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Abstract:	In recent years thanks to enhancements in design of advanced machines, laser metrology and computer control, ultra-precision machining has become increasingly important. In micromachining of metals the depth of cut is usually less than the average grain size of a polycrystalline aggregate; hence, a cutting process can occur entirely within a single crystal. The respective effect of crystallographic anisotropy requires development of machining models that incorporate crystal plasticity for an accurate prediction of micro-scale material removal under such conditions. To achieve this, a 3D finite-element model of orthogonal micro-cutting of a single crystal of b.c.c. brass was implemented in a commercial software ABAQUS/Explicit using a user-defined subroutine VUMAT. Strain-gradient crystal-plasticity theories were used to demonstrate the influence of evolved strain gradients on the cutting process for different cutting directions.	

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Strain-gradient crystal-plasticity modelling of micro-cutting of b.c.c. single crystal

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Abstract

25 In recent years thanks to enhancements in design of advanced machines, laser metrology and computer control, ultra-precision machining has increasingly become important. In micromachining of metals the depth of cut is usually less than the average grain size of a polycrystalline aggregate; hence, a cutting process can occur entirely within a single crystal. The respective effect of crystallographic anisotropy requires development of machining models that incorporate crystal plasticity for an accurate prediction of micro-scale material removal under such conditions. To achieve this, a 3D finiteelement model of orthogonal micro-cutting of a single crystal of b.c.c. brass was implemented in a commercial software ABAQUS/Explicit using a user-defined subroutine VUMAT. Strain-gradient 56 crystal-plasticity theories were 58 demonstrate the influence of evolved strain

gradients on the cutting process for different cutting directions.

Keywords: Strain-gradient crystal-plasticity; orthogonal micro-cutting, brass single crystal; finite-element analysis

1 Introduction and motivation

With continuous miniaturization of industrial products, understanding micro-scale of of materials deformation increases in significance. In micromachining of metals, the depth of cut is usually less than the average grain size of a polycrystalline aggregate. As a result, the cutting action may occur entirely within a single crystal. In the experimental micromachining studies, such parameters as the cutting force, shear angle, dynamic shear stress and chip thickness were observed to depend on the orientation of the cutting direction and the cutting-plane normal with respect to the crystal axis. This is naturally

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explained by the fact that single crystals are highly 1 anisotropic in their physical properties [1]. To elucidate the underlying physics for the micromachining process, different analytical numerical models were proposed.

Sato [2] tried to use the continuum yield theory to 12 analyse changes in the shear stress and shear angle with material anisotropy, but the attempt was unsuccessful as the value of the shear angle was in the reverse phase to shear stress. Later, Sato et al. [3] calculated the shear angle from the vector sum of slip directions on active slip systems based on the assumption that the amount of shearing on the slips system is proportional to its Schmid factor. Shirakashi et al. [4] used the Hill's orthogonal plastic anisotropy theory to predict shear angles in cutting f.c.c. single crystals. This approach, however, was found to be not suitable for predicting machining forces. Lee and Zhou [5] and Lee et al. [6] used an effective Taylor factor to predict a shear angle in single-crystal cutting. For each crystallographic orientation, this factor was calculated for all possible shear angles. However, it was observed (based on the minimum energy criterion) that a range of shear angles might exist for a given type of material's anisotropy. The authors proposed that the most likely shear angle was the one corresponding to the most negative texture-softening factor among the ones with the same minimum shear strength. This work was then extended using Merchant's model to predict the change in cutting forces with crystallographic orientation. Recently,

Kota and Ozdoganlar [7] developed a plasticitybased model of a machining force combining the Bishop and Hill's crystal plasticity models with the Merchant's orthogonal cutting model; the experimental validation of the model was carried out. All these analytical models were developed based on assumption of plain-strain orthogonal cutting.

Continuum numerical models of micro-scale material removal processes compared to analytical ones are very limited. Liang et al. [8] attempted to predict the effects of crystal orientation and grain boundaries on cutting forces using 2D finiteelement (FE) analysis. However, in that study deformation was confined only to the elastic region. Liu and Melkote [9] developed a 3D FE model of micro-cutting including strain-gradient effects. In their study the crystallographic anisotropy was not accounted for in the constitutive equations. Recently, Zahedi et al. [10] and Demiral et al. [11] investigated the effect of crystallographic anisotropy on a response of copper single crystal using a 3D smoothed particle hydrodynamics/FE crystal plasticity model and a strain-gradient crystal-plasticity FE model. respectively.

