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A computer-aided learning package for engineering students: BTEC mathematics at First and National level

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A COMPUTER-AIDED LEARNING PACKAGE
FOR
ENGINEERING STUDENTS.
B/TEC MATHEMATICS AT FIRST AND NATIONAL LEVEL.

by

ROBERT ERNEST FORD.

A Master's by Course Dissertation submitted in partial
fulfilment of the requirements for the award of the degree of
MSc in Computer Education of Loughborough University of
Technology,
January 1988.

Supervisor: H.E.BEZ, B Sc, M Sc, D Phil(Oxon)

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I would like to thank the Principal of Stamford College and the Lincolnshire Education Authority for the support I have received in producing this Computer-Aided Learning package. Particularly for the unlimited use of computer equipment which included the following:

- (i) RM NIMBUS computer and colour monitor.
- (ii) Epson dot-matrix printers LX-80 and LQ-800
- (iii) Software for word-processing "WRITE" by Oxford CC
Software for screen dumping. "PRNDUMP" by ILEA
Software for program writing. "RMBASIC" by
Research Machines Ltd Oxford

I would also like to express my thanks to the students of the B/TEC National Certificate in Engineering Course who took part in the evaluation of the CAL package by answering the questionnaire and making constructive comments.

DECLARATION

I declare that this Computer-Aided Learning package is entirely my own work and is not a copy or a modification of any existing software.

R.E.Ford January 1988.

ABSTRACT

This Computer-Aided Learning package for Mathematics has been written for the use of both teachers and students primarily in further education, although it can equally be used in the secondary education sector. The options I have chosen are topics taken from the mathematics objectives produced by the Business and Technician Education Council, B/TEC, who are responsible for validating many of the courses of a vocational nature offered in colleges of further education. These particular topics are taken from a bank of objectives considered to be relevant to students of engineering.

The educational theory that I have based my work on is that of Skinner and Crowder who pioneered the use of linear and branch programming for the purposes of improving the learning of people of all ages. I have attempted to create an environment in which the student is stimulated to interact with a computer in order to increase his/her awareness of a topic of mathematics. Also through this interaction the student will become computer literate and will lose any apprehension he may have in working with computers.

The computer is now being used in so many situations that soon the vast majority of people will need to be able to interact with them without any fear. Particularly in the various engineering fields, where computers are being used for design, research and development, and for the control of manufacturing processes the engineering student must become aware of their uses.

The Computer-Aided Learning package is being used more and more by the manufacturers of many production and processing systems, to teach the technicians and the operators of the future how to run the systems and also how to diagnose faults

when they arise. By using this package it is my intention that the technicians of the future will become familiar with CAL packages for what ever purpose they are written for.

This CAL package has been produced as an open ended exercise as I intend to continue to add to it as the need arises. The program has been written using RMBASIC incorporating procedures. It will be possible to write a procedure for each additional topic and simply add it on to the end of the existing program.

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SECTION ONE

The Aims of the program in their educational context.

The Business and Technician Education Council, B/TEC, have developed courses for students who wish to obtain vocationally orientated qualifications. The philosophy of B/TEC is to create varied learning situations such as formal classroom teaching, self motivated learning, work experience and so on. We in the Further Education service are being asked to direct our minds to the question of competency based learning. In the consultative document on competency based learning produced by the Further Education Unit in 1984 they made the point that the subjects of science and mathematics, which occupy a central place in the engineering curriculum, are important, but that they are tools of engineering rather than the essence. The measure of a good engineer is that he/she is competent in their performance of various tasks be they motor skills or mental/intellectual skills.

Many of the recent reports are showing that changes are needed in the engineering curricula to keep pace with the changes in the new technologies, which include the uses and applications of microprocessors and computers. It is generally accepted that the quality of education and training of engineers is a key factor upon which national prosperity depends. The Finniston report of 1980, "Engineering our Future" was a catalyst for proposals by the Engineering Council for the future accreditation of engineering courses. And recently the National Council for Vocational Qualifications has been formed to ensure that vocational qualifications not only have a

realistic theoretical content but also that the students receive realistic training in a work placement.

It is essential, because of the changes in technology, to continually consider the curriculum content and the way it is presented to the students. A quote from the report of the Further Education Unit, FEU, states that "the availability of computing facilities from the pocket calculator level upwards has profoundly influenced the further requirements of engineers for mathematical skills. I see these CAL programs that I have written as one of the means by which my students can learn and reinforce the topics of mathematics that are covered in the formal teaching situation, and will help them to not only improve their mathematical ability but also to become familiar with the use of computers.

The B/TEC courses that are offered in colleges today are not only for the school leaver, but are also for the older person who through the support of the Manpower Services Commission and employers are retraining for different occupations. The older person generally is more apprehensive than the younger person when it comes to using the new technologies. Also some B/TEC students are studying with the Open college and therefore are not able to obtain formal teaching, and must rely on other forms of learning such as the CAL package.

The new courses recently introduced by B/TEC contain a core curriculum which contain the following areas of study.

- (i) Communications
- (ii) Mathematics
- (iii) Engineering science
- (iv) Engineering systems
- (v) Information Technology and computing

- (vi) Engineering materials
- (vii) Tools, processes and equipment
- (viii) Industry, environment and society.

The intention is that all these various strands of engineering knowledge will be taught for part of the time as integrated studies, thereby making the student aware of the close relationship that exists between the various topics. This software is a means of combining the knowledge of computing and mathematics. It has been written for use by students studying mathematics for B/TEC Certificates and Diplomas in Mechanical, Production and Electronic Engineering. Students without appropriate G.C.E/G.C.S.E passes will embark on a course of study called the First Certificate, if they are studying part-time, and First Diploma if they are studying full-time. Students with the appropriate G.C.E/G.C.S.E passes will study for the National Certificate if they are part-time students, and the National Diploma if they are full-time students.

Mathematics is an essential subject in both First and National programmes of study. Level I work is comparable with G.C.S.E level whilst level II is comparable with Additional mathematics. At level III there are two units of mathematics comparable with Advanced level mathematics. For students who wish to continue their studies at either a University or a Polytechnic there is a double unit of mathematics at level III.

As I have already mentioned some students are studying through an Open learning situation. B/TEC suggest that learning materials may include texts, workbooks, study guides, assignment briefs, case studies, practical kits and COMPUTER SOFTWARE. The materials adopted for any particular purpose will depend upon the learning objectives. Computer software, I believe, though

very time consuming to produce, can be used both to introduce a new topic or to supplement topics already taught to the students.

Programmed instruction made its appearance in Britain in the early 60's. The innovators of programmed learning claimed that the presentation of organised lesson material to the individual student in a pre-arranged sequence, and at a pace determined by the students own responses, can help to overcome some of the deficiencies associated with the classroom teaching techniques. One of the problems is the lack of continuous feedback. One of the main aims of this educational software is to create the situation where there is continuous feedback to the student whilst he is working his way through the various tasks created by the software and the computer.

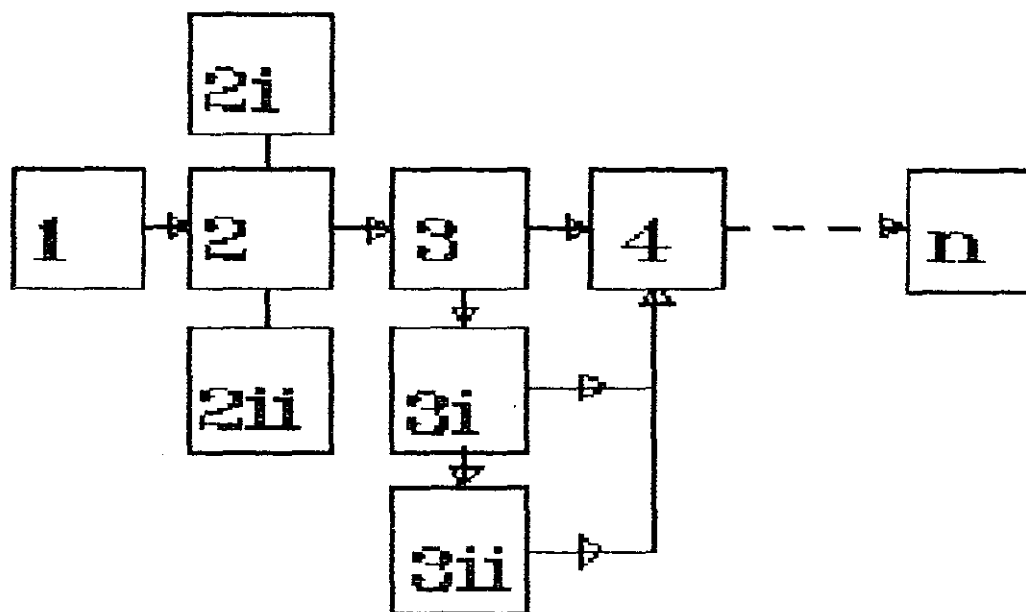
I have based the structure of the programs on the theories of B.F. Skinner and Crowder and their work on linear and branching programmes. It was in 1954 that B.F. Skinner published his article, "The science of learning and the art of teaching". Skinner's reinforcement learning theory was applied to the process of self instruction. His theory was that if a learners actions are followed by rewards they are likely to be repeated and learned. Unreinforced actions on the other hand will disappear from the learners repertoire. Skinner said that "behavioural patterns may, therefore, be shaped at the will of the instructor by use of a series of controlled stimuli".

Crowder who was both a psychologist and statistician suggested modifications to the process of self instruction as advocated by Skinner. Basically what he did was to introduce alternative sequences into programmes of learning. This is what I have attempted to do in this Computer Aided Learning package. The next instruction on the screen, when running the program, is

dependent upon the previous response. Skinner produced what is known as the Linear-type programme which in effect moved from one point to the next in the line without any opportunity to follow an alternative route if say the respondent made an incorrect response. Crowder on the other hand constructed his programme so that the learners responses could be utilised in the determination of the content and the actual presentation of the material.

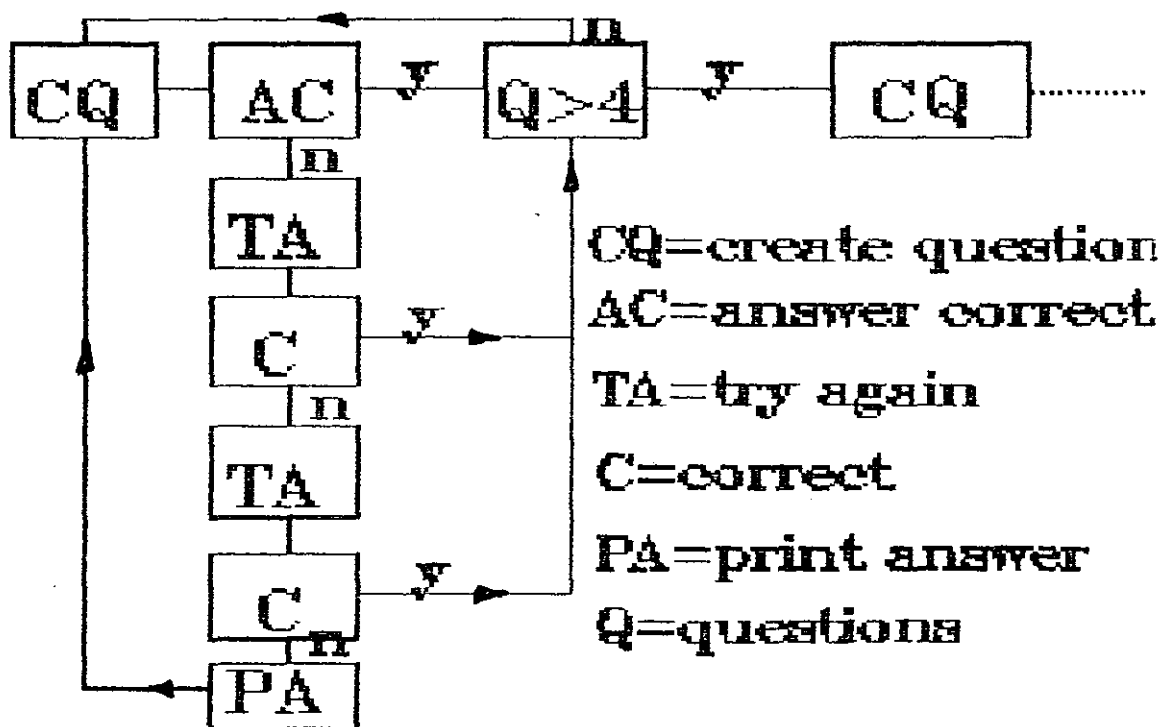
The advocates of programmed learning claim that if a subject can be taught then it can be programmed. According to this claim therefore there are no limits to the areas in which programmed learning can be put to use.

The early forms of programmed learning made use of either books or teaching machines. In the case of books the answer given by the respondent would determine which page to turn to. Similarly with the teaching machine the response would cause a certain frame to appear on the screen. In the design of my program I have created on the screen revision material followed by questions with randomly created parameters. The response from the computer will depend upon whether the students response is correct or not. If it is correct then the next question is created. If it is not correct then the student may have further attempts. If after three attempts the response is still incorrect then the correct method of solution is displayed on the screen and a hard-copy is produced on the printer for further consideration. In fact a hard-copy of all student and computer responses is created as the program is being executed within the computer.



Example of Branching.

Each response will cause a certain procedure to be executed.



SECTION TWO

How the Aims are achieved by the program.

The program is made up of a number of procedures and each procedure contains within it the facility to either create the graphical representation of diagrams or to create questions associated with the diagrams. The diagrams act as a source for refreshing the students awareness of the particular topic of mathematics which he has chosen from the menu presented on the screen. There are four main areas offered on the menu.

- (1) Trigonometry
- (2) Graphs
- (3) 3-Dim Trigonometry
- (4) Properties of the Circle

and in one case, Graphs, there is a sub-menu for selecting either problems associated with straight line graphs or quadratic graphs depending upon the group the teacher is working with.

The main aims of the program of learning as I see it is to offer to the student the topic in such a way that he will be able in the future to tackle similar problems with confidence. My intention is to present a topic by creating realistic questions for students of engineering, and to create questions which require looking at the problem in different ways depending upon the data available. As each question is created the student can then respond via the keyboard and his response is analysed by the computer. The correct response is acknowledged by the word "CORRECT" appearing on the screen, whereas an incorrect response is followed by the words "NO, that is not right, TRY AGAIN". This is incorporating the idea of rewarding the student with an encouraging response

if he is correct, or giving him the opportunity of determining the correct answer to the same question. All the time the answer is incorrect the student attempts the same question for a maximum of three tries. If after the third attempt it is still incorrect then a procedure takes over which shows the student, step by step how to obtain the correct answer. The computer then creates a new question of a similar type for the student to attempt. this procedure continues until the student has successfully answered four questions of a similar type, then a different procedure is called up to create further questions on that topic, but with different unknowns.

