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<https://doi.org/10.1063/1.5086423>

PUBLISHER

AIP Publishing

VERSION

AM (Accepted Manuscript)

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<https://hdl.handle.net/2134/37057>.

Temperature dependence of the effective spin-mixing conductance probed with lateral non-local spin valves

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We report the temperature dependence of the effective spin-mixing conductance between a normal metal (aluminium, Al) and a magnetic insulator ($\text{Y}_3\text{Fe}_5\text{O}_{12}$, YIG). Non-local spin valve devices, using Al as the spin transport channel, were fabricated on top of YIG and SiO_2 substrates. By comparing the spin relaxation lengths in the Al channel on the two different substrates, we calculate the effective spin-mixing conductance (G_s) to be $3.3 \times 10^{12} \Omega^{-1}\text{m}^{-2}$ at 293 K for the Al/YIG interface. A decrease of up to 84% in G_s is observed when the temperature (T) is decreased from 293 K to 4.2 K, with G_s scaling with $(T/T_c)^{3/2}$. The real part of the spin-mixing conductance ($G_r \approx 5.7 \times 10^{13} \Omega^{-1}\text{m}^{-2}$), calculated from the experimentally obtained G_s , is found to be approximately independent of the temperature. We evidence a hitherto unrecognized underestimation of G_r extracted from the modulation of the spin signal by rotating the magnetization direction of YIG with respect to the spin accumulation direction in the Al channel, which is found to be 50 times smaller than the calculated value.

The transfer of spin information between a normal metal (NM) and a magnetic insulator (MI) is the crux of electrical injection and detection of spins in the rapidly emerging fields of magnon spintronics¹ and antiferromagnetic spintronics^{2,3}. The spin current flowing through the NM/MI interface is governed by the spin-mixing conductance⁴⁻⁷, $G_{\uparrow\downarrow}$, which plays a crucial role in spin transfer torque⁸⁻¹⁰, spin pumping^{11,12}, spin Hall magnetoresistance (SMR)^{13,14} and spin Seebeck experiments¹⁵. In these experiments, the spin-mixing conductance ($G_{\uparrow\downarrow} = G_r + iG_i$), composed of a real (G_r) and an imaginary part (G_i), determines the transfer of spin angular momentum between the spin accumulation ($\vec{\mu}_s$) in the NM and the magnetization ($\vec{M}$) of the MI in the *non-collinear* case. However, recent experiments on the spin Peltier effect¹⁶, spin sinking¹⁷ and non-local magnon transport in magnetic insulators^{18,19} necessitate the transfer of spin angular momentum through the NM/MI interface also in the *collinear* case ($\vec{\mu}_s \parallel \vec{M}$). This is taken into account by the effective spin-mixing conductance (G_s) concept, according to which the transfer of spin angular momentum across the NM/MI interface can occur, irrespective of the mutual orientation between $\vec{\mu}_s$ and $\vec{M}$, via local thermal fluctuations of the equilibrium magnetization (thermal magnons²⁰) in the MI. The spin current density ($\vec{j}_s$) through the NM/MI interface can, therefore, be expressed as^{17,21,22}:

$$\vec{j}_s = G_r \hat{m} \times (\vec{\mu}_s \times \hat{m}) + G_i (\vec{\mu}_s \times \hat{m}) + G_s \vec{\mu}_s, \quad (1)$$

where, $\hat{m}$ is a unit vector pointing along the direction of $\vec{M}$. While G_r and G_i have been extensively studied

in spin torque and SMR experiments²³⁻²⁵, direct experimental studies on the temperature dependence of G_s are lacking.