At the experiments same time, recent demonstrated that metallic materials displayed a strong size effect at the micron and sub-micron scales [12,13]. This phenomenon was attributed to of geometrically presence necessary dislocations (GNDs) associated with nonuniform

plastic deformation. In this regard, it becomes 1 essential to account for strain gradients, arising in 3 cutting processes, for accurate prediction of micro-scale material removal in machining models. Since conventional crystal-plasticity theories possess no intrinsic material lengths, they cannot explain the size-dependent material's 12 behaviour at small scales. In this study, an enhanced modelling scheme of a strain-gradient 15 crystal-plasticity (EMSGCP) theory proposed by 16 17 Demiral [14] is used. This work aims to 18 19 demonstrate the influence of strain gradients on 20 21 the deformation response of b.c.c. single-crystal 22 brass in the machining process. 23 24

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63 64 65 This paper is organized as follows: the details of the developed finite-element model of microcutting are introduced in Section 2. Section 3 presents its validation against experimental data and demonstrates its predictive capabilities for different cutting directions. Finally, concluding remarks are given in Section 4. The theory for a strain-gradient crystal-plasticity model with governing equations is presented in Appendix.

2 Finite-element implementation

A FE model of the orthogonal micro-machining experiment on a workpiece with dimensions 20 μ m \times 20 μ m \times 0.48 μ m (Fig. 1) was developed [11]. Considering a compromise between the accuracy and time of computations, 29600 eightnode linear brick elements (C3D8) were used to

discretise the sample, with a minimum element size of 60 nm in the process zone. The cutting tool, modelled as a rigid body with rake and clearance angles of 0°, was displaced in the cutting direction ([abc] in Fig. 1) with a velocity of -1300 mm/s. A depth of cut (a_p) was fixed at 2 μ m and the maximum cutting length of 1.2 µm considered in the simulations. Friction neglected throughout the simulation. Chip separation from the workpiece material was achieved with the use of an element-deletion module available in ABAQUS/Explicit [15]; the Taylor cumulative shear strain on all slip systems (\tilde{y}) was employed as the failure criteria. Physical shear failure occurred when this parameter reached a critical value of 3.

Fig. 1

Here, machining in a single crystal of β -brass with a b.c.c. crystalline structure is studied. It was known that the active slip system of this structure is $\{110\}<111>[16]$; therefore, only this set - from three potential system in b.c.c. materials - was enabled in the simulations. Three material parameters, $C_{11} = 131.0$ GPa, $C_{12} = 115.0$ GPa, $C_{44} = 92.0$ GPa, were used to define the elasticity tensor for the β -brass crystal [17], the respective plasticity parameters used in the simulations are listed in Table 1. The simulations were performed using the EMSGCP and enhanced modelling scheme of crystal-plasticity (EMCP) theories implemented in finite-element the

ABAQUS/Explicit [15] using the user-defined material subroutine (VUMAT). Their comparison elucidates the amount of evolving strain gradients during the deformation process. The summary of the theories is given in Appendix.

Table 1

3 Results and discussion

In this section, results of the FE simulations of orthogonal micro-cutting of single-crystal β-brass are presented. To assess the effect of rotation angle θ for a crystal with the [101] axis parallel to the observation direction (Fig. 1) on the shear angle ϕ , four cutting directions, viz. $\theta = 0^{\circ}$, -35°, -45° and -90°, were chosen. The corresponding values are listed in Table 2.

Table 2

Fig. 2 demonstrates chip shapes obtained in FE simulations based on the EMSGCP theory for different rotation angles of the (1 0 1) β -brass. Apparently, ϕ varies remarkably with θ , resulting in the corresponding values of 42°, 62°, 57° and 39° for $\theta = 0^{\circ}$, -35°, -45° and -90°, respectively (Fig. 3). In ultra-precision machining, a large shear angle is associated with continuous chip formation and good surface finish [22]. Therefore, among the cutting directions investigated here, $\theta = -35^{\circ}$ and -45° are preferable for micro-cutting of brass single crystals for a better surface finish. To

check the accuracy of the model, the obtained results were compared with the experiments presented in [16]. Our FE results demonstrated that the shear angles were predicted accurately for θ equals to -35° and -45°, while some deviations were observed for $\theta = 0^{\circ}$ and -90°. However, the general trends of the curves describing a variation of ϕ for different θ values, obtained numerically and experimentally, were in good agreement. Fig. 3 presents also the analytical results based on the analysis of the Schmid factor reported in [16]. Although the shear angles were captured successfully for $\theta = 0^{\circ}$ and -90° with this approach, a significant deviation was observed for $\theta = -35^{\circ}$, -45°. These results suggest that our numerical predictions are more in accord with the experiments when compared to the analytical ones. It should be emphasized that the frictional, thermal and viscous effects were not accounted in the present model; this might be one of the reasons for overestimation of ϕ values at $\theta = 0^{\circ}$ and -90° using FE analysis.