Also within the program is the facility for obtaining a printout of the students responses whether they are correct or not, and with full model answers if he was unable to input the correct answer after three attempts. This enables him to analyse his responses and this is also a help in reinforcing what he has learnt. When the student runs the program he is asked to input his name, this in turn is printed out so that if he is working on a network with other students all using the same software, he will be able to identify his own printout.

This group of procedures is creating a branching technique which puts up on the screen the appropriate response to the students' response. This is producing a close interaction between the student and the computer. The majority of students seem to respond favourably to this environment.

Many students of engineering will eventually be involved with using the computer as a means of control with CNC machines or engineering processes. Some will be involved with using the computer for design and research. Whatever their jobs are in the future one of the main aims of using CAL packages is to help students become aware of computing facilities.

This CAL package has been written using the RMBASIC high level programming language. A supplementary function of the package could be to use it to show students of computer programming how the language can be used to create graphics, diagrams and carryout numeric manipulation. The program listing can be analysed to see how the procedures are used to create the total package.

SECTION THREE

Review of similar software produced by a commercial company.

Over the years I have made use of a number of software packages written for the teaching of applied mathematics to engineering students at various levels of study. They have ranged from poor to first-class. Some have been written by "amateur" programmers, like me, but many have been written by the professional programmer employed by a software house. These are generally a much better package since they are produced in bulk and therefore a lot more time and money can be invested in them. Thereby creating a much more sophisticated program than the amateur can produce.

Many of these type of packages are produced as a collaborative scheme between a practising teacher and a professional programmer. This is the ideal situation for producing software, so that the teaching aims can be achieved by the use of the software. The design and production of software to achieve well defined aims is by no means an easy task, as I have discovered whilst being involved with this project.

One piece of software that I have used with mathematics and computer studies students is one that teaches the theory and uses of LOGIC gates and TRUTH tables. This collection of programs, produced by RJE software at £15 consists of,

(i) a program for teaching and testing the knowledge required for producing truth tables for 5 different logic gates. (a) AND gate (b) OR gate (c) NAND gate (d) NOR gate and (e) EXOR gate. Each gate is produced on the screen graphically and the truth table is built up step by step as the two inputs are changed from HIGH voltage (1) to LOW voltage (0) status. There is also the facility for applying inverters to each gate and again truth tables are created for each condition. The rules that

apply to each gate are displayed on the screen, and then gates are displayed and the student has to decide and input the expected output. If the answer is incorrect, the rule is again displayed and the student continues until he gets it right.

(ii) The second program enables students to build up a circuit of logic gates with upto 8 gates per circuit with 4 inputs and 4 outputs to LED's simulated on the screen. Each circuit can have inverters added to any gate and a timing diagram can also be displayed showing the status of each output from each gate and the output at each LED. Example circuits are supplied for use with the second program such as the Full-adder, RS flip-flop and D-type flip-flop switch.

(iii) The third program is a set of multi-choice questions suitable for any introductory computer studies course.

I use this set of programs with students attending the B/TEC National Diploma course in Computer Studies and I have evaluated them against the twelve (12) aspects recommended to the M.Sc in Computer Education group.

(1) Do you think that the program achieves the stated aims?

I consider that the program does in as much as it teaches the students the rules to be applied when selecting gates for a particular logic circuit. The students respond to this program with enthusiasm and it creates a certain amount of competition between two or more students using it.

(2) Does the program provide helpful messages to correct errors? Does it provide ways to help the students understand the program. Is it versatile so the student can control what it does?

The program of truth tables puts up on the screen the rules of logic if the student makes a mistake. It is not

versatile enough for the students to control the total output but the program of logic gates does allow students to design a circuit and control such things as output and the choice of having a timing diagram or not.

(3) Does it provide useful feedback to the user? Does it adapt to the students performance? Does it keep records of the students performance?

It does adapt to student performance but only in as much as it puts on the screen the rules to apply if the student makes a mistake. The feedback is in the form of rules of logic in program 1. In program 2, on logic circuits, once the student has embarked on the layout there is no chance of deleting a gate. The whole circuit has to be started again, which means reloading the program from the beginning. There is no record of the students performance, which is a weakness found in many software packages.

(4) Does the user have to make several different types of input or just key presses?

All the programs are executed by the pressing of just one appropriate key and will only operate if the correct key has been pressed. The changing from HIGH level to LOW level, ie from 1 to 0 is done by pressing either the X or Y keys.

(5) Is any use made of the students own language?

No. There is no opportunity to use standard english. The student is only required to respond by pressing just one key.

(6) What is the approximate time between student inputs?

This is under the control of the student. For the truth table program the inputs are on average every 20 to 30 seconds, but obviously it will depend on how confident the

student feels when answering the questions.

(7) Is the student asked significant or trivial questions?

I did not consider any of the questions in the programs to be trivial as they all seemed important if the student is going to learn the rules of logic.

(8) Using answers for 2 to 7 , do you think the programs encourage an interactive learning environment?

Yes, these programs particularly the first two encourage the student to respond to the questions by pressing the appropriate keys and as I have already said a competitive atmosphere develops as the students progress through the programs.

(9) Does the program/documentation allow the teacher to modify the program in any way?

Programs 2 and 3, that is the logic circuits and the multi-choice programs allow some variation particularly 3 which enables the teacher to put into the program a set of their own questions. Therefore as the course progresses the questions can be changed.

(10) Does the program use graphics. If so are they intrinsically important to the learning process?

Graphics are used and are essential for the first two programs. The programs have built into them facilities for producing on screen the logic gates and the circuits, and these are important to the learning process. The student can see at a glance the effect of any changes that are made to the logic circuit diagram. Without the graphics the programs, particularly the second one would be quite useless.

(11) Does the program use colour/animation, if so are they intrinsically important to the learning process?

Colour is extensively used for indicating the HIGH and LOW status levels. Red for HIGH and Green for LOW. these are very useful particularly in the logic gate program as the status of the inputs are indicated and in the logic circuit program the changes of colour can be slowed down so that the effect of changing the inputs can be seen moving around the circuit.

(12) Does the program use sound?

No. Sound is not used and is not really necessary for these applications.

Generally speaking these programs are professionally produced but the one thing that I have incorporated into my program which these do not have and I have not seen it in other programs, is the hardcopy produced on the printer as the program is run, so that students and the teacher can analyse the responses to the questions created.

SECTION FOUR

How the program is used in an educational situation.

I am making use of this software with a number of students who are attending either full-time or part-time B/TEC courses in Engineering. The software is being used on the network system under MS-DOS operating system. Each student can work independently and at his own speed. This is one of the educational advantages of using CAL packages for teaching purposes. The material can also be used as an assignment for the students. At the beginning of a teaching period I can ask them to work their way through the various options which I can choose, and then I can collect the output from the printer and then allocate a mark for their work. There is no way that they can alter the output from their individual workstations as each response is immediately sent to the spooler and saved ready for output to the printer when the appropriate keys are pressed.

TEACHERS' NOTES FOR USING THE SOFTWARE.

The package has been created for use with students studying for B/TEC mathematics at F and N level. It can also be used with students attending classes for GCSE mathematics. It is proposed that the package is used to supplement the formal classroom teacher centred learning with sessions of student centred learning at the computer. Each option has been written to occupy a student for approximately 20 minutes, which is considered to be the optimum time that a student will find a session at the computer stimulating.

By using this package you will find that teaching sessions will become more stimulating for both you and your students. As you know, the frequent change of activity helps to

improve the learning and many students enjoy the opportunity of working on a computer. Not only will it help with their learning of mathematics but will also help them to become computer literate.

There are four options for your students to choose from

(1) Trigonometry

(2) Graphs

(i) Straight-line graphs

(ii) Quadratic equation graphs

(3) 3-Dimensional trigonometry

(4) Properties of the circle

You can use them either as a means of supplanting your teaching of a new topic or they can be used as a means of revision either during a formal teaching session, or students can use them on their own. Comprehensive documentation is supplied with the package.

The facility of obtaining a print-out of all the students responses will enable you to analyse them with your students. You may also wish to use the output as a means of assessment. Once the student has chosen an option he must work through it from beginning to end. The students are not told of the facility for breaking out of the program. If you wish to do so it can be done by pressing the CTL/BREAK keys together.

I hope you find this CAL package a useful addition to your teaching facilities.

EVALUATION OF SOFTWARE.

The software was tested with a class of students who are studying for the B/TEC unit of Mathematics N level which is part of the National Certificate in Engineering. They are studying in the part-time mode. I decided to use this particular group of students as it contained a number of older people who are returning to studying after a break of several years.

Each student was presented with a copy of the documentation and a questionnaire and was asked to work their way through the options at their own pace. They filled in the questionnaire as they worked their way through the options. At the time of the pilot test the group had covered the work on Straight-line graphs and the graphical solution of Quadratic equations, and that week had begun the work on Trigonometry, which was really revision since they should have had basic knowledge of the subject from the previous year, but of course in the case of the older students they had some knowledge but it had been gained a number of years before and were a little "rusty". This was the situation that I had hoped for so that I could get some measure of how useful the software would be for people returning to formal studies.

As the students worked their way through the options I asked them to make comments either in the space provided or to me direct, so that I could take their comments and possibly modify the software in the light of what they said.

One comment that was made by several students was that there was no facility mentioned in the documentation for "breaking out" of the options if they had had enough of the option. I pointed out to them that it was my intention that they did not break-out of the option as this would mean that I

would not be able to get a full measure of their ability when I analysed the print-out with them. If it is necessary to break out of the program this can be done with the CTRL/BREAK keys but this is not made known to the students through the documentation.

Analysis of questionnaires.

Option 1 Trigonometry.

- | | |
|-------------|--|
| Question 1. | 100% had studied the topic before. |
| Question 2. | 80% said that it was at least a year ago since they had studied it.
20% said at least six months since they studied it. |
| Question 3. | 40% said they had found it easy at that time with 60% saying that they had not found it very easy. |
| Question 4. | 80% said they found the graphics quite helpful and 20% found them very helpful. |
| Question 5. | 80% found the documentation quite helpful and 20% found it very helpful. |
| Question 6. | 100% found the method of interaction with the computer easy, i.e. through the keyboard. |
| Question 7. | 100% liked the method of response to their answers. |
| Question 8. | 60% found the output to the printer quite helpful.
40% found it very helpful. |
| Question 9. | The overall reaction from the group was that they had found that working through the option had made the topic |

clearer to them.

The responses to the other options were very similar to the responses to option 1.

The overall reaction was favourable and the students said they enjoyed working through the options. Perhaps a measure of their interest was that they were prepared to continue the session beyond their normal finishing time. This was a twilight class running from 5.30 to 7.00. Most of them stayed on to finish the options for another 15 minutes which means there is enough in the package to keep someone busy for nearly two hours. Normally I would use the package by looking at one option only for about 30 minutes. This I think is long enough for a CAL session.

QUESTIONNAIRE

Pilot testing of software.

Course of Study:

Title of software:

Level of study:

Topic:

Tick where appropriate.

Section A

Question (1)

Have you studied this topic before. Yes/No

(If No go to section B)

Question (2)

How long ago was it.

last week/last month/six months/at least one year

Question (3)

Did you find it,

easy/not very easy/difficult/very difficult

Section B

Select the topic of your choice and work through the
programme answering questions at the appropriate time.

Question (4)

Do you find the graphics and/or diagrams

very helpful/quite helpful/not very helpful/not at all
helpful

Question (5)

Do you find the documentation
very helpful/quite helpful/not very helpful/not at all
helpful

Question (6)

Do you find the method of interaction between you and
the computer i.e via the keyboard
easy/not very easy/quite difficult/very difficult

Question (7)

Do you like the method of response to your answers
yes/no

Question (8)

Do you find the output to the printer
very helpful/quite helpful/not helpful in analysing
your overall response to the questions.

Question (9)

Do you feel that you understand the topic clearer now
that you have worked through the software.
It is no clearer/a little clearer/considerably clearer.

SECTION FIVE
DOCUMENTATION
B/TEC MATHEMATICS FOR ENGINEERING STUDENTS

Introduction.

The following programs have been produced to help you understand more fully the mathematics associated with various aspects of engineering. At the end of the topic you have been working through you are able to obtain a hardcopy of your answers and the responses from the computer. With this printout you can then analyse the results either on your own or with your teacher. I hope you find the programs both interesting and stimulating.

NOTE. This software will only run on RESEARCH MACHINES NIMBUS computers running under either MS-DOS or MS-NET operating system.

Instructions.

How to load the programs.

(a) On a standalone system.

- (i) Insert the disc into the disc drive.
- (ii) Type BASIC and press the ENTER key.
- (iii) Type LOADGO "PROJ" and press the ENTER key.

(b) On a Network system.

- (i) Type in your identity and password code.
- (ii) You should now see the :N> prompt.
- (iii) Type BASIC and press ENTER key.
- (iv) Type LOADGO "PROJ" and press the ENTER key.

You will now see the introduction screen, which after a few seconds will change to the screen which gives you some instructions and asks your to input your name. This is so that when your print out your answers on the printer your name will

be printed out at the top of the sheet for easy recognition. When you have input your name you will be presented with the MENU screen which will allow you choose one of 5 options.

- (1) Trigonometry.
- (2) Graphs.
- (3) 3-dimensional trigonometry.
- (4) Properties of the circle.
- (5) End the session.

Select the number of your choice. Each program has instructions on the screen to guide you to the next stage.

(1) Trigonometry. F Level

You will see before you a right-angled triangle and some of the trigonometrical functions associated with right-angled triangles, i.e. $\sin \theta$, $\cos \theta$, $\tan \theta$. Press the space bar to continue. The computer will now randomly generate values and you will be asked to calculate, using an electronic calculator the unknown value. You will be given upto three attempts at the question. If you are correct then the next question will be created. If you are not correct after three attempts then the correct answer will be put up on the screen, and another question created.

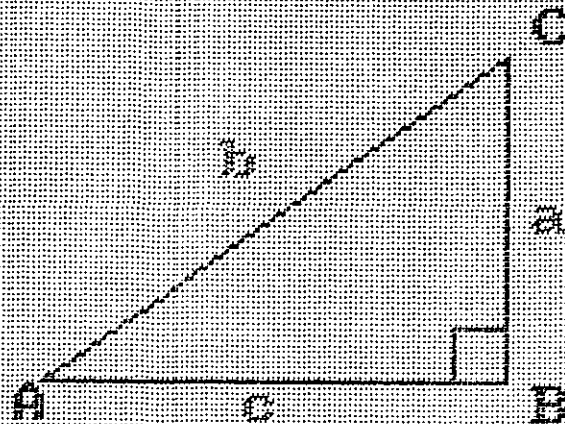
After you have successfully answered 4 questions of the same type then further questions will be created associated with different trigonometrical functions. On completion of the set of questions on trigonometry the HELLO screen will appear again. Input your name and then you can output your answers to the printer by pressing CTRL/ALT/PRTSC and continue with another program or bring the session to a close.