In this letter, we report the first systematic study of G_s versus temperature (T) for a NM/MI interface. For this, we utilize the lateral non-local spin valve (NLSV) geometry, which provides an alternative way to study the spin-mixing conductance using pure spin currents in a NM with low spin-orbit coupling (SOC)^{17,26,27}. A low SOC of the NM in the NLSV technique also ensures that the spin-mixing conductance is not overestimated due to spurious proximity effects in NMs with high SOC or close to the Stoner criterion, such as Pt²⁸⁻³⁰. We exclusively address the temperature dependence of G_s for the aluminium (Al)/ $\text{Y}_3\text{Fe}_5\text{O}_{12}$ (YIG) interface, which is obtained by comparing the spin relaxation length (λ_N) in similar Al channels on a magnetic YIG substrate and a non-magnetic SiO_2 substrate, as a function of temperature. G_s decreases by about 84% when the temperature is decreased from 293 K to 4.2 K and scales with $(T/T_c)^{3/2}$, where $T_c = 560$ K is the Curie temperature of YIG, consistent with theoretical predictions^{19,31-33}. The real part of the spin-mixing conductance (G_r) is then calculated from the experimentally obtained values of G_s and compared with the modulation of the spin signal in rotation experiments, where the magnetization direction of YIG ($\vec{M}$) is rotated with respect to $\vec{\mu}_s$.

The NLSVs with Al spin transport channel were fabricated on top of YIG and SiO_2 thin films in multiple steps using electron beam lithography (EBL), electron beam evaporation of the metallic layers and resist lift-off technique, following the procedure described in Ref. 34. The 210 nm thick YIG film on $\text{Gd}_3\text{Ga}_5\text{O}_{12}$ substrate and the 300 nm thick SiO_2 film on Si substrate were obtained commercially from Matesy GmbH and Silicon Quest International, respectively. Permalloy ($\text{Ni}_{80}\text{Fe}_{20}$, Py) has

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FIG. 1. (a) Schematic illustration of the experimental geometry. The spin accumulation ($\vec{\mu}_s$), injected into the Al channel by the Py injector, has an additional relaxation pathway into the (insulating) magnetic YIG substrate due to local thermal fluctuations of the equilibrium YIG magnetization ($\vec{M}$) or thermal magnons. (b) SEM image of a representative NLSV device along with the illustration of the electrical connections for the NLSV measurements. An alternating current (I) was sourced from the left Py strip (injector) to the left end of the Al channel and the non-local voltage (V_{NL}) was measured across the right Py strip (detector) with reference to the right end of the Al channel. An external magnetic field (B) was swept along the y -axis in the non-local spin valve (NLSV) measurements. In the rotation measurements, B was applied at different angles (θ) with respect to the y -axis in the xy -plane. (c) NLSV measurements at $T = 293$ K for an Al channel length (L) of 300 nm on the YIG substrate (red) and on the SiO_2 substrate (black).

been used as the ferromagnetic electrodes for injecting and detecting a non-equilibrium spin accumulation in the Al channel. A 3 nm thick Ti underlayer was deposited prior to the evaporation of the 20 nm thick Py electrodes. The Ti underlayer prevents direct injection and detection of spins in the YIG substrate via the anomalous spin Hall effect in Py^{35,36}. *In-situ* Ar⁺ ion milling for 20 seconds at an Ar gas pressure of 4×10^{-5} Torr was performed, prior to the evaporation of the 55 nm thick Al channel, ensuring a transparent and clean Py/Al interface. A schematic of the device geometry is depicted in Fig. 1(a) and a scanning electron microscope (SEM) image of a representative device is shown in Fig. 1(b). A low frequency (13 Hz) alternating current source (I) with an r.m.s. amplitude of 400 μA was connected between the left Py strip (injector) and the left end of the Al channel. The non-local voltage (V_{NL}) due to the non-equilibrium spin accumulation in the Al channel was measured between the right Py strip (detector) and the right end of the Al channel using a standard lock-in technique. The measurements were carried out under a low vacuum atmosphere in a variable temperature insert, placed within a superconducting magnet.

In the NLSV measurements, an external magnetic field (B) was swept along the y -axis and the corresponding non-local resistance ($R_{NL} = V_{NL}/I$) was measured. In Fig. 1(c), NLSV measurements for an Al channel length (L) of 300 nm at $T = 293$ K are shown for two devices, one on YIG (red) and another on SiO_2 (black). The spin signal, $R_s = R_{NL}^P - R_{NL}^{AP}$, is defined as the difference in the two distinct states corresponding to the parallel (R_{NL}^P) and the anti-parallel (R_{NL}^{AP}) alignment of the Py electrodes' magnetizations. The R_s was measured as a function of the separation (L) between the injector and