Fig. 2

Fig. 3

Evolution of the calculated cutting forces with an increasing cutting length for different θ values of the (1 0 1) β -brass is shown in Fig. 4. The cutting force was found to vary with different cutting directions. For instance, the measured value of the cutting force at the [-1 2.015 1] and [1 1.414 -1] directions corresponding to θ = -35° and -45°,

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respectively, are larger compared to that in the $[0 - 1 \ 1 \ 0]$ and $[-1 \ 0 \ 1]$ directions ($\theta = 0^{\circ}$ and 90° , respectively). It should be emphasized that the fluctuations observed in the cutting force occur due to variation in the shear angle during the cutting process [23].

Fig. 4

FE simulations were also performed using the EMCP theory. The results obtained with this approach demonstrate that while the EMSGCP theory predicted a cutting force that increased with an increase in the cutting length, the EMCP theory predicted the force value, stabilised at larger cutting-length magnitudes (Fig. 4). These observations are valid for all the studied cutting directions. The difference in the predicted cutting forces for the two theories was due to the fact that the EMSGCP theory characterises the contribution of strain gradients and its evolution during the inhomogeneous cutting process, and, hence, the strain-hardening rate was higher. The averages of force magnitudes for the cutting lengths of 0.6 µm and 1.2 µm were calculated; they are listed in Table 3 (F_{EMCP} and F_{EMSGCP} are the cutting force obtained with the EMCP and EMSGCP theories, respectively). As expected, the values predicted with the EMSGCP theory were noticeably larger (8–9%) when compared to those based on the EMCP theory. It was noted that the extent of respective difference significantly sensitive to the cutting direction.

Table 3

Apparently, the observed differences in realisation of micro-cutting in different directions should be underpinned by some processes at micro scale. Fig. 5 presents the distributions of the sum of magnitudes of effective GND density in all the slip systems $(\sum |n_G^{(\alpha)}|)$ for different cutting This indicates that GNDs directions. significant on the chip surface in contact with the tool for $\theta = 0^{\circ}$, whereas for other directions, the density of GNDs are larger both on that surface and in the primary deformation zone. To get an insight into the distribution of GNDs, the total accumulative shear strain on all slip systems $\tilde{\gamma}$ was checked since their density is directly proportional to the gradients of effective plastic strain. For $\theta = 0^{\circ}$, most of the shear activity and also its variation was observed on the chip surface; hence, the evolving GNDs are observed there. For $\theta = -35^{\circ}$, -45° , shearing occurred on the chip surface and in the primary deformation zone, but with to a higher extent in the former. However, the variation in $\tilde{\gamma}$ were observed in both regions; hence, an increase in the GNDs was found there. For $\theta = 90^{\circ}$, $\tilde{\gamma}$ was more evenly distributed in both regions, but its variation was more pronounced in the primary deformation zone; as a result, more GNDs were observed to occur in this region.

Fig. 5

4 Concluding remarks

In this paper, a numerical implementation of an strain-gradient crystal enhanced model of plasticity was used to demonstrate predictive capabilities of the theory in assessment of the effect of evolved strain gradients on the cutting process for different cutting directions of b.c.c. single crystals of β-brass. The shear angles predicted for different θ values using our FE model are in better agreement with the experimental data than those obtained analytically. It was noted that the amount of evolved GNDs was not significantly sensitive to the cutting direction, but their spatial positions varied considerably: for one orientation they were mostly localised on the chip surface while in other cases they also evolved in the primary shear zone. In this study, only mechanical processes - most prominent in micro-cutting - were considered. The next natural step would be to further develop the suggested approach incorporating frictional, thermal and viscous effects into the constitutive equations.

Appendix

An enhanced modelling scheme for a straingradient crystal-plasticity (EMSGCP) theory proposed by Demiral [14] was used in the simulations. Below, a bold symbol denotes a vector or a tensor and a superposed dot on a symbol indicates a material time derivative. The operation \times is a vector product, a gradient operator is indicated by ∇ , incremental changes in variables due to temporal evolution are indicated by a Δ symbol. A subscript G indicates GNDs and S implies statistically stored dislocations (SSDs).