(2) Graphs. F Level & N Level.

On selecting the option GRAPHS, you will see that you

INTRODUCTION TO TRIGONOMETRY

THE RIGHT-ANGLED TRIANGLE



$$\begin{aligned}\text{SINE } A &= a/b \\ \text{COSINE } A &= c/b \\ \text{TANGENT } A &= a/c\end{aligned}$$

$$\begin{aligned}\text{SINE } C &= c/b \\ \text{COSINE } C &= a/b \\ \text{TANGENT } C &= c/a\end{aligned}$$

From the above it
can be seen that
 $\text{SIN } A = \text{COS } C$
 $\text{COS } A = \text{SIN } C$

$$A = 90 - C$$

Worked example

If $a = 34.5$ cm and
 $c = 23.6$ cm,
solve the triangle.

$$\begin{aligned}\text{TAN } A &= a/c \\ \text{TAN } A &= 34.5/23.6 \\ \text{TAN } A &= 1.462\end{aligned}$$

$$\text{ARCTAN } 1.462 = A$$

$$A = 55.63 \text{ degs}$$

$$C = 90 - 55.63$$

$$C = 34.37 \text{ degs}$$

$$\text{SIN } A = a/b$$

$$b = a/\text{SIN } A$$

$$b = 34.5/0.825$$

$$b = 41.80 \text{ cm}$$

can either work through questions on STRAIGHT-LINE graphs or QUADRATIC equation graphs. Make your choice.

(i) Straight-line graphs.

The computer will generate random integer values for both A and B, the GRADIENT and INTERCEPT respectively. You must decide from the graph the values of A and B and then input them via the keyboard. They can be either positive or negative values. If you are correct then the next line will be generated. If you are not correct then you must try again until you eventually get it right. There is no limit on the number of attempts you can make.

(ii) Quadratic equation graphs.

The computer will create X and Y axes and randomly generate values for A, B and C from which it will draw the curve. You must determine the roots of the equation by reading from the graph. Accuracy is to one decimal place. Five questions will be created for you to answer by reading from the screen direct. A further five questions will be created which you must answer by calculating the roots from the general equation for a Quadratic. You can then input your answer into the computer.

There is no facility in this program for a printout of your responses. At the end of the program the HELLO screen will appear again so that you can either select another program or end the session.

(3) 3-Dimensional Trigonometry. N Level.

This option produces a number of diagrams on the screen which you can look at for as long as you like. You are in control of the rate at which you move from one screen to another. The questions produced are,

(a) Associated with cylindrical prisms.

This is the situation found in the workshop when calculating the angle at which to set the compound vice on the milling machine to create a particular oblique area, and

(b) The measurement of external dovetails.

This gives practice in the mathematics associated with producing dovetails by using a milling machine. You are asked to input your answer to each question.

If correct the next question will appear. Otherwise you will be given three attempts at each question. If still incorrect, the correct answer will appear on the screen before another question is created for you to answer. After you have answered all the cylindrical prism questions then questions associated with external dovetails will be produced. At the end of the option press CTL/ALT/PRTSC keys to printout your responses to the questions so that you can analyse them at your leisure.

(4) Properties of the Circle. F Level.

This option produces a number of diagrams on the screen which you can look at for as long as you like. The control is through the keyboard. After you have looked at the diagrams you will be asked to answer a number of questions. You will be given upto three attempts at each question. If they are all incorrect then the correct answer will be given on the screen, and then another question will be created. Work to at least 2 decimal places of accuracy.

After the option is completed then you can output your results for analysis to the printer by pressing the CTL/ALT/PRTSC keys.

(5) End of the session.

This option will bring the session to a close and will automatically printout the results if they have not already been printed. This ensures that all your printouts are complete and nothing is left stored away in the SPOOLER if you have been working on the network system.

Examples of Hardcopy produced while running the program.

- (1) Trigonometry
- (3) 3-Dimensional Trigonometry
- (4) Properties of the circle

If $a = 81$ cm and $b = 101$ cm then
calculate angle A.

Input your answer for angle A 53.31
CORRECT

If $a = 45$ cm and $b = 58$ cm then
calculate angle C.

Input your answer for angle C 39.11
CORRECT

If $a = 40$ cm and $b = 60$ cm then
calculate angle C.

Input your answer for angle C 5
No! That is not right, try again

Input your answer for angle C 7
No! That is not right, try again

Input your answer for angle C 3
No! That is not right, try again

THIS IS THE CORRECT METHOD OF SOLUTION

ANGLE C = $\text{ArcCos}(a/b)$
 $\text{ArcCos}(40 / 60) = 48.18968$ degs

If $a = 72$ cm and $b = 92$ cm then
calculate angle C.

Input your answer for angle C 38.49
CORRECT

If $a = 97$ cm and $b = 117$ cm then
calculate angle C.

Input your answer for angle C 33.99
CORRECT

If $a = 74$ cm and $b = 87$ cm then
calculate angle C.

Input your answer for angle C 6
No! That is not right, try again

fred
3-Dim Trigonometry

EXAMPLE
=====

CYLINDRICAL PRISM

=====

OBLIQUE AREA = $\text{PI} \times \text{RAD}^2 / \text{COS A}$

IF THE RADIUS IS = 71 MM
AND THE ANGLE IS = 32 DEGS

THEN CALCULATE THE OBLIQUE AREA

INPUT YOUR ANSWER 3
No ! That Is NOT Right, Try Again
INPUT YOUR ANSWER 5
No ! That Is NOT Right, Try Again
INPUT YOUR ANSWER 7
No ! That Is NOT Right, Try Again

THIS IS THE CORRECT METHOD OF SOLUTION

$\text{AREA} = \text{RADIUS}^2 \times \text{PI} / \text{COS ANGLE}$

$71 * 71 * \text{PI} / \text{COS } 32 = 18674.37 \text{ MM}^2$

EXAMPLE
=====

CYLINDRICAL PRISM

=====

OBLIQUE AREA = $\text{PI} \times \text{RAD}^2 / \text{COS A}$

IF THE RADIUS IS = 13 MM
AND THE ANGLE IS = 37 DEGS

THEN CALCULATE THE OBLIQUE AREA

INPUT YOUR ANSWER 664.79

CORRECT

EXAMPLE
=====

CYLINDRICAL PRISM

=====

OBLIQUE AREA = $\text{PI} \times \text{RAD}^2 / \text{COS A}$

IF THE RADIUS IS = 58 MM
AND THE ANGLE IS = 0 DEGS

THEN CALCULATE THE OBLIQUE AREA

INPUT YOUR ANSWER 10568.32

CORRECT

EXAMPLE
 =====
 CYLINDRICAL PRISM
 =====

OBLIQUE AREA = $\text{PI} \times \text{RAD}^2 / \text{COS A}$

IF THE RADIUS IS = 96 MM
 AND THE ANGLE IS = 36 DEGS

THEN CALCULATE THE OBLIQUE AREA

INPUT YOUR ANSWER 4
 No ! That Is NOT Right, Try Again
 INPUT YOUR ANSWER 7
 No ! That Is NOT Right, Try Again
 INPUT YOUR ANSWER 3
 No ! That Is NOT Right, Try Again

THIS IS THE CORRECT METHOD OF SOLUTION

$\text{AREA} = \text{RADIUS}^2 \times \text{PI} / \text{COS ANGLE}$

$96 * 96 * \text{PI} / \text{COS } 36 = 35787.77 \text{ MM}^2$

EXAMPLE
 =====
 CYLINDRICAL PRISM
 =====

OBLIQUE AREA = $\text{PI} \times \text{RAD}^2 / \text{COS A}$

IF THE RADIUS IS = 12 MM
 AND THE ANGLE IS = 27 DEGS

THEN CALCULATE THE OBLIQUE AREA

INPUT YOUR ANSWER 507.72

CORRECT

EXAMPLE
 =====
 CYLINDRICAL PRISM
 =====

OBLIQUE AREA = $\text{PI} \times \text{RAD}^2 / \text{COS A}$

IF THE RADIUS IS = 35 MM
 AND THE ANGLE IS = 8 DEGS

THEN CALCULATE THE OBLIQUE AREA

If the radius $r = 32$ cm then calculate
the area of the circle shown above.

AREA = 4

No! You have made a mistake, try again

AREA = 5

No! You have made a mistake, try again

AREA = 7

No! You have made a mistake, try again

THIS IS THE CORRECT METHOD OF SOLUTION.

AREA = $\text{PI} \times \text{RADIUS} \times \text{RADIUS}$

AREA = 3216.991 CM2

If the radius $r = 34$ cm then calculate
the area of the circle shown above.

AREA = 3631.68

WELL DONE

If the radius $r = 12$ cm then calculate
the area of the circle shown above.

AREA = 452.38

WELL DONE

If the radius $r = 8$ cm then calculate
the area of the circle shown above.

AREA = 201.06

WELL DONE

If the radius $r = 3$ cm then calculate
the area of the circle shown above.

AREA = 28.27

WELL DONE

SECTION SIX

The program listing.

The program was written in the High Level language called BASIC and particularly in the dialect RMBASIC developed by Research Machines Ltd of Oxford. It is a language which is easily learned and the RMBASIC is much more structured than the original dialect of BASIC. This dialect contains a number of advanced facilities including procedures which makes the program more structured. The program can be built up of simple modules to create a comprehensive program.

It also contains facilities for colour and sound, a choice of a 40 column or 80 column mode for screen presentation, and graphics facilities for creating diagrams and graphs. Text can also be created in either graphics or normal print mode thereby giving variations in text style and presentation. Global variables can be used within programs so that a variable can be used in a number of procedures. Also arrays of text and numbers can be handled and sub-routines and functions can be incorporated into procedures.

Graphics and text areas can be specified and upto 9 different areas can be written to in any one program. This makes for a more professional presentation on the screen. I found it a very user-friendly language to work with and it was quite adequate for this project. The program requires 60KBytes of memory.

Explanation of Program Listing.

Lines 10 - 300 These create the initial logo on the screen.

Line 310 Clears the graphics from memory.

Lines 320 - 470 These create the "HELLO" screen and waits for the inputting of the students name.

Line 480 Receives name.

Lines 490 - 670 Creates "MENU" screen.

Lines 690 - 740 Options are selected and according to which option is chosen appropriate procedures are executed.

Lines 750 - 820 These lines are executed if option 5, "end the session" has been chosen.

Lines (830 - 4270) Procedure named TRIG. This procedure starts by giving instructions for answering the

830 - 1020 questions created further on in the procedure.

1030 - 1300 This block of coding creates drawing 1.(see screen printouts in documentation section.)

1310 - 1650 This block of coding creates drawing 2.

1660 - 1950 This block of coding creates drawing 3.

1960 - 2120 This creates the rectangular prism.

2130 Start of the first calculations.

2390 Awaits answer.

2400 Prints out answer to printer.

2410 Calculates true value.

2420 Compares values.

2470 Keeps the total number of attempts at question.

2510 Keeps a count of the number of questions created of a given type.

2540 - 2610 Sub-routine to print correct answer on the screen.

2620 - 3060 Creates different type of question associated

with oblique areas.

3070 - 3460 Creates third type of question involved with oblique areas.

3470 - 3820 Creates drawing of external dovetail on the screen.

3830 - 4270 Creates questions and if necessary the sub-routine is executed in order to give the correct answer.

Lines (4280 - 5160) Procedure for GRAPHS option.

4320 - 4360 Creates introduction panel to GRAPHS option.

4370 - 4440 GRAPHS menu screen.

4470 Choose GRAPHS options from menu.

4480 Choice of procedures to draw axes for graphs.

4500 Executes AXES procedure.

4510 - 5150 Creates questions of GRADIENT and INTERCEPT.

Lines 5170 - 5450 AXES procedure defined.

5470 Executes AXES2 procedure for Quadratic equation option.

5480 Executes TEXT procedure. 2

5490 - 5660 Creates values of A,B and C for $AX^2 + BX + C$

5670 - 5890 Creates further questions about quadratic equations.

Lines (5900 - 7030) Main procedure for creating diagrams for Properties of a Circle option.

5940 - 6000 Introduction screen.

6010 - 6270 Creates first diagram.

6280 - 6500 Creates second diagram.

6510 - 6740 Creates third diagram.

6750 - 6970 Creates fourth diagram.

6980 - 7020 Executes procedures named ROUND1 to ROUND5.

Each procedure creates questions and prints the

correct answer if necessary by calling up
a sub-routine.

Lines 7040 - 7470 Procedure named ROUND1 defined.

7480 - 7910	ROUND2	..
7920 - 8430	ROUND3	..
8440 - 8940	ROUND4	..
8950 - 9410	ROUND5	..

Each procedure has a built-in sub-routine
for printing on the screen and the printer
the correct answer if necessary.

9420 - 9730 Procedure AXES2 defined.

9740 - 9790 Procedure TEXT defined.

9800 - 9840 Procedure TEXT1 defined. Used for variation
in Quadratic equation questions.

Lines (9850 - 10380) Procedure TRIG1 defined. This creates
the diagrams and trigonometrical functions
associated with a right-angled triangle.

10320 - 10380 Executes in turn the procedures, ALPHA, BETA,
GAMMA, ALPHA1, EPSILON and PHI. Each procedure
creates questions and puts up on the screen
the responses of the student and also prints
out the correct answer if required.

10390 - 10830 Procedure ALPHA defined.

10840 - 11270	..	BETA	..
11280 - 11710	..	GAMMA	..
11720 - 12150	..	ALPHA1	..
12160 - 12590	..	EPSILON	..
12600 - 13040	..	PHI	..

The student is required to answer the questions
created by using an electronic calculator. The
combined use of calculator and computer is

required throughout the question and answer session for most of the options chosen. Each procedure has built-in subroutines to printout the correct answers before moving on to the next question.