the detector electrodes for several devices fabricated on YIG and SiO_2 substrates, as shown in Fig. 2(a). To determine the spin relaxation length (λ_N) in the Al channels on YIG ($\lambda_{N, \text{YIG}}$) and SiO_2 ($\lambda_{N, \text{SiO}_2}$) substrates, the experimental data in Fig. 2(a) were fitted with the spin diffusion model³⁷ for transparent contacts:

$$R_s = \frac{4\alpha_F^2}{(1 - \alpha_F^2)^2} \mathcal{R}_N \left(\frac{\mathcal{R}_F}{\mathcal{R}_N} \right)^2 \frac{e^{-L/\lambda_N}}{1 - e^{-2L/\lambda_N}}, \quad (2)$$

where, α_F is the bulk spin polarization of Py, $\mathcal{R}_N = \rho_N \lambda_N / w_N t_N$ and $\mathcal{R}_F = \rho_F \lambda_F / w_F t_F$ are the spin resistances of Al and Py, respectively. $\lambda_{N(F)}$, $\rho_{N(F)}$, $w_{N(F)}$ and t_N are the spin relaxation length, electrical resistivity, width and thickness of Al (Py), respectively. At room temperature, $\lambda_{N, \text{YIG}} = (276 \pm 30)$ nm and $\lambda_{N, \text{SiO}_2} = (468 \pm 20)$ nm were extracted, with $\alpha_F \lambda_F = (0.84 \pm 0.05)$ nm.

The NLSV measurements were carried out at different temperatures, enabling the extraction of $\lambda_{N, \text{YIG}}$ and $\lambda_{N, \text{SiO}_2}$, as shown in Fig. 2(b). From this temperature dependence, it is obvious that $\lambda_{N, \text{YIG}}$ is lower than $\lambda_{N, \text{SiO}_2}$ throughout the temperature range of 4.2 K to 293 K. The corresponding electrical conductivities of the Al channel (σ_N) on the two different substrates were also measured by the four-probe technique as a function of T , as shown in Fig. 2(c). The similar values of σ_N for the Al channels on both YIG and the SiO_2 substrates suggests that there is no significant difference in the structure and quality of the Al films between the two substrates. Therefore, considering the dominant Elliott-Yafet spin relaxation mechanism in Al³⁸, differences in the spin relaxation rate within the Al channels cannot account for the difference in the effective spin relaxation lengths between the two substrates.

FIG. 2. (a) The spin signal (R_s) plotted as a function of the Al channel length (L) for NLSV devices on YIG (red circles) and SiO₂ (black square) substrates at 293 K. The solid lines represent the fits to the spin diffusion model (Eq. 2). (b) The effective spin relaxation length in the Al channel (λ_N) extracted at different temperatures (T). λ_N is smaller on the YIG substrate as compared to the SiO₂ substrate. (c) The electrical conductivity (σ_N) of the Al channels on the YIG and the SiO₂ substrates as a function of temperature. The close match between the two conductivities suggests similar quality of the Al film grown on both substrates.

The smaller values of $\lambda_{N, \text{YIG}}$ as compared to $\lambda_{N, \text{SiO}_2}$ suggest that there is an additional spin relaxation mechanism for the spin accumulation in the Al channel on the magnetic YIG substrate. This is expected via additional spin-flip scattering at the Al/YIG interface, mediated by thermal magnons in YIG and governed by the effective spin-mixing conductance (G_s). As described in Ref. 17, $\lambda_{N, \text{YIG}}$ and $\lambda_{N, \text{SiO}_2}$ are related to G_s as

$$\frac{1}{\lambda_{N, \text{YIG}}^2} = \frac{1}{\lambda_{N, \text{SiO}_2}^2} + \frac{1}{\lambda_r^2}, \quad (3)$$

where, $\lambda_r = 2G_s/(t_{\text{Al}}\sigma_N)$. Using the extracted values of λ_N from Fig. 2(b) and the measured values of σ_N for the devices on YIG from Fig. 2(c), we calculate $G_s = 3.3 \times 10^{12} \Omega^{-1} \text{m}^{-2}$ at 293 K. At 4.2 K, G_s decreases by about 84% to $5.4 \times 10^{11} \Omega^{-1} \text{m}^{-2}$.

