic disturbances. The former are caused by guiding the vehicle along the intended track variations, such as gradients or curves. The latter occur due to track irregularities. The design aim is to limit the maximum suspension deflection for the deterministic input, while isolating the stochastic component and achieving the best possible ride quality. It should be emphasised that the maximum suspension deflection is often not considered for a normal passive suspension, but this does become an important constraint with the active suspension control strategies, which are most appropriately based upon absolute or “skyhook” damping [9].

Track irregularities

Although it is possible to use real measured track irregularities to give predictions for a real section of track, for a research assessment a generalised simplified power spectrum to represent track irregularities can be used [9] which provides a good representation of the irregularities in the range 0.1-10Hz, although it over-emphasises their size at higher frequencies.

$$S_t(f_t) = \frac{A_v}{f_t^2} \quad (1)$$

where A_v is the track roughness factor and f_t is a spatial frequency [cycles/m]. Using the speed of the train v this can be converted to a temporal frequency and the track vertical velocity input

modelled by a band-limited Gaussian white noise with a flat spectrum given in Equation 2, where the units are now $(\text{ms}^{-1})^2/\text{Hz}$.

$$G_{\dot{z}_t}(f) = (2\pi)^2 A_v v \quad (2)$$

The roughness factor was taken as $1 \times 10^{-7} \text{m}$ and the velocity as 55 m/s, i.e. to represent typical conditions for a 200 km/h train. Appropriate speed-dependent time delays are used to provide the inputs to the other three axles of the vehicle.

Ride quality has been assessed using RMS acceleration values. It would be possible to use frequency weighting to allow for human susceptibility to vibration, for example as specified by ISO 2631, but in fact unweighted accelerations are used in this study.

Deterministic input

A gradient of 2% was assumed as the deterministic input, which included a transition section having a superimposed vertical acceleration of 0.3m/s^2 . Obviously these values will vary between different administrations and routes, but represent a typical worst case for which the suspension control might have to be designed.

3. DEFINITION OF CONTROL STRATEGIES

There are two distinct issues to be described: firstly the basic suspension control strategy which generates active force commands that are appropriate to provide ride quality improvements; secondly, when the actuator is non-ideal, the inner loop that achieves force control of the actuator (Figure 5). These two issues are explained in the following sub-sections.

3.1 Suspension control strategies

Although there is a wide variety of active secondary suspension control possibilities that have been described, in one way or another they normally employ the concept of “skyhook” damping, or absolute velocity damping (which is a more scientific description). Both the full- and semi-active controllers used for this analysis are based upon skyhook damping, although each has important variations, and Figures 7-10 describe the progressive development of the basic skyhook strategy to accommodate the different practicalities.

Full-active control

A practical skyhook control strategy involves modifying the basic skyhook concept in two important ways:

- i. Pure absolute velocity damping creates large suspension deflections on track gradients (or curves for an active lateral suspension), and it is necessary to include a high-pass filter to remove the inputs associated with such features [9]. This filter diminishes the improvements that are possible, but is essential to meet the maximum deflection constraint. Normally the absolute velocity measurement is derived by integrating the signal from an accelerometer, and in order to avoid integrator drift it is practical to combine with the high-pass filter (Figure 7), in other words the high-pass effect serves two purposes. Cut-off frequency of 0.16 Hz (1 rad/s) has been used, the same as in [9].
- ii. Applying the damping in modal sense (bounce and pitch for a vertical suspension) is beneficial for ride quality, as shown in Figure 8. This is because it is possible to use a higher skyhook damping coefficient in the pitch mode than the bounce mode, a consequence of the deterministic input into the pitch mode being much smaller.

Fig 7 Scheme of the skyhook damping suspension controller

Fig 8 Scheme of modal skyhook control strategy *[new figure]*

Semi-active control

The same suspension control strategy can be used but it's necessary to convert the force command into a control signal for the semi-active device, essentially a damper setting, and Figure 9 illustrates the way that this can be done, also taking into account the maximum and minimum damping rate limits available for the device. Due to the division by actuator velocity, the demanded damping rate may clearly become very large, but the controller prevents this by means of the maximum limit (although the program code would need to have overflow and divide by zero protection).

Fig 9 Basic semi-active control strategy *[new figure]*

3.2 Real actuator control

Actuator for full-active suspension

Figure 10 Real actuator controller *[new figure]*

Figure 10 shows the scheme for a force-feedback controller. Achieving fast control action is a challenge for the design of the controller itself. Since the controller has a relatively low gain, high force errors are needed to produce enough flow, but the suspension strategy demands very small force at high frequency to provide a good ride quality, and these two requirements are in conflict. Better performance can be achieved by including a spring in series with the actuator, and a spring with a stiffness k_{secF} of 20 times the secondary suspension stiffness k_{sec} was used –

essentially this is in series with the compressibility of the oil in the actuator chambers. A corresponding integral plus phase advance controller was designed based upon optimising the force tracking performance of the inner loop. The parameters both for the force controller and for the “modal skyhook” suspension controller are given in the Appendix.