13050 - 13120 Procedure TRIANGLE defined. This creates a right-angled triangle at the top of the screen for students to refer to when answering questions.

```
10 REM *M.SC PROJECT COMP ED*

20 CLS : HOME

30 SET MODE 40

40 GLOBAL Fred$

50 REM * CREATE LOGO *

60 SET PAPER 1 : SET BORDER 1 : CLS

70 FOR I := 1 TO 100 STEP 10

80   SET BRUSH 1 / 10

90   AREA 5 + I, 200 - I; 105 + I, 200 - I; 105 + I, 100 - I; 5 + I, 100 - I; 5 + I, 200 - I

100 NEXT I

110 SET BRUSH 0

120 CIRCLE 20, 145, 60

130 SET BRUSH 15 : CIRCLE 17, 145, 60

140 SET BRUSH 8 : CIRCLE 15, 145, 60

150 SET BRUSH 1 : AREA 190, 80; 190, 85; 196, 85; 196, 80

160 SET BRUSH 0 : CIRCLE 2, 145, 32; 145, 15; 170, 60; : AREA 143, 32; 147, 32; 147, 15; 143, 15

170 SET BRUSH 15 : AREA 105, 105; 145, 105; 145, 85; 105, 85

180 SET BRUSH 2 : PLOT "CAMET", 106, 90

190 SET BRUSH 15 : PLOT "LOUGHBOROUGH UNIVERSITY OF TECHNOLOGY", 10, 240

200 PLOT "M.Sc. COMPUTER EDUCATION", 60, 230

210 PLOT "(C) R.E.FORD", 100, 220

220 PLOT "CENTRE FOR ADVANCEMENT OF MATHEMATICAL", 10, 210

230 PLOT "EDUCATION IN TECHNOLOGY", 60, 200

240 SET BRUSH 4 : PLOT "B/TEC MATHEMATICS", 160, 180

250 PLOT "F & N LEVEL ", 200, 170

260 PLOT "FOR ENGINEERING", 180, 160

270 PLOT "STUDENTS", 220, 150

280 SET BRUSH 5 : PLOT "A COMPUTER-AIDED", 180, 130

290 PLOT "LEARNING PACKAGE", 180, 120
```

```
300 FOR I := 1 TO 5000 : NEXT I

310 CLG

320 SET MODE 80

330 SET PAPER 3 : SET BORDER 1 : SET PEN 0 : CLS

340 SET BRUSH 2 : AREA 5, 5; 5, 244; 634, 244; 634, 5 STYLE 3

350 AREA 7, 7; 7, 242; 632, 242; 632, 7 STYLE 3

360 PLOT "Hello,", 20, 220 SIZE 2

370 PLOT "welcome to a mathematics revision session.You will be asked to select", 50, 210

380 PLOT "the topic of mathematics that you would like to revise,and as you work your", 15, 200

390 PLOT "way through the exercises an output to the printer will be created. If you", 15, 190

400 PLOT "are working on a NIMBUS NETWORK system then at the end of your session press", 15, 180

410 SET BRUSH 1 : PLOT "ctrl/alt/prtsc", 15, 170 : SET BRUSH 2

420 PLOT "keys simultaneously so that you can obtain your own individual", 130, 170

430 PLOT "printout with your name on it for easy recognition.Please tell me your name", 15, 160

440 PLOT "and I hope you find the revision session stimulating.Go for it!", 15, 150

450 SET WRITING 1 TO 5, 11; 75, 22

460 SET BRUSH 1 : PLOT "What is your name", 80, 47 SIZE 2

470 SET WRITING 1 : SET CURPOS 50, 20

480 SET WRITING 1 : INPUT Fred$

490 SET MODE 40

500 SET PAPER 1 : CLS : SET BORDER 8

510 AREA 5, 5; 5, 235; 315, 235; 315, 5

520 SET BRUSH 8 : AREA 6, 6; 6, 234; 314, 234; 314, 6

530 FOR I := 2 TO 200 STEP 40

540 SET BRUSH 15 : AREA 11, 9 + I; 11, 19 + I; 31, 19 + I; 31, 9 + I

550 SET BRUSH 4 : AREA 10, 10 + I; 10, 20 + I; 30, 20 + I; 30, 10 + I

560 NEXT I

570 PLOT "MENU", 145, 220

580 PLOT "ENGINEERING MATHEMATICS", 70, 210
```