The temperature dependence of G_s is shown in Fig. 3(a). Since the concept of the effective spin-mixing conductance is based on the thermal fluctuation of the magnetization (thermal magnons), G_s is expected to scale as $(T/T_c)^{3/2}$, where T_c is the Curie temperature of the magnetic insulator^{6,19,31,32}. Using $T_c = 560$ K for YIG, we fit the experimental data to $C(T/T_c)^{3/2}$, which is depicted as the solid line in Fig. 3(a). The temperature independent prefactor, C , was found to be $8.6 \times 10^{12} \Omega^{-1} \text{m}^{-2}$. The agreement with the experimental data confirms the expected scaling of G_s with temperature. Note that the deviation from the $(T/T_c)^{3/2}$ scaling at lower temperatures could be in part due to slightly different quality of the Al film on the YIG substrate. Nevertheless, the small difference of $\approx 10\%$ in the electrical conductivities of the Al channel on the two different substrates at $T < 100$ K in Fig. 2(c) cannot account for the differences in λ_N . On the other hand, we note that quantum magnetization fluctuations^{39,40} in YIG can also play a role at low T , leading to an enhanced G_s .

Next, we investigate the temperature dependence of the real part of the spin-mixing conductance (G_r). For

this, we first calculate G_r from the experimentally obtained G_s , using the following expression¹⁹:

$$G_s = \frac{3\zeta(3/2)}{2\pi s \Lambda^3} G_r, \quad (4)$$

where $\zeta(3/2) = 2.6124$ is the Riemann zeta function calculated at $3/2$, $s = S/a^3$ is the spin density with total spin $S = 10$ in a unit cell of volume $a^3 = 1.896 \text{ nm}^3$, and $\Lambda = \sqrt{4\pi D_s/k_B T}$ is the thermal de Broglie wavelength for magnons, with $D_s = 8.458 \times 10^{-40} \text{ Jm}^2$ being the spin wave stiffness constant for YIG^{19,41}. The temperature dependence of the calculated G_r is shown in Fig. 3(b). Keeping in mind that Eq. 4 is not valid in the limits of $T \rightarrow T_c$ and $T \rightarrow 0$, we ignore the data points below 100 K. Above this temperature, G_r is almost constant at $\approx 5.7 \times 10^{13} \Omega^{-1} \text{m}^{-2}$, represented by the dashed line in Fig. 3(b). This is consistent with Ref. 25, where G_r was found to be T -independent. Moreover, the magnitude of G_r is comparable with previously reported values for

FIG. 3. (a) Temperature dependence of the effective spin-mixing conductance (black symbols). G_s scales with the temperature as $(T/T_c)^{3/2}$ (solid line). (b) The real part of the spin-mixing conductance (G_r) is calculated from Eq. 4 by using the experimentally obtained values of G_s . G_r ($\approx 5.7 \times 10^{13} \Omega^{-1} \text{m}^{-2}$) is essentially found to be constant (dashed line) for $T > 100$ K.

FIG. 4. (a) NLSV measurement for a device on the YIG substrate with $L = 300$ nm at 150 K. (b) Rotation measurement for the same device with $B = 20$ mT applied at different angles (θ) with respect to the y -axis. The black and the red symbols correspond to the average of ten rotation measurements carried out with the magnetization of the Py electrodes in the parallel (P) and the anti-parallel (AP) configurations, respectively. (c) The spin signal ($R_s = R_{\text{NL}}^{\text{P}} - R_{\text{NL}}^{\text{AP}}$) exhibits a periodic modulation of magnitude ΔR_s when the angle θ between the magnetization direction in YIG ($\vec{M}$) and the spin accumulation direction in Al ($\vec{\mu}_s$) is changed. The black symbols represent the experimental data at 150 K, while the red line is the numerical modelling result corresponding to $G_r = 1 \times 10^{12} \Omega^{-1}\text{m}^{-2}$.

Al/YIG¹⁷ and Pt/YIG^{19,42} interfaces.