In the EMSGCP theory, the initial strength of the slip systems $(g_T^{\alpha}|_{t=0})$, i.e. the *critical resolved* shear stress (CRSS), is governed by pre-existing GNDs in the workpiece together with SSDs, i.e. $g_T^{\alpha}|_{t=0} = \sqrt{(g_S^{\alpha}|_{t=0})^2 + (g_G^{\alpha}|_{t=0})^2}$. In this theory, $g_{\rm S}^{\alpha}|_{t=0}$ and $g_{\rm G}^{\alpha}|_{t=0}$ were linked with initial SSD ($\rho_{\rm S}|_{t=0}$) and GND ($\rho_{\rm G}|_{t=0}$) densities as $g_S^\alpha|_{t=0} = K \sqrt{\rho_s|_{t=0}} \ , \ g_G^\alpha|_{t=0} = K \sqrt{\rho|_{t=0} \big(\overline{S/V}\big)^2}$ via the constant, K, similar to the Taylor relation. The GND density term was expressed as a function of the normalized surface-to-volume $(\overline{S/V})$ ratio (hence, dimensionless) for the component under study. In this study the surfaceto-volume ratio of the workpiece materials was normalized with an idealised workpiece geometry corresponding to $S/V = 1 \, \mu \text{m}^{-1}$.

The evolution of slip resistance during loading is the result of hardening due to the SSDs (Δg_s^{α}) and GNDs (Δg_s^{α}) on the slip system, which follows:

$$g_T^{\alpha} = g_T^{\alpha} \mid_{t=0} + \sqrt{(\Delta g_S^{\alpha})^2 + (\Delta g_G^{\alpha})^2},$$

$$\Delta g_S^{\alpha} = \sum_{\beta=1}^{N} h_{\alpha\beta} \Delta \gamma^{\beta}, \quad \Delta g_G^{\alpha} = \alpha_T \mu \sqrt{b n_G^{\alpha}},$$
(1)

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here, $h_{\alpha\beta}$, $\alpha_{\rm T}$, μ , b and $n_{\rm G}^{\alpha}$ corresponds to the slipa hardening modulus, the Taylor coefficient, the shear modulus, the Burgers vector and the effective density of geometrically necessary dislocations, respectively.

The hardening model proposed by Peirce et al. [20] was used to represent $h_{\alpha\beta}$, as follows:

$$h_{\alpha\alpha} = h_0 \operatorname{sech}^2 \left| \frac{h_0 \tilde{\gamma}}{g_T^{\alpha}|_{\operatorname{sat}} - g_T^{\alpha}|_{t=0}} \right|,$$

$$h_{\alpha\beta} = q h_{\alpha\alpha} (\alpha \neq \beta),$$

$$\tilde{\gamma} = \sum_{\alpha} \int_0^t |\dot{\gamma}^{\alpha}| dt,$$
(2)

where h_0 is the initial hardening parameter, $g_T^{\alpha}|_{\text{sat}}$ is the saturation stress of the slip system α , **q** is the latent hardening ratio, and $\tilde{\gamma}$ is the Taylor cumulative shear strain on all slip systems. The effective GND density (n_G^{α}) is given by

$$n_G^{\alpha} = \left| \boldsymbol{m}^{\alpha} \times \sum_{\beta} s^{\alpha\beta} \, \nabla \gamma^{\beta} \times \boldsymbol{m}^{\beta} \right|, \tag{3}$$

where s^{α} is the slip direction, \mathbf{m}^{α} is the slip-plane normal, $s^{\alpha\beta} = \mathbf{s}^{\alpha}$. \mathbf{s}^{β} and $\nabla \gamma^{\beta}$ is the gradient of shear strain in each slip system. To calculate $\nabla \gamma^{\beta}$ the scheme proposed in Demiral et al. [24] was 52 followed.

In Eq. (2), $\dot{\gamma}^{\alpha}$ is the shearing rate on the slip system α . A power-law representation for $\dot{\gamma}^{\alpha}$ was 61 chosen:

$$\dot{\gamma}^{\alpha} = \dot{\gamma}_{0}^{\alpha} \operatorname{sgn} \left(\tau^{\alpha} \right) \left| \frac{\tau^{\alpha}}{g_{T}^{\alpha}} \right|^{n},$$
 (4)

where $\dot{\gamma}_0^{\alpha}$ is the reference strain rate, n is the macroscopic rate-sensitivity parameter, τ^{α} is the resolved shear stress, g_{τ}^{α} is the strength of the slip system α at the current time, and sgn(*) is the signum function of *.

To demonstrate the relative contribution of the evolution of GNDs to local hardening of the material in EMSGCP, an enhanced model of crystal-plasticity (EMCP) was introduced, where the incipient density of GNDs in the experimental samples was accounted for, but not GNDs evolving in the course of deformation. This model can be derived from the proposed EMSGCP theory by setting $\Delta g_G^{\alpha} = 0$ [11].