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590 SET BRUSH 14 : PLOT "1  TRIGONOMETRY", 18, 172 : PLOT "F  LEVEL", 200, 172
600 PLOT "2  GRAPHS", 18, 132 : PLOT "F&N  LEVEL", 200, 132
610 PLOT "3  3 DIMENSIONAL", 18, 92 : PLOT "F&N  LEVEL", 200, 92
620 PLOT "TRIGONOMETRY", 50, 82
630 PLOT "4  PROPERTIES OF", 18, 52 : PLOT "F  LEVEL", 200, 52
640 PLOT "THE CIRCLE", 50, 42
650 PLOT "5  END SESSION", 18, 12
660 SET BRUSH 2 : PLOT "SELECT THE NUMBER", 170, 30
670 PLOT "OF YOUR CHOICE", 185, 20
680 SET CURSOR 0
690 Answer$ := GET$( )
700 IF Answer$ = "1" THEN Trig1 : CLG : GOTO 310
710 IF Answer$ = "2" THEN Graph : CLG : SET MODE 40 : GOTO 310
720 IF Answer$ = "3" THEN Trig : CLG : GOTO 310
730 IF Answer$ = "4" THEN Round : CLG : GOTO 310
740 IF Answer$ = "5" THEN CLS : SET BRUSH 15 : PLOT "END OF SESSION", 105, 150
750 PRINT #2 ! ! !, TAB (10) "END OF SESSION"
760 PLOT "DO NOT FORGET YOUR PRINTOUT", 50, 140
770 PLOT "I hope you have found the session useful", 1, 130
780 SET BRUSH 14 : PLOT "GOODBYE", 100, 100 SIZE 2
790 FOR I := 1 TO 5000 : NEXT I
800 PRINT #2 ! ! ! !, "GOODBYE", Fred$
810 REM BYE
820 IF Answer$ > "5" OR Answer$ < "1" THEN 570
830 PROCEDURE Trig
840   GLOBAL Fred$
850   PRINT #2, Fred$
860   PRINT #2, "3-Dim Trigonometry"
870   CLG : SET BRUSH 0 : AREA 35, 95; 25, 105; 25, 185; 35, 195; 295, 195; 305, 185; 305, 105; 295, 95

```

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880  SET BRUSH 15 : AREA 30, 100; 20, 110; 20, 190; 30, 200; 290, 200; 300, 190; 300, 110; 290, 100
890  SET BRUSH 11 : PLOT "3-DIMENSIONAL", 55, 170 SIZE 2
900  PLOT "TRIGONOMETRY", 60, 150 SIZE 2
910  SET BRUSH 6 : PLOT "F & N LEVEL", 70, 110 SIZE 2
920  FOR I := 1 TO 2000 : NEXT I
930  CLG : SET BRUSH 4 : AREA 0, 249; 319, 249; 319, 176; 0, 176
940  SET BRUSH 1 : AREA 5, 245; 314, 245; 314, 180; 5, 180
950  SET BRUSH 15 : PLOT "This set of exercises is to help you", 7, 235
960  PLOT " understand some applications of", 7, 225
970  PLOT "ENGINEERING TRIGONOMETRY.The computer", 7, 215
980  PLOT "will create questions for you to ", 7, 205
990  PLOT "answer.You will need a CALCULATOR.", 7, 195
1000 PLOT "The diagrams are for revision purposes.", 7, 185
1010 SET CURSOR 0 : SET CURPOS 10, 20 : PRINT "PRESS ANY KEY TO CONTINUE"
1020 Answer$ := GET$( ) : CLG
1030 REM * DRAW FIGURE 1 *
1040 SET BRUSH 10
1050 AREA 20, 50; 150, 150; 300, 150; 170, 50
1060 SET BRUSH 2
1070 LINE 70, 70; 170, 245
1080 SET BRUSH 15 : LINE 170, 240; 170, 100; 70, 70 STYLE 3
1090 PLOT "O", 85, 80
1100 PLOT "A", 175, 235
1110 PLOT "B", 175, 100
1120 PLOT "C", 60, 60
1130 LINE 150, 95; 150, 120; 170, 126
1140 PLOT "D", 140, 150
1150 PLOT "E", 305, 150
1160 PLOT "F", 175, 40

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```
1170  PLOT "G", 10, 40
1180  PLOT "POINT A IS ", 185, 225
1190  PLOT "PROJECTED DOWN", 185, 215
1200  PLOT "TO POINT B ON", 185, 205
1210  PLOT "PLANE DEFG", 185, 195
1220  SET BRUSH 2 : PLOT "PLANE DEFG", 185, 125
1230  AREA 5, 240; 140, 240; 140, 200; 5, 200
1240  SET BRUSH 15
1250  PLOT "THE ANGLE BETWEEN", 5, 225
1260  PLOT "LINE AC AND PLANE", 5, 215
1270  PLOT "DEFG IS 0", 35, 205
1280  SET CURPOS 10, 23 : PRINT "PRESS ANY KEY TO CONTINUE"
1290  Answer$ := GET$(1)
1300  CLS
1310  REM * DRAW FIGURE 2 *
1320  SET BRUSH 8
1330  AREA 50, 50; 50, 125; 200, 200; 200, 125
1340  SET BRUSH 7
1350  AREA 50, 50; 50, 125; 200, 90; 200, 15
1360  SET BRUSH 2
1370  LINE 200, 163; 50, 87; 200, 53 STYLE 5
1380  PLOT "A", 205, 90
1390  PLOT "B", 205, 5
1400  PLOT "C", 40, 45
1410  PLOT "D", 40, 125
1420  PLOT "E", 205, 200
1430  PLOT "F", 205, 115
1440  SET BRUSH 14
1450  PLOT "I", 40, 85
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1460 PLOT "H", 205, 158
1470 PLOT "J", 205, 48
1480 PLOT "O", 65, 83
1490 AREA 5, 240; 150, 240; 150, 210; 5, 210
1500 SET BRUSH 2
1510 PLOT "THE ANGLE BETWEEN", 10, 230
1520 PLOT "TWO INTERSECTING", 10, 220
1530 PLOT "      PLANES", 10, 210
1540 SET BRUSH 3
1550 PLOT "PLANE ABCD", 120, 40
1560 PLOT "PLANE CDEF", 120, 150
1570 AREA 220, 220; 319, 220; 319, 150; 220, 150
1580 SET BRUSH 14
1590 PLOT "THE ANGLE", 225, 205
1600 PLOT "BETWEEN THE", 225, 195
1610 PLOT "TWO PLANES", 225, 185
1620 PLOT "IS ANGLE HIJ", 225, 175
1630 PLOT "SHOWN AS O", 225, 165
1640 SET CURPOS 28, 21 : PRINT "PRESS ANY KEY" : SET CURPOS 28, 22 : PRINT " TO CONTINUE"
1650 Answer$ := GET$(1) : CLG
1660 REM THIRD FIGURE
1670 AREA 5, 230; 100, 230; 100, 180; 5, 180
1680 SET BRUSH 6
1690 PLOT "LENGTHS AND", 9, 220
1700 PLOT "AREAS ON AN", 9, 207 : PLOT "INCLINED", 20, 194 : PLOT "PLANE", 30, 181
1710 SET BRUSH 2 : AREA 220, 220; 310, 220; 310, 120; 220, 120
1720 SET BRUSH 7 : PLOT "DE", 289, 200 : PLOT "COS O = --", 225, 190 : PLOT "DC", 289, 180
1730 PLOT "ABCD=----", 225, 150 : PLOT "AFED", 265, 160; : PLOT "COS O", 265, 140
1740 SET BRUSH 3 : AREA 50, 100; 150, 200; 200, 150; 100, 50; 50, 100

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```

1750 SET BRUSH 4

1760 AREA 100, 50; 200, 150; 200, 100

1770 SET BRUSH 7

1780 LINE 50, 100; 150, 150; 150, 200 STYLE 3

1790 LINE 150, 150; 200, 100 STYLE 3

1800 PLOT "A", 40, 90

1810 PLOT "B", 150, 205

1820 PLOT "C", 205, 150

1830 PLOT "D", 97, 35

1840 PLOT "E", 200, 85

1850 PLOT "F", 156, 150

1860 PLOT "O", 130, 70

1870 SET BRUSH 4

1880 AREA 150, 10; 300, 60; 300, 10

1890 SET BRUSH 7

1900 PLOT "D", 140, 5

1910 PLOT "C", 302, 62

1920 PLOT "E", 305, 5

1930 PLOT "O", 180, 8

1940 SET CURPOS 2, 23 : PRINT "PRESS ANY KEY" : SET CURPOS 2, 24 : PRINT " TO CONTINUE "

1950 Answer$ := GET$( ) : CLG

1960 REM INSTRUCTIONS FOR CALCULATIONS

1970 SET PAPER 1 : SET BRUSH 9 : CLS : AREA 5, 245; 314, 245; 314, 170; 5, 170

1980 SET BRUSH 15 : PLOT "THE OBLIQUE AREA OF A PRISM", 45, 230

1990 PLOT "OBLIQUE AREA = -----", 20, 190 : SET BRUSH 2 : PLOT "CROSS-SECTIONAL AREA", 150, 20

2000 PLOT "COS 0", 200, 180

2010 SET BRUSH 14 : AREA 5, 165; 314, 165; 314, 5; 5, 5

2020 SET BRUSH 0 : LINE 10, 150; 260, 150; 260, 100; 10, 100; 10, 150

2030 SET BRUSH 2 : AREA 260, 150; 285, 130; 285, 80; 260, 100

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2040 SET BRUSH 0 : LINE 285, 80; 35, 80; 10, 100 : LINE 100, 100; 100, 150
2050 LINE 260, 130; 35, 130; 10, 150 STYLE 3 : LINE 35, 130; 35, 80 STYLE 3
2060 SET BRUSH 2 : AREA 100, 100; 150, 150; 175, 130; 125, 80
2070 PLOT "0", 103, 110
2080 SET BRUSH 0 : LINE 125, 90; 125, 60 : LINE 270, 95; 270, 60
2090 PLOT "OBLIQUE AREA.", 70, 45
2100 PLOT "CROSS-SECT AREA.", 190, 45
2110 SET CURPOS 2, 23 : PRINT "PRESS ANY KEY TO CONTINUE"
2120 Answer$ := GET$( ) : CLG
2130 REM START FIRST SET OF CALCULATIONS
2140 Total := 0 : Count := 0
2150 Radius := INT(RND(1) * 90) + 10
2160 Angle := INT(RND(1) * 45)
2170 CLS : HOME
2180 SET PAPER 14 : SET RAD TRUE
2190 CLS
2200 SET PEN 2
2210 PRINT TAB (15) "EXAMPLE"
2220 PRINT &2, ! ! TAB (15) "EXAMPLE"
2230 PRINT TAB (15) "====="
2240 PRINT &2, TAB (15) "====="
2250 PRINT TAB (11) "CYLINDRICAL PRISM"
2260 PRINT &2, TAB (11) "CYLINDRICAL PRISM"
2270 PRINT TAB (11) "====="
2280 PRINT &2, TAB (11) "====="
2290 PRINT ! TAB (5) "OBLIQUE AREA =  $\pi \times \text{RAD} \times \text{RAD} / \cos A$ "
2300 PRINT &2, ! TAB (5) "OBLIQUE AREA =  $\pi \times \text{RAD} \times \text{RAD} / \cos A$ "
2310 PRINT ! TAB (5) "IF THE RADIUS IS = "; Radius; "MM"
2320 PRINT &2, ! TAB (5) "IF THE RADIUS IS = "; Radius; "MM"

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2330 PRINT TAB (5) "AND THE ANGLE IS = "; Angle; "DEGS"
2340 PRINT h2, TAB (5) "AND THE ANGLE IS = "; Angle; "DEGS"
2350 PRINT ! TAB (3) "THEN CALCULATE THE OBLIQUE AREA"
2360 PRINT h2, ! TAB (3) "THEN CALCULATE THE OBLIQUE AREA"
2370 PRINT ! ! !
2380 PRINT h2, ! ! !
2390 PRINT TAB (5) "INPUT YOUR ANSWER "; : INPUT Oblique Area
2400 PRINT h2, TAB (5) "INPUT YOUR ANSWER "; : PRINT h2, Oblique Area,
2410 True Area := PI * Rad * Rad / COS(Angle * PI / 180)
2420 IF ABS(True Area - Oblique Area) < 1e-02 THEN SET BRUSH 1 : PLOT "CORRECT", 80, 10 SIZE 3 ELSE 2450
2430 IF ABS(True Area - Oblique Area) < 1e-02 THEN PRINT h2, "CORRECT"
2440 FOR I := 1 TO 2000 : NEXT I : IF ABS(True Area - Oblique Area) < 1e-02 THEN 2510
2450 PRINT TAB (2) " No ! That Is NOT Right, Try Again "
2460 PRINT h2, TAB (2) " No ! That Is NOT Right, Try Again "
2470 Total := Total + 1
2480 IF Total < 3 THEN 2390
2490 GOSUB 2540
2500 GOTO 2130
2510 Count := Count + 1
2520 IF Count < 4 THEN 2150
2530 GOTO 2620
2540 PRINT ! ! TAB (1) "THIS IS THE CORRECT METHOD OF SOLUTION"
2550 PRINT h2, ! ! TAB (1) "THIS IS THE CORRECT METHOD OF SOLUTION"
2560 PRINT ! TAB (7) "AREA=RAD*RAD*PI/COS ANGLE"
2570 PRINT h2, ! TAB (7) "AREA=RAD*RAD*PI/COS ANGLE"
2580 PRINT ! TAB (2) Radius; "*"; Radius; "* PI/COS"; Angle; "="; True Area; "MM2"
2590 PRINT h2, ! TAB (2) Radius; "*"; Radius; "* PI/COS"; Angle; "="; True Area; "MM2"
2600 FOR I := 1 TO 5000 : NEXT I
2610 RETURN

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```

2620  Total := 0 : Count := 0 : REM START SECOND CALCULATIONS.
2630  Radius := INT(RND(10) + 8)
2640  Oblique Area := INT(RND(100) + 1100)
2650  CLS : HOME
2660  PRINT TAB (15); "EXAMPLE"
2670  PRINT #2, ! ! TAB (15); "EXAMPLE"
2680  PRINT TAB (15) "====="
2690  PRINT #2, TAB (15) "====="
2700  PRINT TAB (11) "CYLINDRICAL PRISM"
2710  PRINT #2, TAB (11) "CYLINDRICAL PRISM"
2720  PRINT TAB (11) "====="
2730  PRINT #2, TAB (11) "====="
2740  PRINT TAB (5) "ANGLE A=ARCCOS(R*R*PI/OBLIQUE AREA)"
2750  PRINT #2, TAB (5) "ANGLE A=ARCCOS(R*R*PI/OBLIQUE AREA)"
2760  PRINT ! TAB (7) "IF THE RADIUS IS = "; Radius; "MM"
2770  PRINT #2, ! TAB (7) "IF THE RADIUS IS = "; Radius; "MM"
2780  PRINT ! TAB (7) "AND THE OBLIQUE AREA="; Oblique Area; "MM2"
2790  PRINT #2, ! TAB (7) "AND THE OBLIQUE AREA="; Oblique Area; "MM2"
2800  PRINT ! TAB (5) "CALCULATE THE OBLIQUE ANGLE"
2810  PRINT #2, ! TAB (5) "CALCULATE THE OBLIQUE ANGLE"
2820  PRINT ! TAB (10) "INPUT YOUR ANSWER"; : INPUT A
2830  PRINT #2, ! TAB (10) "INPUT YOUR ANSWER"; : PRINT #2, A,
2840  Y := PI * Radius * Radius / Oblique Area
2850  Oba := (- ATN(Y / SQRT(- Y * Y + 1)) + PI / 2) * 180 / PI
2860  IF ABS(Oba - A) < 1e-02 THEN SET BRUSH 1 : PLOT "CORRECT", 80, 10 SIZE 3 ELSE 2900
2870  IF ABS(Oba - A) < 1e-02 THEN PRINT #2, "CORRECT"
2880  FOR I := 1 TO 2000 : NEXT I
2890  IF ABS(Oba - A) < 1e-02 THEN 2960
2900  PRINT TAB (5) "NO!That is not right,try again"

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2910 PRINT k2, TAB (5) "NO!That is not right,try again"
2920 Total := Total + 1
2930 IF Total < 3 THEN 2820
2940 GOSUB 2990
2950 GOTO 2620
2960 Count := Count + 1
2970 IF Count < 4 THEN 2630
2980 GOTO 3070
2990 PRINT ! ! TAB (1) "THIS IS THE CORRECT METHOD OF SOLUTION"
3000 PRINT k2, ! ! TAB (1) "THIS IS THE CORRECT METHOD OF SOLUTION"
3010 PRINT ! "ARCCOS(R*R*PI/OBLIQUE AREA)=ANGLE A"
3020 PRINT k2, ! "ARCCOS(R*R*PI/OBLIQUE AREA)=ANGLE A"
3030 PRINT ! "ARCCOS("; Radius; "*"; Radius; "*PI/"; Oblique Area; ")="; Oba; "DEG"
3040 PRINT k2, ! "ARCCOS("; Radius; "*"; Radius; "*PI/"; Oblique Area; ")="; Oba; "DEG"
3050 FOR I := 1 TO 5000 : NEXT I
3060 RETURN
3070 Total := 0 : Count := 0 : REM START THIRD CALCULATIONS.
3080 Angle := INT(RND(45))
3090 Oblique Area := INT(RND(100) + 1100)
3100 CLS : HOME
3110 PRINT TAB (15) "EXAMPLE"
3120 PRINT k2, ! ! TAB (15) "EXAMPLE"
3130 PRINT TAB (15) "====="
3140 PRINT k2, TAB (15) "====="
3150 PRINT ! TAB (4) "RADIUS=SQR(OBLIQUE AREA*COS A/PI)"