An alternative approach for extracting G_r from the NLSVs fabricated on the YIG substrate, is by the rotation of the sample with respect to a low magnetic field in the xy -plane. We have also followed this method, described in Refs. 17 and 26. In the rotation experiments, the angle θ between the magnetization direction in YIG ($\vec{M}$) and the spin accumulation direction in Al ($\vec{\mu}_s$) is changed, which results in the modulation of the spin signal in the Al channel due to the transfer of spin angular momentum across the Al/YIG interface, as described in Eq. 1, dominated by the G_r term. First, the NLSV measurement for a device with $L = 300$ nm was carried out at 150 K, as shown in Fig. 4(a). In the next step, $B = 20$ mT was applied in the xy -plane and the sample was rotated, with the magnetization orientations of the Py electrodes set in the parallel (P) or the anti-parallel (AP) configuration. For improving the signal-to-noise ratio, ten measurements were performed for each of the configurations (P and AP). The average of these measurements is shown in Fig. 4(b). The spin signal is extracted from Fig. 4(b) and plotted as a function of θ in Fig. 4(c). R_s exhibits a periodic modulation with the maxima at $\theta = 0^\circ$ and minima at $\theta = \pm 90^\circ$, consistent with the behaviour predicted in Eq. 1. The modulation in the R_s , defined as $\frac{(R_s^{0^\circ} - R_s^{\pm 90^\circ})}{R_s^{0^\circ}} = \frac{\Delta R_s}{R_s^{0^\circ}}$, was found to be 2.8%. A similar modulation of 2.9% was reported in Ref 26 for an NLSV with a Cu channel on YIG with $L = 570$ nm at the same temperature.

G_r is estimated from the rotation measurements using 3D finite element modelling, as described in Ref. 17. From the modelled curve for the spin signal modulation, shown as the red line in Fig. 4(c), we extract $G_r = 1 \times 10^{12} \Omega^{-1}\text{m}^{-2}$. This value is comparable to that reported in Ref. 26, within a factor of 2, for an evaporated Cu channel on YIG. However, this value is more than 50 times smaller than our estimated value from Eq. 4, and

also that reported in Ref. 17 for a sputtered Al channel on YIG. One reason behind the small magnitude of G_r extracted from the rotation measurements can be attributed to the thin film deposition technique used. In Ref. 14, it was shown that the SMR signal for a sputtered Pt film on YIG is about an order of magnitude larger than that for an evaporated Pt film. Moreover, during the fabrication of our NLSVs, an Ar^+ ion milling step is carried out prior to the evaporation of the NM channel for ensuring a clean interface between the NM and the ferromagnetic injector and detector electrodes^{17,26}. Consequently, this also leads to the milling of the YIG surface on which the NM is deposited, resulting in the formation of an ≈ 2 nm thick amorphous YIG layer at the interface⁴³. Since an external magnetic field of 20 mT is not sufficient to completely align the magnetization direction within this amorphous layer parallel to the field direction⁴⁴, the resulting modulation in the spin signal will be smaller. This might lead to the underestimation of G_r . Note that since the effect of G_s does not depend on the magnetization orientation of YIG (Eq. 1), the milling does not affect the estimation of G_s . Our observations are consistent with a similarly small value of $G_r \approx 4 \times 10^{12} \Omega^{-1}\text{m}^{-2}$ reported in Ref. 26 for the Cu/YIG interface, where the Cu channel was evaporated following a similar Ar^+ ion milling step. Using the reported values of $\lambda_N = 522$ nm (680 nm) on YIG (SiO_2) substrate for the 100 nm thick Cu channel at 150 K in Ref. 26, we extract $G_s = 2 \times 10^{12} \Omega^{-1}\text{m}^{-2}$, which is 5 times larger than their reported G_r extracted from rotation measurements.

In summary, we have studied the temperature dependence of G_s and G_r using the non-local spin valve technique for the Al/YIG interface. From NLSV measurements, we extracted G_s to be $3.3 \times 10^{12} \Omega^{-1}\text{m}^{-2}$ at 293 K, which decreases by about 84% at 4.2 K, approximately obeying the $(T/T_c)^{3/2}$ law. While G_r remains almost constant with the temperature, the value extracted from

the modulation of the spin signal ($1 \times 10^{12} \Omega^{-1}\text{m}^{-2}$) was around 50 times smaller than the calculated value ($5.7 \times 10^{13} \Omega^{-1}\text{m}^{-2}$). The lower estimate of G_r from the rotation experiment can be attributed to the formation of an amorphous YIG layer at the interface due to Ar^+ ion milling prior to the evaporation of the Al channel, a consideration missing in the literature so far.