Semi-active device

Figure 11 Scheme of the real semi-active device controller

Figure 11 shows the controller used for the semi-active device, including the actuator model as previously described. The skyhook force command is generated using the same controller as for the full-active solution. The scheme of Fig 9 is used to define the required damping constant, with $c_{\min}$ and $c_{\max}$ defined as $0.2 c_{\sec}$ and $2c_{\sec}$ respectively. (The relationship between valve current and damping constant is derived using the damper equations assuming a very high value of series stiffness.)

4. SIMULATION STUDIES

A large number of simulations involving both time and frequency domain analysis were undertaken to determine optimum settings for the various parameters and the values used for the suspension controller (bounce and pitch skyhook damping values, high-pass filter cut-off

frequency) are listed in the Appendix.

4.1 Time domain results

Table 1 shows the overall performance comparison derived from the time domain simulation, both in absolute RMS acceleration and percentage change (negative is an improvement in ride quality), with the ride quality of the passive suspension as a reference. It can be seen both that full-active always out-performs the semi-active approach, and also that adding “real” actuator technology inevitably provides some degradation. The percentage figures highlighted in grey indicate the size of this degradation, real v. ideal.

The table emphasises the crucial benefit when using active control. It shows that the improvement at the front and rear of the vehicle is significantly higher than in the middle, with the rear of the vehicle benefitting from the highest improvement (although in terms of absolute values the rear starts off as the worst).

Table 1 Ride quality and suspension deflection results from time simulation

	RMS values of the body vertical acceleration (%g)									Max defl. (mm)	
	Front			Centre			Rear			Front	Rear
	RMS	%age Real v. ideal	%age v. passive	RMS	%age Real v. ideal	%age v. passive	RMS	%age Real v. ideal	%age v. passive		
Passive	3.14		⌊	1.65		⌊	3.58		⌊		
Ideal full	1.41	⌊	-55.1%	1.02	⌊	-38.2%	1.51	⌊	-57.2%	28.5	25.9
Real full	1.70	+20.6%	-45.9%	1.16	+13.7%	-29.7%	1.78	+17.9%	-50.3%	28.5	25.4
Ideal semi	1.94	⌊	-38.2%	1.31	⌊	-20.6%	2.02	⌊	-43.6%	24.9	24.4
Real semi	2.06	+6.2%	-34.4%	1.37	+4.6%	-17.6%	2.13	+5.4%	-40.5%	24.8	24.1

Since the full-active suspension system is entirely linear the RMS values can also be derived analytically based upon frequency response analysis and using a calculation of the transfer function from disturbances to acceleration with the inner force and outer skyhook loops closed.

The RMS values are given by

$$a_{RMS} = \sqrt{\int_0^{\infty} |H(j\omega)|^2 G_{z_i}(j\omega) d\omega} \quad (3)$$

where the transfer function $H(j\omega)$ has to include the speed-dependent time delay information between track input and the four wheel sets, i.e.

$$H(j\omega) = H_0(j\omega) + \sum_{i=1}^3 H_i(j\omega) e^{-j\omega \frac{y_i}{v}} \quad (4)$$

Table 2 gives these analytical results for the full-active system, which shows an excellent match with the corresponding results in Table 1. As already mentioned the semi-active skyhook control law is highly non-linear and so the same analysis cannot be applied to the semi-active suspension.

Table 2 RMS body acceleration and relative benefits – values based on analytical calculations

RMS values of the body's vertical acceleration in %g						
	Front		Centre		Rear	
	RMS	%age v. Passive	RMS	%age v. Passive	RMS	%age v. Passive
Passive	3.11	—	1.60	—	3.55	—
Ideal full	1.39	- 55.3%	1.00	- 37.1%	1.48	- 58.3%
Real full	1.69	- 45.7%	1.15	- 28.8%	1.76	- 50.5%

4.2 PSD Analysis

Power spectral density information has also been investigated (partly in the process of optimising the control schemes). Of course this reflects what has been seen in previous active

suspension studies, but it is useful to include some results in order to show where the various benefits are achieved in terms of different frequencies. In all cases the comparisons are based upon acceleration PSDs over the rear suspension of the vehicle.