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References

[1] Lawson BL, Kota N, Ozdoganlar OB (2008) **Effects** crystallographic anistropy orthogonal micromachining of single-crystal aluminum. J Manuf Sci Eng 130(3):031116.

- [2] Sato M, Kato K, Tuchiya K (1978) Effect of material and anisotropy upon the cutting mechanism. Trans JIM 9: 530-536.
- [3] Sato M, Kato Y, Aoki S, Ikoma, A (1983)
- Effects of Crystal Orientation on the Cutting
- Mechanism of the Aluminum Single Crystal: 2nd
- 10 Report: On the (111) plane and the (112) end
- 12 Cutting. Bulletin of JSME 26(215):890-896.
- [4] Shirakashi T, Yoshino M, Kurashima H (1991)
- 15 16 Study on cutting mechanism of single crystal
- ¹⁷ based on simple shear plane model. Int J Japan
- ¹⁹ Soc Precis Eng 25(2):96-97.
- 21 [5] Lee WB, Zhou M (1993) A theoretical 22
- 23 analysis of the effect of crystallographic
- orientation on chip formation in micromachining.
- ²⁶ Int J Mach Tools Manuf 33:439-447.
- ²⁸ [6] Lee WB, Cheung CF, To S (2002) A
- ³⁰ microplasticity analysis of micro-cutting force
 - variation in ultra-precision diamond turning. J
- 34 Manuf Sci Eng 124(2):170-177.
- 36 [7] Kota N, Ozdoganlar, OB (2010) A model
 - based analysis of orthogonal cutting for single-
- 39 crystal fcc metals including crystallographic
- ⁴¹ anisotropy. Mach Sci Tech 14(1):102-127.
- 43 [8] Liang Y, Moronuki N, Furukawa, Y (1994)
- 45 Calculations of the effect of material anisotropy
- 46 47 on microcutting processes. Precis Eng 16(2):132-
- ⁴⁸ 138.

37

38

42

53

57

60 61 62

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- 50 [9] Liu K, Melkote SN (2007) Finite element
- 52 analysis of the influence of tool edge radius on
- 54 size effect in orthogonal micro-cutting process. Int
- ₅₆ J Mech Sci 49:650-660.
- ⁵⁹ Silberschmidt VV (2012) EE/SDU modelling of
 - Silberschmidt VV (2013) FE/SPH modelling of

- orthogonal micro-machining of f.c.c. single crystal. Comp Mater Sci 78:104-109.
- [11] Demiral M, Roy A, El Sayed T, Silberschmidt VV (2014) Numerical modelling of micro-machining of fcc single crystal: Influence of strain gradients. Comp Mater Sci 94: 273-278.
- [12] Huang Y, Qu S, Hwang KC, Li M, Gao H (2004) A conventional theory of mechanism-based strain gradient plasticity. Int J Plast 20(4):753-782.
- [13] Ertürk I, Van Dommelen JAW, Geers MGD (2014) Gradient crystal plasticity modelling of anelastic effects in particle strengthened metallic thin films. Meccanica 49:2657-2685.
- [14] Demiral M (2012) Enhanced gradient crystalplasticity study of size effects in b.c.c. metal. Dissertation, Loughborough University, UK.
- [15] Dassault Systemes (2013) Abaqus 6. 13 Analysis User Manual.
- [16] Ueda K, Iwata K, Nakayama K (1980) Chip formation mechanism in single crystal cutting of β-brass. CIRP Annals-Manuf Tech 29(1):41-46.
- [17] Jona F, Marcus PM (2001) Structural and elastic properties of β -brass. Journal of Physics: Condensed Matter 13(23):5507.
- [18] Jia N, Roters F, Eisenlohr P, Kords C, Raabe D (2012) Non-crystallographic shear banding in crystal plasticity FEM simulations: Example of texture evolution in α -brass. Acta Mater 60(3):1099-1115.
- [19] Beyerlein IJ, Mara NA, Bhattacharyya D, Alexander DJ, Necker CT (2011) Texture evolution via combined slip and deformation

57

63 64 65

1 nanocomposite. Int J Plast 27(1):121-146. 3 [20] Peirce D, Asaro R, Needleman A (1982) An analysis of nonuniform and localized deformation in ductile single crystals. Acta Metallur 30:1087-

twinning in rolled silver-copper cast eutectic

1119.

[21] Schulze D, Paufler P (1979) Physikalische 12 Grundlagenmechanischer Festkörpereigenschaften, Akademie-Verlag, Berlin.