ACKNOWLEDGMENTS

We acknowledge the technical support from J. G. Holstein, H. M. de Roos, H. Adema, T. Schouten and H. de Vries and thank G. E. W. Bauer and F. Casanova for discussions. We acknowledge the financial support of the Zernike Institute for Advanced Materials and the Future and Emerging Technologies (FET) programme within the Seventh Framework Programme for Research of the European Commission, under FET-Open Grant No. 618083 (CNTQC). This project is also financed by the NWO Spinoza prize awarded to Prof. B. J. van Wees by the NWO.

- ¹A. V. Chumak, V. I. Vasyuchka, A. A. Serga, and B. Hillebrands, *Nature Physics* **11**, 453 (2015).
- ²T. Jungwirth, X. Marti, P. Wadley, and J. Wunderlich, *Nature Nanotechnology* **11**, 231 (2016).
- ³V. Baltz, A. Manchon, M. Tsoi, T. Moriyama, T. Ono, and Y. Tserkovnyak, *Rev. Mod. Phys.* **90**, 015005 (2018).
- ⁴A. Brataas, Y. V. Nazarov, and G. E. W. Bauer, *Phys. Rev. Lett.* **84**, 2481 (2000).
- ⁵A. Brataas, G. E. W. Bauer, and P. J. Kelly, *Physics Reports* **427**, 157 (2006).
- ⁶S. Takahashi, E. Saitoh, and S. Maekawa, *J. Phys.: Conf. Ser.* **200**, 062030 (2010).
- ⁷X. Jia, K. Liu, K. Xia, and G. E. W. Bauer, *EPL* **96**, 17005 (2011).
- ⁸M. D. Stiles and A. Zangwill, *Phys. Rev. B* **66**, 014407 (2002).
- ⁹D. C. Ralph and M. D. Stiles, *Journal of Magnetism and Magnetic Materials* **320**, 1190 (2008).
- ¹⁰A. Brataas, A. D. Kent, and H. Ohno, *Nature Materials* **11**, 372 (2012).
- ¹¹Y. Tserkovnyak, A. Brataas, and G. E. W. Bauer, *Phys. Rev. Lett.* **88**, 117601 (2002).
- ¹²P. Deorani and H. Yang, *Appl. Phys. Lett.* **103**, 232408 (2013).
- ¹³H. Nakayama, M. Althammer, Y.-T. Chen, K. Uchida, Y. Kajiwara, D. Kikuchi, T. Ohtani, S. Geprägs, M. Opel, S. Takahashi, R. Gross, G. E. W. Bauer, S. T. B. Goennenwein, and E. Saitoh, *Phys. Rev. Lett.* **110**, 206601 (2013).
- ¹⁴N. Vlietstra, J. Shan, V. Castel, B. J. van Wees, and J. Ben Youssef, *Phys. Rev. B* **87**, 184421 (2013).
- ¹⁵K. Uchida, J. Xiao, H. Adachi, J. Ohe, S. Takahashi, J. Ieda, T. Ota, Y. Kajiwara, H. Umezawa, H. Kawai, G. E. W. Bauer, S. Maekawa, and E. Saitoh, *Nature Materials* **9**, 894 (2010).
- ¹⁶J. Flipse, F. Dejene, D. Wagenaar, G. Bauer, J. B. Youssef, and B. van Wees, *Phys. Rev. Lett.* **113**, 027601 (2014).
- ¹⁷F. K. Dejene, N. Vlietstra, D. Luc, X. Waintal, J. Ben Youssef, and B. J. van Wees, *Phys. Rev. B* **91**, 100404 (2015).
- ¹⁸L. J. Cornelissen, J. Liu, R. A. Duine, J. B. Youssef, and B. J. v. Wees, *Nature Physics* **11**, 1022 (2015).
- ¹⁹L. J. Cornelissen, K. J. H. Peters, G. E. W. Bauer, R. A. Duine, and B. J. van Wees, *Phys. Rev. B* **94**, 014412 (2016).
- ²⁰B. A. Kalinikos and A. N. Slavin, *J. Phys. C: Solid State Phys.* **19**, 7013 (1986).