3160 PRINT k2, ! TAB (4) "RADIUS=SQR(OBLIQUE AREA*COS A/PI)"
3170 PRINT ! TAB (5) "IF THE OBLIQUE ANGLE="; Angle; "DEG"
3180 PRINT k2, ! TAB (5) "IF THE OBLIQUE ANGLE="; Angle; "DEG"
3190 PRINT ! TAB (5) "AND THE OBLIQUE AREA="; Oblique Area; "MM2"

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3200 PRINT A2, ! TAB (5) "AND THE OBLIQUE AREA="; Oblique Area; "MM2"
3210 PRINT ! TAB (5) "THEN CALCULATE THE RADIUS"
3220 PRINT A2, ! TAB (5) "THEN CALCULATE THE RADIUS"
3230 PRINT ! ! TAB (10) "INPUT YOUR ANSWER"; : INPUT Radius
3240 PRINT A2, ! ! TAB (10) "INPUT YOUR ANSWER"; : PRINT A2, Radius,
3250 R0 := SQRT(Oblique Area * COS(Angle * PI / 180) / PI)
3260 IF ABS(R0 - Radius) < 1e-02 THEN SET BRUSH 1 : PLOT "CORRECT", 80, 10 SIZE 3 ELSE 3300
3270 IF ABS(R0 - Radius) < 1e-02 THEN PRINT A2, "CORRECT"
3280 FOR I := 1 TO 2000 : NEXT I
3290 IF ABS(R0 - Radius) < 1e-02 THEN 3360
3300 PRINT TAB (5) "NO!That is not right,try again"
3310 PRINT A2, TAB (5) "NO!That is not right,try again"
3320 Total := Total + 1
3330 IF Total < 3 THEN 3230
3340 GOSUB 3390
3350 GOTO 3070
3360 Count := Count + 1
3370 IF Count < 4 THEN 3080
3380 GOTO 3470
3390 PRINT ! ! TAB (1) "THIS IS THE CORRECT METHOD OF SOLUTION"
3400 PRINT A2, ! ! TAB (1) "THIS IS THE CORRECT METHOD OF SOLUTION"
3410 PRINT TAB (2) "RADIUS=SQR(OBLIQUE AREA*COS A/PI)"
3420 PRINT A2, TAB (2) "RADIUS=SQR(OBLIQUE AREA*COS A/PI)"
3430 PRINT "SQR("; Oblique Area; "*COS "; Angle; "/PI)="; R0
3440 PRINT A2, "SQR("; Oblique Area; "*COS "; Angle; "/PI)="; R0
3450 FOR I := 1 TO 5000 : NEXT I
3460 RETURN
3470 REM MEASUREMENT OF EXT DOVETAIL
3480 REM DRAW DIAGRAM OF DOVE TAIL
3490 SET BORDER 10 : SET PAPER 10 : CLS

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3500 SET BRUSH 15 : AREA 5, 245; 314, 245; 314, 220; 5, 220
 3510 SET BRUSH 2 : PLOT "MEASUREMENT OF EXTERNAL DOVETAIL", 30, 232
 3520 PLOT "BY THE USE OF PRECISION ROLLERS.", 30, 222
 3530 AREA 50, 85; 50, 110; 130, 110; 90, 160; 210, 160; 170, 110; 250, 110; 250, 85; 50, 85
 3540 SET BRUSH 8 : FLOOD 140, 125
 3550 SET BRUSH 7 : CIRCLE 20, 88, 130; 212, 130
 3560 SET BRUSH 0 : LINE 68, 137; 68, 185 : LINE 232, 137; 232, 185
 3570 LINE 68, 180; 232, 180
 3580 AREA 68, 180; 74, 182; 74, 178 : AREA 232, 180; 226, 182; 226, 178
 3590 PLOT "M", 147, 182 : LINE 88, 130; 130, 110; 88, 110; 88, 130
 3600 LINE 212, 130; 170, 110; 212, 110; 212, 130
 3610 LINE 130, 107; 130, 70
 3620 LINE 170, 107; 170, 70
 3630 LINE 130, 73; 170, 73
 3640 AREA 130, 73; 136, 75; 136, 71
 3650 AREA 170, 73; 164, 75; 164, 71
 3660 PLOT "REF", 140, 74
 3670 PLOT "d dia", 20, 130
 3680 LINE 60, 130; 70, 125
 3690 LINE 88, 107; 88, 70;
 3700 LINE 212, 107; 212, 70
 3710 LINE 88, 73; 212, 73
 3720 AREA 88, 73; 94, 75; 94, 71
 3730 AREA 130, 73; 124, 75; 124, 71
 3740 AREA 170, 73; 176, 75; 176, 71
 3750 AREA 212, 73; 206, 75; 206, 71
 3760 PLOT "X", 106, 74; 187, 74
 3770 PLOT "O", 106, 109; 190, 109
 3780 SET BRUSH 15 : AREA 5, 60; 314, 60; 314, 20; 5, 20


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3790 SET BRUSH 0 : PLOT "REF = M - 2(d/2+X)", 60, 50
3800 PLOT "tanA=d/2X : 2X=d/tanA : 2X=d*cotanA", 10, 35
3810 SET BRUSH 3 : PLOT "REF = M - d(1+cotanA)", 60, 20
3820 SET PEN 15 : SET CURPDS 2, 24 : PRINT "      PRESS ANY KEY TO CONTINUE"
3830 Answer$ := GET$( ) : CLG
3840 CLG : HOME
3850 Total := 0 : Count := 0
3860 SET PEN 4 : SET PAPER 14 : CLS : PRINT TAB (15); "EXAMPLES"
3870 PRINT k2, ! ! TAB (15); "EXAMPLES"
3880 PRINT TAB (15); "======"
3890 PRINT k2, TAB (15); "======"
3900 SET PEN 9 : PRINT ! TAB (8); "REF = M - d(1+CotanA)"
3910 PRINT k2, ! TAB (8); "REF = M - d(1+CotanA)"
3920 M := (RND(50)) + 75
3930 D := 25 : A := 30 : REM CONSTANT VALUES OF DIAMETER AND ANGLE
3940 Ref := M - 25 * ( 2.732051)
3950 PRINT ! TAB (10); "IF THE READING M IS"; M; "mm,"
3960 PRINT k2, ! TAB (10); "IF THE READING M IS"; M; "mm,"
3970 PRINT ! TAB (10); "THE DIAMETER,d=25 mm"
3980 PRINT k2, ! TAB (10); "THE DIAMETER,d=25 mm"
3990 PRINT ! TAB (10); "AND THE ANGLE,A=30 deg"
4000 PRINT k2, ! TAB (10); "AND THE ANGLE,A=30 deg"
4010 PRINT ! TAB (5); "THEN CALCULATE THE VALUE OF REF"
4020 PRINT k2, ! TAB (5); "THEN CALCULATE THE VALUE OF REF"
4030 PRINT ! TAB (5) "INPUT YOUR ANSWER"; : INPUT R0
4040 PRINT k2, ! TAB (5) "INPUT YOUR ANSWER"; : PRINT k2, R0,
4050 IF ABS(Ref - R0) < 0.1 THEN PLOT "CORRECT", 70, 10 SIZE 3 ELSE 4090
4060 IF ABS(Ref - R0) < 0.1 THEN PRINT k2, "CORRECT"
4070 FOR I := 1 TO 1000 : NEXT I
4080 GOTO 4150

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4090 PRINT TAB (3) "NO!That is NOT right,try again"
4100 PRINT h2, TAB (3) "NO!That is NOT right,try again"
4110 Total := Total + 1
4120 IF Total < 3 THEN 4030
4130 GOSUB 4180
4140 GOTO 3850
4150 Count := Count + 1
4160 IF Count < 4 THEN CLS : HOME : GOTO 3860
4170 GOTO 4270
4180 PRINT ! "THIS IS THE CORRECT METHOD OF SOLUTION"
4190 PRINT h2, ! "THIS IS THE CORRECT METHOD OF SOLUTION"
4200 PRINT ! TAB (5); "REF = M - d(1+cotanA)"
4210 PRINT h2, ! TAB (5); "REF = M - d(1+cotanA)"
4220 PRINT ! TAB (5); M; "-25(1+cotan30)="; Ref; "aa"
4230 PRINT h2, ! TAB (5); M; "-25(1+cotan30)="; Ref; "aa"
4240 FOR I := 1 TO 3000 : NEXT I
4250 CLG : HOME
4260 RETURN
4270 ENDPROC
4280 PROCEDURE Graph
4290 GLOBAL Fred$
4300 PRINT h2, Fred$
4310 PRINT h2, "Graphs"
4320 CLG : SET BRUSH 0 : AREA 35, 95; 25, 105; 25, 185; 35, 195; 295, 195; 305, 185; 305, 105; 295, 95
4330 SET BRUSH 15 : AREA 30, 100; 20, 110; 20, 190; 30, 200; 290, 200; 300, 190; 300, 110; 290, 100
4340 SET BRUSH 10 : PLOT "GRAPHS", 65, 140 SIZE 4
4350 PLOT "F & N LEVEL", 30, 110 SIZE 3
4360 FOR I := 1 TO 2000 : NEXT I
4370 CLS : HOME

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4380 AREA 0, 0; 0, 249; 319, 249; 319, 0 BRUSH 4 STYLE 3
4390 AREA 2, 2; 2, 247; 317, 247; 317, 2 BRUSH 4 STYLE 3
4400 SET BRUSH 14 : PLOT "GRAPHS", 140, 225
4410 PLOT "(1) STRAIGHT LINE GRAPHS:  $Y = AX + B$ ", 10, 205
4420 PLOT "(2) QUADRATIC GRAPHS:  $Y = AX^2 + BX + C$ ", 10, 185
4430 PLOT "CHOOSE A NUMBER AND PRESS ENTER KEY.", 20, 125
4440 PLOT "YOU WILL NEED A CALCULATOR.", 45, 105
4450 SET CURPOS 20, 20
4460 Count := 1
4470 INPUT Choose
4480 ON Choose GOSUB 4500, 5460
4490 IF Choose > 2 THEN 4370
4500 Axes
4510 FOR Count := 1 TO 10 STEP 2
4520   A := RND(6)
4530   B := RND(10)
4540   X1 := - 100 : Y1 := A * X1 + B * 10
4550   X2 := 100 : Y2 := A * X2 + B * 10
4560   SET BRUSH Count
4570   LINE X1, Y1; X2, Y2
4580   SET WRITING 1 TO 50, 20; 60, 22
4590   SET WRITING 1 : SET PAPER 3
4600   CLS
4610   SET WRITING 1 : INPUT " A"; A1 : IF ABS(A1 - A) < 1 THEN PRINT " CORRECT" ELSE PRINT " TRY AGAIN"
      : GOTO 4610
4620   INPUT " B"; B1 : IF ABS(B1 - B) < 1 THEN PRINT " CORRECT" ELSE PRINT " TRY AGAIN" : GOTO 4620
4630   SET BRUSH 3 : PLOT "PRESS ANY KEY TO CONTINUE", 20, - 90
4640   Answer$ := GET$( )
4650   SET BRUSH 0 : PLOT "PRESS ANY KEY TO CONTINUE", 20, - 90

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4660   CLS
4670   NEXT Count
4680   Axes
4690   FOR Count := 1 TO 10 STEP 2
4700     A := - (RND(6)) : B := RND(10)
4710     X1 := - 100 : Y1 := A * X1 + B * 10
4720     X2 := 100 : Y2 := A * X2 + B * 10
4730     SET BRUSH Count
4740     LINE X1, Y1; X2, Y2
4750     SET WRITING 1 TO 50, 20; 60, 22
4760     SET WRITING 1 : SET PAPER 3
4770     CLS
4780     SET WRITING 1 : INPUT " A"; A1 : IF ABS(A1 - A) < 1 THEN PRINT "  CORRECT" ELSE PRINT "  TRY AGAIN"
        : GOTO 4780
4790     INPUT " B"; B1 : IF ABS(B1 - B) < 1 THEN PRINT "  CORRECT" ELSE PRINT "  TRY AGAIN" : GOTO 4790
4800     SET BRUSH 3 : PLOT "PRESS ANY KEY TO CONTINUE", 20, - 90
4810     Answer$ := GET$( )
4820     SET BRUSH 0 : PLOT "PRESS ANY KEY TO CONTINUE", 20, - 90
4830   CLS : NEXT Count
4840   Axes
4850   FOR Count := 1 TO 10 STEP 2
4860     A := RND(6) : B := - (RND(10))
4870     X1 := - 100 : Y1 := A * X1 + B * 10
4880     X2 := 100 : Y2 := A * X2 + B * 10
4890     SET BRUSH Count
4900     LINE X1, Y1; X2, Y2
4910     SET WRITING 1 TO 50, 20; 60, 22 : SET WRITING 1 : SET PAPER 3
4920     CLS
4930     SET WRITING 1 : INPUT " A"; A1 : IF ABS(A1 - A) < 1 THEN PRINT "  CORRECT" ELSE PRINT "  TRY AGAIN"

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      : GOTO 4930

4940   INPUT " B"; B1 : IF ABS(B1 - B) < 1 THEN PRINT " CORRECT" ELSE PRINT " TRY AGAIN" : GOTO 4940
4950   SET BRUSH 3 : PLOT "PRESS ANY KEY TO CONTINUE", 20, - 90
4960   Answer$ := GET$( )
4970   SET BRUSH 0 : PLOT "PRESS ANY KEY TO CONTINUE", 20, - 90
4980   CLS : NEXT Count
4990   Axes

5000   FOR Count := 1 TO 10 STEP 2
5010     A := - (RND(6)) : B := - (RND(10))
5020     X1 := - 100 : Y1 := A * X1 + B * 10
5030     X2 := 100 : Y2 := A * X2 + B * 10
5040     SET BRUSH Count
5050     LINE X1, Y1; X2, Y2
5060     SET WRITING 1 TO 50, 20; 60, 22
5070     SET WRITING 1 : SET PAPER 3
5080     CLS
5090     SET WRITING 1 : INPUT " A"; A1 : IF ABS(A1 - A) < 1 THEN PRINT " CORRECT" ELSE PRINT " TRY AGAIN"
      : GOTO 5090

5100   INPUT " B"; B1 : IF ABS(B1 - B) < 1 THEN PRINT " CORRECT " ELSE PRINT " TRY AGAIN" : GOTO 5100
5110   SET BRUSH 3 : PLOT "PRESS ANY KEY TO CONTINUE", 20, - 90
5120   Answer$ := GET$( )
5130   SET BRUSH 0 : PLOT "PRESS ANY KEY TO CONTINUE", 20, - 90
5140   CLS : NEXT Count
5150   SET WRITING 0
5160 ENDPROC

5170 PROCEDURE Axes
5180   SET MODE 80, 200, 200
5190   SET ORIGIN 100, 100
5200   SET PEN 2

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5210 SET BRUSH 3
5220 LINE - 100, 0; 100, 0
5230 LINE 0, - 100; 0, 100
5240 FOR I := 0 TO 200 STEP 5
5250     LINE - 100 + I, 5; - 100 + I, 0
5260 NEXT I
5270 FOR J := 0 TO 200 STEP 5
5280     LINE - 5, - 100 + J; 0, - 100 + J
5290 NEXT J
5300 FOR In := 0 TO 200 STEP 10
5310     LINE - 100 + In, - 5; - 100 + In, 0
5320 NEXT In
5330 FOR Vin := 0 TO 200 STEP 10
5340     LINE 3, - 100 + Vin; 0, - 100 + Vin
5350 NEXT Vin
5360 SET BRUSH 2
5370 PLOT "-10", 3, - 102; - 100, - 19
5380 PLOT "-5", 3, - 52; - 52, - 19
5390 PLOT "5", 5, 48; 50, - 19
5400 PLOT "10", 5, 95; 95, - 19
5410 PLOT "Y = AX + B", - 90, 90
5420 PLOT "Determine the values", - 90, 80
5430 PLOT "of A and B from the graph.", - 90, 70
5440 PLOT "A and B are integers.", - 90, 60
5450 ENDPROC
5460 FOR Count := 1 TO 10 STEP 2
5470     Axes2
5480     Text
5490     A := RND(3) : B := - (RND(5)) : C := - (RND(8))

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5500  FOR X := - 10 TO 10 STEP 0.2
5510    Y := A * X*X + B * X + C
5520    SET BRUSH 2
5530    POINTS X * 5, Y STYLE 2
5540  NEXT X
5550  R1 := (- B - SQRT(B 2 - 4 * A * C)) / (2 * A)
5560  R2 := (- B + SQRT(B 2 - 4 * A * C)) / (2 * A)
5570  SET CURPOS 50, 3 : SET PEN 3 : PRINT "Y = "; A; "X 2 "; B; "X "; C
5580  SET PEN 3 : SET CURPOS 50, 6 : CLL 2
5590  INPUT "INPUT LEFT ROOT" Left1
5600  SET CURPOS 50, 7 : IF ABS(R1 - Left1) < 0.15 THEN PRINT "LEFT ROOT CORRECT" ELSE 5580
5610  SET CURPOS 50, 8 : PRINT "TRUE VALUE =", R1
5620  FOR I := 1 TO 1000 : NEXT I : SET CURPOS 50, 10 : CLL 2
5630  INPUT "INPUT RIGHT ROOT" Right1
5640  SET CURPOS 50, 11 : IF ABS(R2 - Right1) < 0.15 THEN PRINT "RIGHT ROOT CORRECT" ELSE 5620
5650  SET CURPOS 50, 12 : PRINT "TRUE VALUE =", R2
5660  FOR I := 1 TO 2000 : NEXT I : NEXT Count
5670  FOR Count := 1 TO 10 STEP 2
5680    Axes2
5690    Text1
5700    A := RND(3) : B := - (RND(5)) : C := - (RND(8))
5710    FOR X := - 10 TO 10 STEP 0.2
5720      Y := A * X 2 + B * X + C
5730      SET BRUSH 2
5740      POINTS X * 5, Y STYLE 2
5750    NEXT X
5760    R1 := (- B - SQRT(B 2 - 4 * A * C)) / (2 * A)