[22] Lee WB (1990) Prediction of microcutting force variation in ultra-precision machining. Precis Eng 12(1):25-28.

21 [23] Tajalli SA, Movahhedy MR, Akbari J (2014) 23 Simulation of orthogonal micro-cutting of FCC materials based on rate-dependent crystal plasticity finite element model. Comp Mater Sci 86:79-87.

[24] Demiral M, Roy A, Silberschmidt VV (2013) Indentation studies in bcc crystals with enhanced model of strain-gradient crystal plasticity. Comp Mater Sci 79:896-902.

Figure captions

43 Fig. 1: Dimensions and coordinate system for 45 orthogonal cutting of single-crystal workpiece ₄₇ material

Fig. 2: Numerically obtained chip morphologies for different rotation angles of $(1\ 0\ 1)$ β -brass

Fig. 3: Variation of shear angle with rotation angle 54 obtained in experiments [16], simulations (via the EMSGCP theory) and analytical solutions [16] for $(1\ 0\ 1)\ \beta$ -brass

Fig. 4: Evolution of cutting forces obtained using EMSGCP and EMCP theories for different cutting directions

Fig. 5: Distribution of effective density of GNDs in all slip systems $\sum |n_G^{(\alpha)}|$ (top) and total accumulative shear strain on all slip systems $(\tilde{\gamma})$ (bottom) at cutting length of 2.2 μm obtained with FE simulations using EMSGCP theory for (1 0 1) single-crystal β -brass for various θ

Table captions

Table 1: Plastic parameters used in FE simulations [11,18-21]

Table 2: Different cutting directions ([abc]) and cutting-plane normals ([def]) for different θ values of [1 0 1] axis parallel to the observation direction (see Fig. 1)

Table 3: Average cutting forces obtained with EMSGCP and EMCP theories and their relative differences for different θ values.

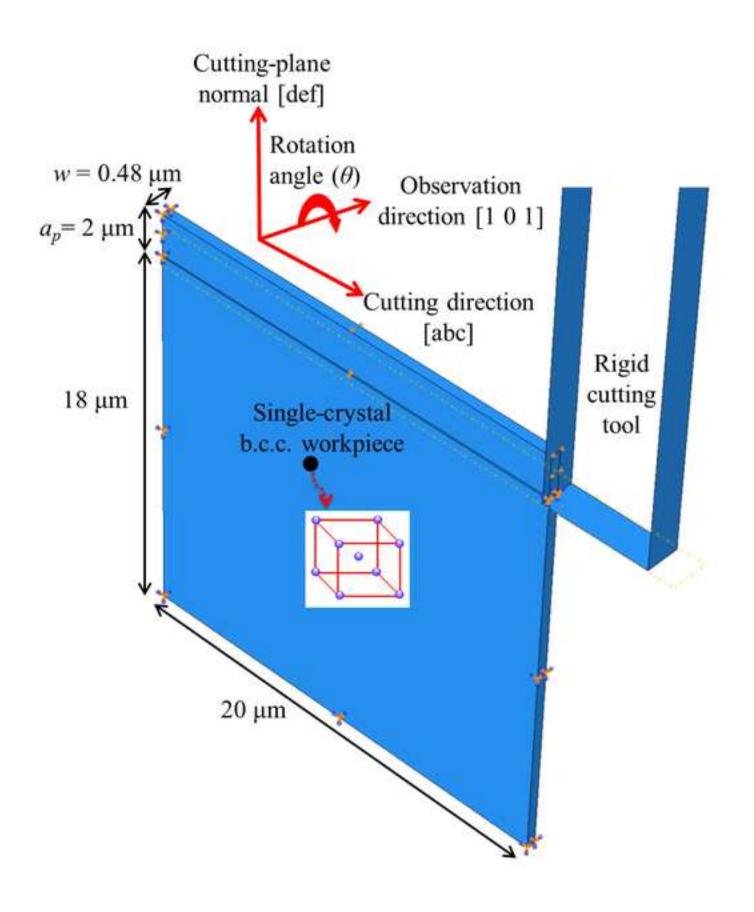
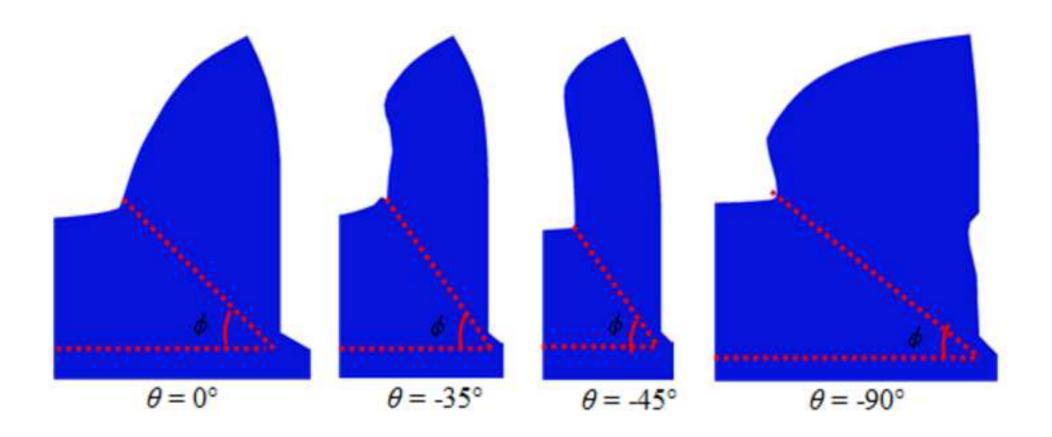