- ²¹A. Brataas, Y. Tserkovnyak, G. E. W. Bauer, and P. J. Kelly, in *Spin Current*, edited by S. Maekawa, S. O. Valenzuela, E. Saitoh, and T. Kimura (Oxford University Press, United Kingdom, 2012) pp. 87–135.
- ²²Y.-T. Chen, S. Takahashi, H. Nakayama, M. Althammer, S. T. B. Goennenwein, E. Saitoh, and G. E. W. Bauer, *Phys. Rev. B* **87**, 144411 (2013).
- ²³K. Xia, P. J. Kelly, G. E. W. Bauer, A. Brataas, and I. Turek, *Phys. Rev. B* **65**, 220401 (2002).
- ²⁴N. Vlietstra, J. Shan, V. Castel, J. Ben Youssef, G. E. W. Bauer, and B. J. van Wees, *Appl. Phys. Lett.* **103**, 032401 (2013).
- ²⁵S. Meyer, M. Althammer, S. Geprägs, M. Opel, R. Gross, and S. T. B. Goennenwein, *Appl. Phys. Lett.* **104**, 242411 (2014).
- ²⁶E. Villamor, M. Isasa, S. Vélez, A. Bedoya-Pinto, P. Vavassori, L. E. Hueso, F. S. Bergeret, and F. Casanova, *Phys. Rev. B* **91**, 020403 (2015).
- ²⁷P. K. Muduli, M. Kimata, Y. Omori, T. Wakamura, S. P. Dash, and Y. Otani, *Phys. Rev. B* **98**, 024416 (2018).
- ²⁸S. Y. Huang, X. Fan, D. Qu, Y. P. Chen, W. G. Wang, J. Wu, T. Y. Chen, J. Q. Xiao, and C. L. Chien, *Phys. Rev. Lett.* **109**, 107204 (2012).
- ²⁹Y. M. Lu, J. W. Cai, S. Y. Huang, D. Qu, B. F. Miao, and C. L. Chien, *Phys. Rev. B* **87**, 220409 (2013).
- ³⁰A. B. Cahaya, O. A. Tretiakov, and G. E. W. Bauer, *Appl. Phys. Lett.* **104**, 042402 (2014).
- ³¹S. S.-L. Zhang and S. Zhang, *Phys. Rev. B* **86**, 214424 (2012).
- ³²S. A. Bender and Y. Tserkovnyak, *Phys. Rev. B* **91**, 140402 (2015).
- ³³J. Xiao and G. E. W. Bauer, *arXiv:1508.02486 [cond-mat]* (2015), arXiv: 1508.02486.
- ³⁴K. S. Das, F. K. Dejene, B. J. van Wees, and I. J. Vera-Marun, *Phys. Rev. B* **94**, 180403 (2016).
- ³⁵K. S. Das, W. Y. Schoemaker, B. J. van Wees, and I. J. Vera-Marun, *Phys. Rev. B* **96**, 220408 (2017).
- ³⁶K. S. Das, J. Liu, B. J. van Wees, and I. J. Vera-Marun, *Nano Lett.* **18**, 5633 (2018).
- ³⁷S. Takahashi and S. Maekawa, *Phys. Rev. B* **67**, 052409 (2003).
- ³⁸I. Žutić, J. Fabian, and S. Das Sarma, *Rev. Mod. Phys.* **76**, 323 (2004).
- ³⁹A. Zholud, R. Freeman, R. Cao, A. Srivastava, and S. Urazhdin, *Phys. Rev. Lett.* **119**, 257201 (2017).
- ⁴⁰J. W. Kim, S. Khim, S. H. Chun, Y. Jo, L. Balicas, H. T. Yi, S.-W. Cheong, N. Harrison, C. D. Batista, J. Hoon Han, and K. Hoon Kim, *Nature Communications* **5**, 4419 (2014).
- ⁴¹V. Cherepanov, I. Kolokolov, and V. L'vov, *Physics Reports* **229**, 81 (1993).
- ⁴²S. Vélez, A. Bedoya-Pinto, W. Yan, L. E. Hueso, and F. Casanova, *Phys. Rev. B* **94**, 174405 (2016).
- ⁴³F. Casanova, “Private communication,” (2018).
- ⁴⁴D. Wesenberg, T. Liu, D. Balzar, M. Wu, and B. L. Zink, *Nature Physics* **13**, 987 (2017).