5770    R2 := (- B + SQRT(B 2 - 4 * A * C)) / (2 * A)
5780    SET CURPOS 50, 3 : SET PEN 3 : PRINT "Y = "; A; "X 2 "; B; "X "; C

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5790 ENDPROC

5800 SET PEN 3 : SET CURPOS 50, 6 : CLL 2

5810 INPUT "INPUT LEFT ROOT" Left1

5820 SET CURPOS 50, 7 : IF ABS(R1 - Left1) < 0.15 THEN PRINT "LEFT ROOT CORRECT" ELSE 5800

5830 SET CURPOS 50, 8 : PRINT "TRUE VALUE =", R1

5840 FOR I := 1 TO 1000 : NEXT I : SET CURPOS 50, 10 : CLL 2

5850 INPUT "INPUT RIGHT ROOT" Right1

5860 SET CURPOS 50, 11 : IF ABS(R2 - Right1) < 0.15 THEN PRINT "RIGHT ROOT CORRECT" ELSE 5840

5870 SET CURPOS 50, 12 : PRINT "TRUE VALUE =", R2

5880 FOR I := 1 TO 2000 : NEXT I : NEXT Count

5890 SET MODE 40 : GOTO 310

5900 PROCEDURE Round

5910  GLOBAL Fred$

5920  PRINT k2, Fred$

5930  PRINT k2, "Properties of a Circle"

5940  CLG : SET BRUSH 0 : AREA 35, 95; 25, 105; 25, 185; 35, 195; 295, 195; 305, 185; 305, 105; 295, 95

5950  SET BRUSH 15 : AREA 30, 100; 20, 110; 20, 190; 30, 200; 290, 200; 300, 190; 300, 110; 290, 100

5960  SET BRUSH 4 : PLOT "TERMINOLOGY", 75, 170 SIZE 2

5970  PLOT "AND PROPERTIES OF", 27, 150 SIZE 2

5980  PLOT "THE CIRCLE", 80, 130 SIZE 2

5990  SET BRUSH 9 : PLOT "F LEVEL", 100, 100 SIZE 2

6000  FOR I := 1 TO 2000 : NEXT I

6010  CLG : SET BRUSH 4 : PLOT "TERMINOLOGY & PROPERTIES OF THE CIRCLE", 10, 235

6020  SET BRUSH 4 : CIRCLE 50, 160, 180 STYLE 3

6030  PLOT "O", 157, 173

6040  PLOT "A circle is a plane figure enclosed by a", 1, 115

6050  PLOT "curved line, every point on which is equi", 1, 105

6060  PLOT "distant from a point within called the", 1, 95

6070  PLOT "CENTRE.O is the centre of the circle.", 1, 85

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6080  FOR I := 1 TO 5000 : NEXT I
6090  SET BRUSH 2 : LINE 160, 180; 208, 190
6100  PLOT "A", 212, 190
6110  PLOT "r", 180, 190
6120  PLOT "The distance from the centre to the ", 15, 75
6130  PLOT "curve,OA,is called the RADIUS,r, of the", 1, 65
6140  PLOT "circle.", 1, 55
6150  FOR I := 1 TO 3000 : NEXT I
6160  SET BRUSH 15 : LINE 160, 130; 160, 230
6170  PLOT "B", 162, 218
6180  PLOT "C", 162, 130
6190  PLOT "Any straight line passing through the", 15, 45
6200  PLOT "d", 150, 180
6210  PLOT "centre and touching the circumference", 15, 35
6220  PLOT "at each end as BC does is called the", 15, 25
6230  PLOT "DIAMETER,d.The diameter is twice the", 15, 15
6240  PLOT "length of the radius.d=2r.", 15, 5 : FOR I := 1 TO 5000 : NEXT I
6250  PLOT "PRESS SPACE-BAR", 5, 135
6260  PLOT "TO CONTINUE", 5, 125
6270  Answer$ := GET$(1) : CLG
6280  CIRCLE 50, 160, 180 STYLE 3
6290  SET BRUSH 6 : LINE 160, 130; 160, 230
6300  PLOT "d", 165, 185 : SET BRUSH 15
6310  SET BRUSH 6
6320  PLOT "The boundary of a circle,that is the", 15, 115
6330  PLOT "perimeter,is called the CIRCUMFERENCE,", 15, 105
6340  PLOT "c.c/d is equal to the constant PI.", 15, 95
6350  PLOT "PI=3.142 to three decimal places.", 15, 85
6360  SET DEG TRUE : SLICE 50, 0 TO 115, 160, 180 STYLE 3

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6370 SET BRUSH 1 : LINE 160, 180; 205, 159
6380 SET BRUSH 15 : PLOT "O", 157, 174
6390 SET BRUSH 6 : POINTS 205, 159; 160, 180
6400 FOR I := 1 TO 6000 : NEXT I
6410 SET BRUSH 5 : LINE 97, 130; 119, 230 : LINE 160, 180; 112, 191
6420 SET BRUSH 15 : PLOT "H", 100, 192 : SET BRUSH 5 : PLOT "F", 88, 125
6430 PLOT "G", 110, 230
6440 PLOT "A TANGENT to a circle is a straight", 15, 65
6450 PLOT "line which meets the circle at one", 15, 55
6460 PLOT "point,H.FG is a Tangent to the circle.", 15, 45
6470 PLOT "If radius OH is drawn then FHO is", 15, 35
6480 PLOT "a RIGHT-ANGLE.", 15, 25 : FOR I := 1 TO 7000 : NEXT I
6490 SET BRUSH 3 : PLOT "PRESS SPACE-BAR TO CONTINUE.", 50, 5
6500 Answer$ := GET$( ) : CLG
6510 SET BRUSH 2 : SLICE 50, 60 TO 120, 160, 180
6520 SET BRUSH 15 : CIRCLE 50, 160, 180 STYLE 3
6530 SET BRUSH 15 : PLOT "O", 155, 177
6540 PLOT "X", 210, 150 : PLOT "Y", 210, 200
6550 PLOT "The shaded portion OXY is called a", 5, 115
6560 PLOT "SECTOR.", 5, 105
6570 PLOT "If the sector is less than a semi-", 5, 95
6580 PLOT "circle it is a MINOR SECTOR.If larger", 5, 85
6590 PLOT "than a semi-circle it is a MAJOR SECTOR.", 5, 75
6600 FOR I := 1 TO 3000 : NEXT I
6610 LINE 132, 138; 160, 230
6620 PLOT "U", 122, 130
6630 PLOT "V", 160, 230
6640 PLOT "The line UV is a CHORD.", 5, 65
6650 FOR I := 1 TO 1000 : NEXT I

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6660 SET BRUSH 5 : FLOOD 130, 180
6670 PLOT "The shaded portion UV is a SEGMENT.", 5, 55
6680 PLOT "The shortest distance between U and V ", 5, 45
6690 PLOT "along the circumference is called the", 5, 35
6700 PLOT "MINOR ARC.The remaining part of the", 5, 25
6710 PLOT "circumference is the MAJOR ARC.", 5, 15
6720 FOR I := 1 TO 2000 : NEXT I
6730 SET BRUSH 4 : PLOT "PRESS THE SPACE BAR TO CONTINUE.", 30, 5
6740 Answer$ := GET$( ) : CLG
6750 CIRCLE 50, 160, 180 STYLE 3
6760 SET BRUSH 15 : SLICE 50, 0 TO 57, 160, 180 STYLE 3
6770 PLOT "0", 165, 190
6780 PLOT "r", 185, 185; 185, 230
6790 PLOT "An angle can be measured in DEGREES or", 2, 115
6800 PLOT "RADIANS.A RADIAN is defined as the angle", 2, 105
6810 PLOT "formed at the centre of a circle by an", 2, 95
6820 PLOT "ARC equal in length to the RADIUS.", 2, 85
6830 PLOT "0 = 1 radian = 57.3 deg.", 30, 65
6840 PLOT "2xPI radians = 360 degs.", 60, 45
6850 SET BRUSH 3 : PLOT "PRESS SPACE BAR TO CONTINUE", 50, 15
6860 Answer$ := GET$( ) : CLG
6870 SET BRUSH 2 : CIRCLE 50, 160, 180
6880 SET BRUSH 15 : PLOT "r", 185, 185
6890 LINE 160, 180; 210, 180
6900 PLOT "2", 235, 115; 180, 98
6910 PLOT "Area of a circle =  $\pi r^2$ ", 50, 110
6920 PLOT "or  $\pi r^2$ ", 125, 90
6930 PLOT "----", 150, 85
6940 PLOT "4", 160, 80

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```

6950  PLOT "Have a go at the following questions.", 10, 50
6960  PLOT "PRESS SPACE BAR TO CONTINUE", 50, 30
6970  Answer$ := GET$( )
6980  Round1
6990  Round2
7000  Round3
7010  Round4
7020  Round5
7030  ENDPROC
7040  PROCEDURE Round1
7050  CLS : SET PAPER 1 : SET BRUSH 8
7060  CIRCLE 40, 170, 200
7070  SET BRUSH 4 : LINE 170, 200; 210, 200
7080  PLOT "r", 177, 200
7090  PLOT "AREA OF A CIRCLE          PROBLEM", 1, 220
7100  Total := 0 : Count := 0
7110  SET WRITING 1 TO 1, 11; 40, 15
7120  SET WRITING 2 TO 1, 16; 40, 25
7130  LINE 0, 150; 319, 150
7140  SET WRITING 1 : SET PAPER 15
7150  SET WRITING 1 : CLS : SET WRITING 2 : CLS : SET PEN 6
7160  R := RND(50)
7170  PRINT 1, "If the radius r ="; R; "cm then calculate"
7180  PRINT A2 !, "If the radius r ="; R; "cm then calculate"
7190  PRINT 1; TAB (3); "the area of the circle shown above."
7200  PRINT A2 !; TAB (3); "the area of the circle shown above."
7210  SET CURPOS 0, 1 : PRINT 2 ! "Input your answer for the area";
7220  SET WRITING 2 : INPUT A1 : PRINT A2 !; "AREA = "; A1
7230  A := PI * R * R

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```

7240 IF ABS(A - A1) < 1e-02 THEN SET BRUSH 1 : PLOT "WELL DONE", 60, 10 SIZE 3 ELSE 7270
7250 IF ABS(A - A1) < 1e-02 THEN PRINT h2 !, "WELL DONE"
7260 FOR I := 1 TO 2000 : NEXT I : CLS 2 : IF ABS(A - A1) < 1e-02 THEN 7350
7270 PRINT 2, TAB (2) "No! You have made a mistake,try again"
7280 PRINT h2 !, TAB (2) "No! You have made a mistake,try again"
7290 FOR I := 1 TO 1000 : NEXT I
7300 CLS 2
7310 Total := Total + 1
7320 IF Total < 3 THEN 7210
7330 GOSUB 7380
7340 GOTO 7050
7350 Count := Count + 1
7360 IF Count < 4 THEN 7150
7370 GOTO 7470
7380 SET CURPOS 0, 1 : PRINT 2 ! TAB (1) "THIS IS THE CORRECT METHOD OF SOLUTION."
7390 PRINT h2 !, TAB (1) "THIS IS THE CORRECT METHOD OF SOLUTION."
7400 PRINT 2 !, TAB (7) "AREA = PIxRADIUSxRADIUS"
7410 PRINT h2 !, TAB (7) "AREA = PIxRADIUSxRADIUS"
7420 PRINT 2, TAB (7) "AREA = "; PI * R * R; "CM2"
7430 PRINT h2 !, TAB (7) "AREA = "; PI * R * R; "CM2"
7440 PRINT 2 !, TAB (6); "PRESS SPACE-BAR TO CONTINUE"
7450 Answer$ := GET$(1)
7460 RETURN
7470 ENDPROC
7480 PROCEDURE Round2
7490 CLG : SET PAPER 1 : SET BRUSH 8
7500 CIRCLE 40, 170, 200
7510 SET BRUSH 4 : LINE 130, 200; 210, 200
7520 PLOT "d", 168, 200

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7530 PLOT "AREA OF A CIRCLE          PROBLEM", 1, 220
7540 Total := 0 : Count := 0
7550 SET WRITING 1 TO 1, 11; 40, 15
7560 SET WRITING 2 TO 1, 16; 40, 25
7570 LINE 0, 150; 319, 150
7580 SET WRITING 1 : SET PAPER 15
7590 SET WRITING 1 : CLS : SET WRITING 2 : CLS : SET PEN 6
7600 D := RND(25)
7610 PRINT 1, "If the diameter d="; D; "cm then calculate"
7620 PRINT K2 !, "If the diameter d="; D; "cm then calculate"
7630 PRINT 1; TAB (3); "the area of the circle shown above."
7640 PRINT K2 !; TAB (3); "the area of the circle shown above."
7650 SET CURPOS 0, 1 : PRINT 2 ! TAB (2) "Input your answer for the area";
7660 SET WRITING 2 : INPUT A1 : PRINT K2; "AREA = "; A1
7670 A := PI * D * D / 4
7680 IF ABS(A - A1) < 1e-02 THEN SET BRUSH 1 : PLOT "WELL DONE", 60, 10 SIZE 3 ELSE 7710
7690 IF ABS(A - A1) < 1e-02 THEN PRINT K2 !, "WELL DONE"
7700 FOR I := 1 TO 2000 : NEXT I : CLS 2 : IF ABS(A - A1) < 1e-02 THEN 7790
7710 PRINT 2, TAB (2) "No! You have made a mistake,try again"
7720 PRINT K2 !, TAB (2) "No! You have made a mistake,try again"
7730 FOR I := 1 TO 1000 : NEXT I
7740 CLS 2
7750 Total := Total + 1
7760 IF Total < 3 THEN 7650
7770 GOSUB 7820
7780 GOTO 7490
7790 Count := Count + 1
7800 IF Count < 4 THEN 7590
7810 GOTO 7910

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7820 SET CURPOS 0, 1 : PRINT 2 ! TAB (1) "THIS IS THE CORRECT METHOD OF SOLUTION."
7830 PRINT #2 !, TAB (1) "THIS IS THE CORRECT METHOD OF SOLUTION."
7840 PRINT 2 !, TAB (7) "AREA = PIxDIAxDIA"
7850 PRINT #2 !, TAB (7) "AREA = PIxDIAxDIA"
7860 PRINT 2, TAB (7) "AREA = "; PI * D * D; "CM2"
7870 PRINT #2 !, TAB (7) "AREA = "; PI * D * D; "CM2"
7880 PRINT 2 !, TAB (6); "PRESS SPACE-BAR TO CONTINUE"
7890 Answer$ := GET$( )
7900 RETURN
7910 ENDPROC
7920 PROCEDURE Round3
7930 CLG : SET PAPER 15 : SET BRUSH 8
7940 CIRCLE 40, 170, 200 STYLE 3
7950 SET DEG FALSE
7960 SET BRUSH 4 : SLICE 40, 1 TO 2, 170, 200
7970 SET BRUSH 15 : PLOT "O", 180, 195
7980 SET BRUSH 8 : PLOT "A", 205, 220
7990 PLOT "B", 205, 168
8000 PLOT "r", 185, 210
8010 PLOT "LENGTH OF ARC", 1, 235
8020 PLOT "PROBLEM", 5, 225
8030 PLOT " ARC,AB = RADIUS X 0(RAD)", 1, 148
8040 Total := 0 : Count := 0
8050 SET WRITING 1 TO 1, 12; 40, 15
8060 SET WRITING 2 TO 1, 16; 40, 25
8070 LINE 0, 148; 319, 148
8080 SET WRITING 1 : CLS : SET WRITING 2 : CLS : SET PEN 6
8090 SET DEG FALSE
8100 R := RND(20) + 5 : Angle := RND(1) * 2 * PI

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8110 PRINT 1, TAB (5); "If the radius ="; R; "cm and the"
8120 PRINT &2 !, TAB (5); "If the radius ="; R; "cm and the"
8130 PRINT 1, TAB (5) "angle = " Angle; " rads then"
8140 PRINT &2 !, TAB (5) "angle = " Angle; " rads then"
8150 PRINT 1, TAB (5) "calculate the ARC length AB"
8160 PRINT &2 !, TAB (5) "calculate the ARC length AB"
8170 SET CURPOS 0, 1 : PRINT 2 ! " Input your answer for the arc length ";
8180 SET WRITING 2 : INPUT Arc1 : PRINT &2 !; "ARC = "; Arc1
8190 Arc := R * Angle
8200 IF ABS(Arc - Arc1) < 1e-02 THEN SET BRUSH 1 : PLOT "WELL DONE", 60, 10 SIZE 3 ELSE B230
8210 IF ABS(Arc - Arc1) < 1e-02 THEN PRINT &2 !, "WELL DONE"
8220 FOR I := 1 TO 2000 : NEXT I : CLS 2 : IF ABS(Arc - Arc1) < 1e-02 THEN B310
8230 PRINT 2, TAB (2) "No! You have made a mistake,try again"
8240 PRINT &2 !, TAB (2) "No! You have made a mistake,try again"