Figure 12 shows the passive vehicle response in comparison with ideal full-active and ideal semi-active, which shows the profound improvements that are possible with both types of active suspension. Figure 13 omits the passive response and gives a clearer view of the additional improvements achievable with full-active: the semi-active solution gives slightly reduced acceleration levels at low frequencies below about 0.6Hz, whereas the full-active is superior for higher frequencies.

Fig 12 Acceleration PSDs at rear of vehicle, passive v. ideal full- and semi-active

Fig 13 Acceleration PSDs at rear of vehicle, ideal full- and semi-active

Figures 14 and 15 show the effects of real actuator technology. Very little difference is seen for the real semi-active solution in Figure 14, which reflects the small degradation of 5.4% listed in Table 1, whereas Figure 15 shows a larger change for the real full-active, Table 1 indicating a 17.9% degradation. Note that from 1-3 Hz the real actuator is slightly better, but the degradation arises from the higher accelerations which can just be seen beyond 5Hz, but the true impact is obscured by the restricted logarithmic frequency axis: Figure 16 has a linear axis extending from 10Hz to 30Hz and shows that the degradation occurs at higher frequencies, particularly around 20Hz, a problem that doesn't happen with the real semi-active solution, results for which are shown in Figure 17.

Fig 14 Acceleration PSDs at rear of vehicle, ideal v. real semi-active

Fig 15 Acceleration PSDs at rear of vehicle, ideal v. real full-active

Fig 16 PSDs at rear of vehicle, ideal v. real full-active (30Hz frequency range)

Fig 17 PSDs at rear of vehicle, ideal v. real semi-active (30Hz frequency range)

4.3 Overall summary

Table 1 is the principal outcome of the research study and effectively answers the research question regarding the relative performance of the control options. It is also useful to present

the percentage improvements in the context of the overall problem as set out in Figure 1, and Figure 18 indicates the performance benefits based upon the average improvement (front, centre and rear).

Figure 18 Overall performance summary

The average improvement (percentage reduction in RMS acceleration) across the vehicle is 50.2% for full-active compared with 34% for semi-active, and the effect of actuator technology is to change these to 42% and 30.8% for full- and semi-active respectively.

5. CONCLUSIONS

The study provides a rigorous assessment of the relative benefits of full- active versus semi-active suspension approaches for the vertical suspension of a railway vehicle. It is clear that full-active provides more improvements in ride quality, but semi-active can certainly provide improvements throughout the vehicle. The results provide a basis for understanding the trade-off between the additional ride quality benefits of the full-active approach set against the greater complexity.

Further work should consider other actuator technologies, in particular electro-mechanical, although the characteristics make this less practical as a semi-active solution. It is also necessary to repeat the assessment for the lateral secondary suspension so that a full picture of

the relative benefits of full- and semi-active suspensions can be completed.

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APPENDIX – Modelling details

Suspension equations

$$\begin{aligned}\ddot{z} &= \frac{1}{m_B} \left(-k_{Sec} (2z - z_1 - z_2) + F_{a1} + F_{a2} \right) \\ \ddot{\Theta} &= \frac{y_b}{I_{xxB}} \left(-k_{Sec} (2y_b \Theta - z_1 + z_2) + F_{a1} - F_{a2} \right) \\ \ddot{z}_i &= \frac{1}{m_b} \left(k_{Sec} (z + y_b \Theta - z_i) - k_{Pri} (2z_i - z_{i1} - z_{i2}) - c_{Pri} (2v_i - v_{i1} - v_{i2}) - F_{ai} \right) \\ \ddot{\Theta}_i &= \frac{y_w}{I_{xxb}} \left(-k_{Pri} (2y_w \Theta_i - z_{i1} + z_{i2}) - c_{Pri} (2y_w \omega_1 - v_{i1} + v_{i2}) \right)\end{aligned}$$

where z and Θ are body vertical and pitch displacements, and z_i and Θ_i are bogie vertical and pitch displacements with $i \in [1, 2]$

Table A1 Suspension parameters

Description	Notation	Value
Mass of the vehicle	m_B	38,000 kg
Body pitch Inertia	I_{xxB}	$2.31 \times 10^6 \text{ kgm}^2$
Mass of the bogie frame	m_b	2,500 kg
Bogie frame pitch Inertia	I_{xxb}	$2.604 \times 10^3 \text{ kgm}^2$
Semi longitudinal spacing of the sec. susp.	y_b	9 m
Semi longitudinal spacing of the wheelsets	y_w	1.25 m
Secondary spring stiffness per bogie	k_{Sec}	508 kNm^{-1}
Secondary damping stiffness per bogie	k_{SecD}	1.016 MNm^{-1}
Secondary passive damping per bogie	c_{Sec}	64.11 kNsm^{-1}
Primary spring stiffness per axle	k_{Pri}	4.935 MNm^{-1}
Primary passive damping per axle	c_{Pri}	50.74 kNsm^{-1}