Figure2 Click here to download high resolution image



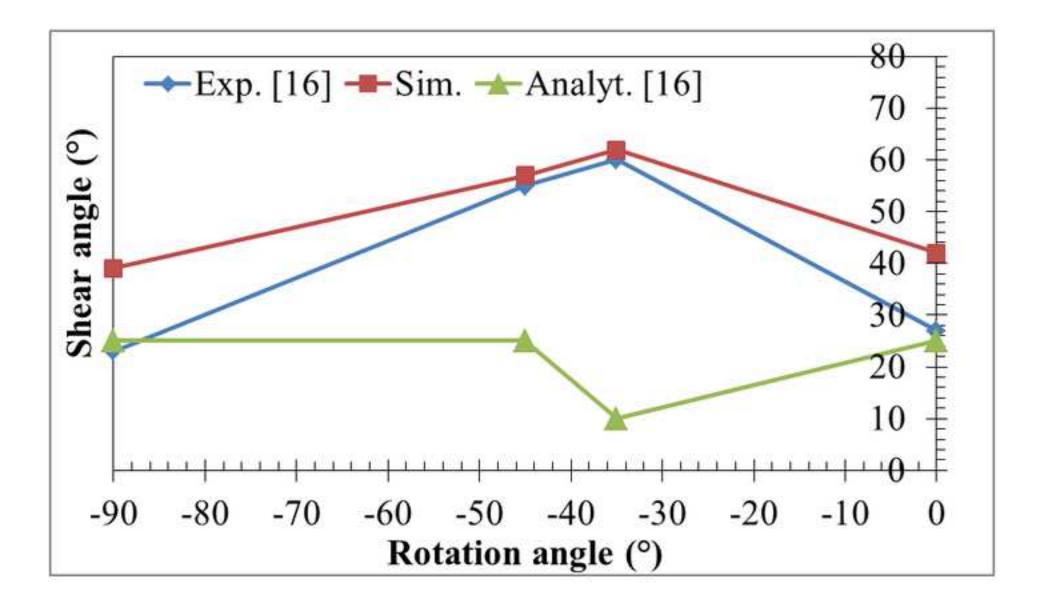


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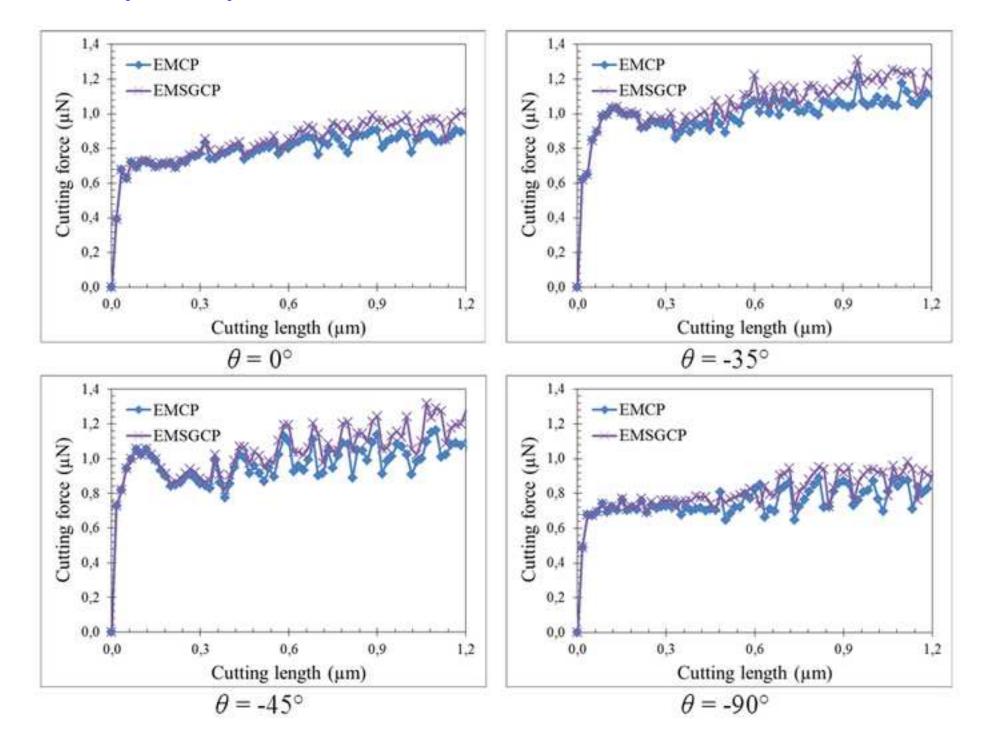
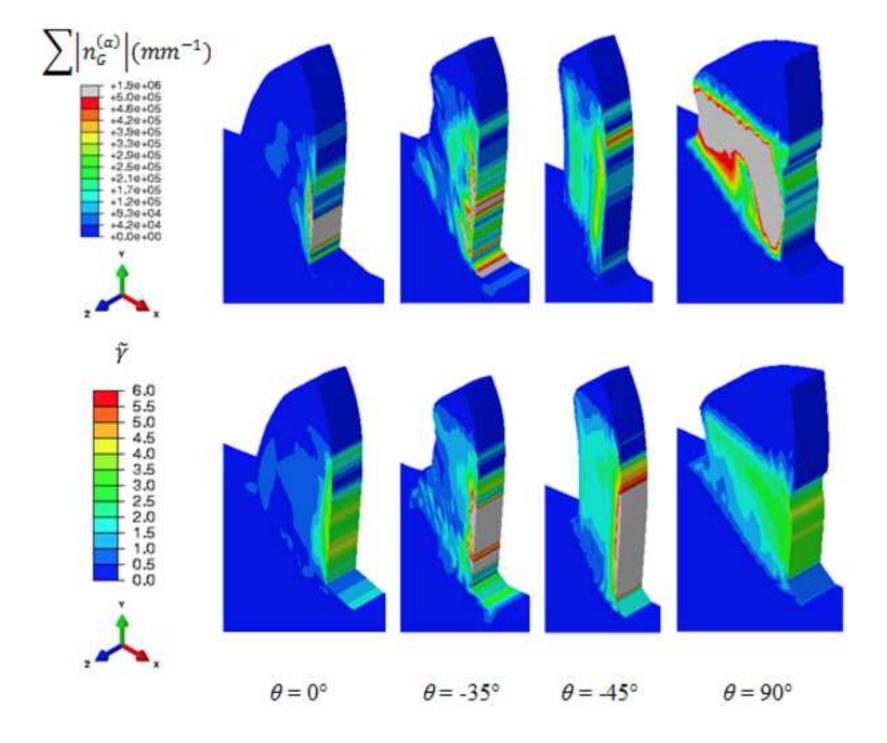


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$\dot{\gamma}_0^{\alpha} (s^{-1})$	10^{-3}	K (MPa mm)	0.04
n	20	μ _s (GPa)	27.12
q	1	b (mm)	2.56×10^{-7}
h_0 (MPa)	294	$\rho_s _{t=0} \; (\text{mm}^{-2})$	6.8 10 ⁵
$g_T^{\alpha} _{\text{sat}}$ (MPa)	60	$\rho _{t=0} \; (\text{mm}^{-2})$	5.0 104
$\alpha_{ m T}$	0.7	$\overline{S/V}$	4.36

Table2 Click here to download high resolution image

θ	0°	-35°	-45°	-90°
[abc]	$[0 - 1 \ 0]$	[-1 2.015 1]	$[1\ 1.414\ -1]$	[-1 0 1]
[def]	[-1 0 1]	[2.015 2 - 2.015]	[1 - 1.414 - 1]	[0 1 0]

Table3
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θ	$F_{\rm EMCP}(\mu { m N})$	$F_{\mathrm{EMSGCP}}\left(\mu\mathrm{N}\right)$	$(F_{\mathrm{EMSGCP}} - F_{\mathrm{EMCP}})/$ F_{EMSGCP} (%)
0°	0.853	0.929	8.18
-35°	1.063	1.165	8.81
-45°	1.027	1.139	9.86
-90°	0.801	0.875	8.48