Full active actuator – equations

$$\begin{aligned}\frac{d}{dt} p_1(t) &= -\beta \frac{A_1 v_p - q_1}{V_{01} + A_1 z_p} \\ \frac{d}{dt} p_2(t) &= \beta \frac{A_2 v_p - q_2}{V_{02} - A_2 z_p}\end{aligned} \quad \text{and} \quad \begin{aligned}q_1 &= \begin{cases} \alpha A_o(|x_v|) \sqrt{\frac{2}{\rho}} \sqrt{p_s - p_1} & \text{for } x_v > 0 \\ -\alpha A_o(|x_v|) \sqrt{\frac{2}{\rho}} \sqrt{p_1 - p_t} & \text{for } x_v \leq 0 \end{cases} \\ q_2 &= \begin{cases} \alpha A_o(|x_v|) \sqrt{\frac{2}{\rho}} \sqrt{p_2 - p_t} & \text{for } x_v > 0 \\ -\alpha A_o(|x_v|) \sqrt{\frac{2}{\rho}} \sqrt{p_s - p_2} & \text{for } x_v \leq 0 \end{cases}\end{aligned}$$

Where the piston velocity is v_p and $A_o(|x_v|)$ signifies the opening area of the valve and x_v is the

valve position.

The load pressure is defined by the difference of the pressure in the chambers $p_L = p_1 - p_2$,

where the sum is constant and equal to the supply pressure $p_s = p_1 + p_2$. The load flow $q_L = \frac{q_1 + q_2}{2}$

is simply the average flow through the valve. By means of these definitions the differential equations of the chamber pressures result in one differential equation for the load pressure

which is given by

$$q_L = A_F dv + \dot{p}_L \frac{V_t}{4\beta} \quad (2)$$

where $A_F = \frac{A_1 + A_2}{2}$ is the area of the piston and $V_t = V_{01} + V_{02}$ is the entire volume.

Table A2 Full active actuator parameters

Description	Notation	Value
Effective area of cylinder	A_F	$10.66 \times 10^{-4} \text{ m}^2$
Chamber volumes of cylinder	V_{01}, V_{02}	$1.066 \times 10^{-4} \text{ m}^3$
Constant discharge coefficient	A	0.7
Bulk modulus of the oil	β	$1.38 \times 10^9 \text{ Pa}$
Density of the oil	ρ	858.2 kgm^{-3}
Area gradient of the valve	D	$5.6734 \times 10^{-6} \text{ m}^2/\%$
Supply pressure	P_s	$210 \times 10^5 \text{ Pa}$
Tank pressure	P_T	$\sim 0 \text{ Pa}$
Flow gain	K_q	$0.01196 \text{ m}^3 \text{ s}^{-1}/\%$
Flow pressure sensitivity	K_c	$4.492 \times 10^{-13} \text{ m}^3 \text{ s}^{-1} \text{ Pa}^{-1}$
Unit conversion gain	K_a	$33.333 \text{ \%}/\text{A}$
Damping of the servo-valve	ζ_{VF}	0.3
Undamped natural freq. of the servo-valve	ω_{VF}	$2\pi \times 100 \text{ rad/sec}$

Table A3 Semi-active actuator parameters

Description	Notation	Value
Effective area of cylinder	A_s	$60.23 \times 10^{-4} \text{ m}^2$
Chamber volumes of cylinder	V_{ts}	$6.023 \times 10^{-4} \text{ m}^3$
Bulk modulus of the oil	β	$1.38 \times 10^9 \text{ Pa}$
Damping of the servo-valve	ζ_{vs}	0.3
Undamped natural freq. of the bypass-valve	ω_{vs}	$2\pi \times 50 \text{ rad/sec}$

Table A4 Controller parameters

Description	Notation	Value
Damping ratio of the high pass filter	ζ_{HPF}	0.7
Cut off frequency of the high pass filter	ω_{HPF}	1 rad/sec
Bounce mode skyhook damping coefficient (full-act)	c_{bF}	65 kNsm^{-1}
Pitch mode skyhook damping coefficient (full-act)	c_{pF}	100 kNsm^{-1}
Bounce mode skyhook damping coefficient (full-act)	c_{bS}	$1.4 \times c_{bF}$
Pitch mode skyhook damping coefficient (full-act)	c_{pS}	$1.8 \times c_{pF}$