8250 FOR I := 1 TO 1000 : NEXT I
8260 CLS 2
8270 Total := Total + 1
8280 IF Total < 3 THEN B170
8290 GOSUB B340
8300 GOTO 7930
8310 Count := Count + 1
8320 IF Count < 4 THEN B0B0
8330 GOTO B430
8340 SET CURPOS 0, 1 : PRINT 2 ! TAB (1) "THIS IS THE CORRECT METHOD OF SOLUTION."
8350 PRINT &2 !, TAB (1) "THIS IS THE CORRECT METHOD OF SOLUTION."
8360 PRINT 2 !, TAB (7) "ARC =RADIUS X ANGLE(RAD)"
8370 PRINT &2 !, TAB (7) "ARC =RADIUS X ANGLE(RAD)"
8380 PRINT 2, TAB (7) "ARC = "; R * Angle; "CM"
8390 PRINT &2 !, TAB (7) "ARC = "; R * Angle; "CM"

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8400 PRINT 2 !, TAB (6); "PRESS SPACE-BAR TO CONTINUE"

8410 Answer$ := GET$(1)

8420 RETURN

8430 ENDPROC

8440 PROCEDURE Round4

8450 CLG : SET PAPER 15 : SET BRUSH 8

8460 CIRCLE 40, 170, 200 STYLE 3

8470 SET BRUSH 4 : SLICE 40, 1 TO 2, 170, 200

8480 SET BRUSH 15 : PLOT "O", 180, 195

8490 SET BRUSH 8 : PLOT "A", 205, 220

8500 PLOT "B", 205, 168

8510 PLOT "r", 185, 210

8520 PLOT "LENGTH OF ARC", 1, 235

8530 PLOT "PROBLEM", 5, 225

8540 PLOT " ARC,AB = RADIUS X  $\theta$  (RAD)", 1, 148

8550 Total := 0 : Count := 0

8560 SET WRITING 1 TO 1, 12; 40, 15

8570 SET WRITING 2 TO 1, 16; 40, 25

8580 LINE 0, 148; 319, 148

8590 SET WRITING 1 : CLS : SET WRITING 2 : CLS : SET PEN 6

8600 SET DEG FALSE

8610 R := RND(20) + 5 : Arc := RND(40) + 10

8620 PRINT 1, TAB (5); "If the radius ="; R; "cm and the"

8630 PRINT &2 !, TAB (5); "If the radius ="; R; "cm and the"

8640 PRINT 1, TAB (5) "ARC = " Arc; " cm then"

8650 PRINT &2 !, TAB (5) "ARC = " Arc; " cm then"

8660 PRINT 1, TAB (5) "calculate the angle  $\theta$  in rads"

8670 PRINT &2 !, TAB (5) "calculate the angle  $\theta$  in rads"

8680 SET CURPOS 0, 1 : PRINT 2 ! TAB (5) "Input your answer for the angle  $\theta$ "

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8690 SET WRITING 2 : INPUT Angle1 : PRINT #2 !; "angle = "; Angle1
8700 Angle := Arc / R
8710 IF ABS(Angle - Angle1) < 1e-02 THEN SET BRUSH 1 : PLOT "THAT'S RIGHT", 20, 10 SIZE 3 ELSE 8740
8720 IF ABS(Angle - Angle1) < 1e-02 THEN PRINT #2 !, "THAT'S RIGHT"
8730 FOR I := 1 TO 2000 : NEXT I : CLS 2 : IF ABS(Angle - Angle1) < 1e-02 THEN 8820
8740 PRINT 2, TAB (2) "No! You have made a mistake,try again"
8750 PRINT #2 !, TAB (2) "No! You have made a mistake,try again"
8760 FOR I := 1 TO 1000 : NEXT I
8770 CLS 2
8780 Total := Total + 1
8790 IF Total < 3 THEN 8680
8800 GOSUB 8850
8810 GOTO 8450
8820 Count := Count + 1
8830 IF Count < 4 THEN 8590
8840 GOTO 8940
8850 SET CURPOS 0, 1 : PRINT 2 ! TAB (1) "THIS IS THE CORRECT METHOD OF SOLUTION."
8860 PRINT #2 !, TAB (1) "THIS IS THE CORRECT METHOD OF SOLUTION."
8870 PRINT 2 !, TAB (7) "ANGLE 0 =ARC/RADIUS"
8880 PRINT #2 !, TAB (7) "ANGLE 0 = ARC/RADIUS"
8890 PRINT 2, TAB (7) "ANGLE = "; Arc / R; "Rads"
8900 PRINT #2 !, TAB (7) "ANGLE = "; Arc / R; "Rads"
8910 PRINT 2 !, TAB (6); "PRESS SPACE-BAR TO CONTINUE"
8920 Answer$ := GET$( )
8930 RETURN
8940 ENDPROC
8950 PROCEDURE Round5
8960 CLG : SET PAPER 15 : SET BRUSH 8
8970 CIRCLE 40, 170, 200 STYLE 3

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8980 PLOT "AREA OF SECTOR", 20, 235
8990 PLOT "PROBLEMS", 35, 225
9000 PLOT " AREA OF SECTOR = RADxRADxANGLE(rads)/2", 0, 148
9010 Total := 0 : Count := 0
9020 SET WRITING 1 TO 1, 12; 40, 15
9030 SET WRITING 2 TO 1, 16; 40, 25
9040 LINE 0, 148; 319, 148
9050 SET WRITING 1 : CLS : SET WRITING 2 : CLS : SET PEN 6
9060 SET DEG FALSE
9070 R := RND(20) + 5 : Angle := RND(1) * 2 * PI + 0.25
9080 SET BRUSH 4 : SLICE 40, 0 TO Angle, 170, 200
9090 PRINT 1; TAB (5) "If the radius ="; R; "cm and the"
9100 PRINT A2 !, TAB (5); "If the radius ="; R; "cm and the"
9110 PRINT 1, "angle = " Angle; " rads then calculate"
9120 PRINT A2 !, TAB (5) "angle = " Angle; " rads then"
9130 PRINT 1, "the area of the SECTOR in cm2"
9140 PRINT A2 !, TAB (5) "calculate the area of the SECTOR in cm2"
9150 SET CURPOS 0, 1 : PRINT 2 ! TAB (5) "Input your answer for the area"
9160 SET WRITING 2 : INPUT Areal : PRINT A2 !; "area = "; Areal
9170 Sector Area := R * R * Angle / 2
9180 IF ABS(Sector Area - Areal) < 1e-02 THEN SET BRUSH 1 : PLOT "THAT'S RIGHT", 20, 10 SIZE 3 ELSE 9210
9190 IF ABS(Sector Area - Areal) < 1e-02 THEN PRINT A2 !, "THAT'S RIGHT"
9200 FOR I := 1 TO 2000 : NEXT I : CLS 2 : IF ABS(Sector Area - Areal) < 1e-02 THEN 9290
9210 PRINT 2, TAB (2) "No! You have made a mistake,try again"
9220 PRINT A2 !, TAB (2) "No! You have made a mistake,try again"
9230 FOR I := 1 TO 1000 : NEXT I
9240 CLS 2
9250 Total := Total + 1
9260 IF Total < 3 THEN 9150

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9270 GOSUB 9320

9280 GOTO 8960

9290 Count := Count + 1

9300 IF Count < 4 THEN 9050

9310 GOTO 9410

9320 SET CURPOS 0, 1 : PRINT 2 ! TAB (1) "THIS IS THE CORRECT METHOD OF SOLUTION."

9330 PRINT A2 !, TAB (1) "THIS IS THE CORRECT METHOD OF SOLUTION."

9340 PRINT 2 !, TAB (2) "AREA OF SECTOR = RAD x RAD x ANGLE/2"

9350 PRINT A2 !, TAB (7) "AREA OF SECTOR = RAD x RAD x ANGLE/2"

9360 PRINT 2, TAB (2) "AREA OF SECTOR = "; R * R * Angle / 2; "cm2"

9370 PRINT A2 !, TAB (7) "AREA OF SECTOR = "; R * R * Angle / 2; "cm2"

9380 PRINT 2 !, TAB (6); "PRESS SPACE-BAR TO CONTINUE"

9390 Answer$ := GET$( )

9400 RETURN

9410 ENDPROC

9420 PROCEDURE Axes2

9430 SET MODE 80, 100, 120

9440 SET ORIGIN 50, 20

9450 SET PEN 2

9460 SET BRUSH 3

9470 LINE - 50, 0; 50, 0

9480 LINE 0, - 20; 0, 100

9490 FOR I := 0 TO 110 STEP 2.5

9500 LINE - 50 + I, 1; - 50 + I, 0

9510 NEXT I

9520 FOR J := 0 TO 120 STEP 5

9530 LINE - 0.5, - 20 + J; 0, - 20 + J

9540 NEXT J

9550 FOR In := 0 TO 100 STEP 1.25

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9560     LINE - 50 + In, - 1; - 50 + In, 0
9570 NEXT In
9580 FOR Vin := 0 TO 120 STEP 2.5
9590     LINE 0.3, - 20 + Vin; 0, - 20 + Vin
9600 NEXT Vin
9610 SET BRUSH 2
9620 PLOT "-10", - 50, - 8
9630 PLOT "-5", - 27, - 8
9640 PLOT "5", 25, - 8
9650 PLOT "10", 48, - 8
9660 PLOT "-20", 2, - 21
9670 PLOT "20", 3, 18
9680 PLOT "40", 3, 38
9690 PLOT "60", 3, 58
9700 PLOT "80", 3, 78
9710 PLOT "100", 3, 96
9720 SET BRUSH 3
9730 ENDPROC
9740 PROCEDURE Text
9750 PLOT "Y = AXxX + BX + C", - 45, 90
9760 PLOT "Determine the values", - 45, 85
9770 PLOT "of the ROOTS of the", - 45, 80
9780 PLOT "equation from the graph.", - 45, 75
9790 ENDPROC
9800 PROCEDURE Text1
9810 PLOT "Calculate the ROOTS of", - 45, 85
9820 PLOT "the equation shown", - 45, 80
9830 PLOT "by using the general formula", - 45, 75
9840 ENDPROC
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9850 PROCEDURE Trig1
9860  GLOBAL Fred$
9870  PRINT #2, Fred$
9880  PRINT #2, "Trigonometry"
9890  CLG : SET PAPER 1 : SET BRUSH 0 : AREA 35, 95; 25, 105; 25, 185;
      35, 195; 295, 195; 305, 185; 305, 105; 295, 95
9900  SET BRUSH 15 : AREA 30, 100; 20, 110; 20, 190; 30, 200; 290, 200; 300, 190; 300, 110; 290, 100
9910  SET BRUSH 8 : PLOT "TRIGONOMETRY", 20, 150 SIZE 3
9920  SET BRUSH 3 : PLOT "F LEVEL", 80, 120 SIZE 3
9930  FOR I := 1 TO 1000 : NEXT I
9940  CLG : SET BORDER 1 : SET BRUSH 15 : PLOT "INTRODUCTION TO TRIGONOMETRY", 50, 230
9950  PLOT "THE RIGHT-ANGLED TRIANGLE", 60, 220
9960  SET BRUSH 15 : AREA 10, 150; 100, 210; 100, 150 STYLE 3
9970  LINE 90, 150; 90, 160; 100, 160
9980  PLOT "A", 5, 140 : PLOT "B", 105, 140 : PLOT "C", 105, 210
9990  SET BRUSH 10 : PLOT "a", 105, 175 : PLOT "b", 45, 185 : PLOT "c", 50, 140
10000 PLOT "SINE A = a/b", 5, 120
10010 PLOT "COSINE A = c/b", 5, 110
10020 PLOT "TANGENT A = a/c", 5, 100
10030 SET BRUSH 14 : PLOT "SINE C = c/b", 5, 80
10040 PLOT "COSINE C = a/b", 5, 70
10050 PLOT "TANGENT C = c/a", 5, 60
10060 SET BRUSH 6 : PLOT "From the above it", 5, 40
10070 PLOT "can be seen that", 5, 30
10080 PLOT "SIN A = COS C", 5, 20
10090 PLOT "COS A = SIN C", 5, 10
10100 PLOT "TAN A = 1/TAN C", 5, 0
10110 SET BRUSH 15 : LINE 160, 210; 160, 0
10120 PLOT "A = 90 - C", 185, 190

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10130  PLOT "Worked example", 175, 170
10140  PLOT "If a = 34.5 cm and", 165, 150
10150  PLOT "c = 23.6 cm,", 165, 140
10160  PLOT "solve the triangle.", 165, 130
10170  PLOT "TAN A = a/c", 165, 120
10180  PLOT "TAN A = 34.5/23.6", 165, 110
10190  PLOT "TAN A = 1.462", 165, 100
10200  PLOT "ARCTAN 1.462 = A", 165, 90
10210  SET BRUSH 2 : PLOT "A = 55.63 degs", 175, 80
10220  SET BRUSH 15 : PLOT "C = 90 - 55.63", 175, 70
10230  SET BRUSH 2 : PLOT "C = 34.37 degs", 175, 60
10240  SET BRUSH 15 : PLOT "SIN A = a/b", 175, 50
10250  PLOT "b = a/SIN A", 175, 40
10260  PLOT "b = 34.5/0.825", 175, 30
10270  SET BRUSH 2 : PLOT "b = 41.80 cm", 175, 20
10280  FOR I := 1 TO 200 : NEXT I
10290  SET BRUSH 13 : PLOT "PRESS SPACE-BAR", 175, 10
10300  PLOT "TO CONTINUE", 195, 0
10310  Answer$ := GET$( )
10320  Alpha
10330  Beta
10340  Gamma
10350  Alphas
10360  Epsilon
10370  Phi
10380  ENDPROC
10390  PROCEDURE Alpha
10400  SET PAPER 1 : Triangle
10410  Total := 0 : Count := 0

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10420 SET WRITING 1 TO 1, 11; 40, 15
10430 SET WRITING 2 TO 1, 16; 40, 25
10440 LINE 0, 150; 319, 150
10450 SET WRITING 1 : SET PAPER 15
10460 SET WRITING 1 : CLS : SET WRITING 2 : CLS : SET PEN 6
10470 Opp := RND(100) + 20
10480 Hyp := Opp + RND(10) + 10
10490 PRINT 1 !, TAB (5); "If a =" ; Opp; "cm and b=" ; Hyp; " then"
10500 PRINT k2 !, TAB (5); "If a =" ; Opp; "cm and b =" ; Hyp; "cm then"
10510 PRINT 1; TAB (3); "calculate angle A."
10520 PRINT k2, TAB (3); "calculate angle A."
10530 SET CURPOS 0, 1 : PRINT 2 !, TAB (2); "Input your answer for angle A";
10540 PRINT k2 !, TAB (2); "Input your answer for angle A";
10550 SET WRITING 2 : INPUT Angle
10560 PRINT k2, Angle
10570 SET DEG TRUE
10580 X := Opp / Hyp
10590 Angle1 := ATN(X / SQR(1 - X * X + 1))
10600 IF ABS(Angle1 - Angle) < 1e-02 THEN SET BRUSH 1 : PLOT "CORRECT", 80, 10 SIZE 3 ELSE 10630
10610 IF ABS(Angle1 - Angle) < 1e-02 THEN PRINT k2, "CORRECT"
10620 FOR I := 1 TO 2000 : NEXT I : CLS 2 : IF ABS(Angle1 - Angle) < 1e-02 THEN 10710
10630 PRINT 2, TAB (2) "No! That is not right,try again"
10640 PRINT k2, TAB (2) "No! That is not right,try again"
10650 FOR I := 1 TO 1000 : NEXT I
10660 CLS 2
10670 Total := Total + 1
10680 IF Total < 3 THEN 10530
10690 GOSUB 10740
10700 GOTO 10400

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10710 Count := Count + 1
10720 IF Count < 4 THEN 10470
10730 GOTO 10830
10740 SET CURPOS 0, 1 : PRINT 2 ! TAB (1) "THIS IS THE CORRECT METHOD OF SOLUTION"
10750 PRINT h2 !, TAB (1) "THIS IS THE CORRECT METHOD OF SOLUTION"
10760 PRINT 2 !, TAB (7) "ANGLE A =ArcSin(a/b)"
10770 PRINT h2 !, TAB (7) "ANGLE A =ArcSin(a/b)"
10780 PRINT 2, TAB (2) "ArcSin("; Opp; "/" ; Hyp; ")="; Angle1; "deg"
10790 PRINT h2, TAB (2) "ArcSin("; Opp; "/" ; Hyp; ")="; Angle1; "deg"
10800 PRINT 2 !, TAB (6); "PRESS SPACE-BAR TO CONTINUE"
10810 Answer$ := GET$( )
10820 RETURN
10830 ENDPROC
10840 PROCEDURE Beta
10850 Triangle
10860 Total := 0 : Count := 0
10870 SET WRITING 1 TO 1, 11; 40, 15
10880 SET WRITING 2 TO 1, 16; 40, 25
10890 LINE 0, 150; 319, 150
10900 SET WRITING 1 : SET PAPER 15
10910 SET WRITING 1 : CLS : SET WRITING 2 : CLS : SET PEN 6
10920 Opp := RND(100) + 20
10930 Hyp := Opp + RND(10) + 10
10940 PRINT 1 !, TAB (5); "If a ="; Opp; "cm and b ="; Hyp; "cm then"
10950 PRINT h2 !, TAB (5); "If a ="; Opp; "cm and b ="; Hyp; "cm then"
10960 PRINT 1; TAB (3); "calculate angle C."
10970 PRINT h2, TAB (3); "calculate angle C."
10980 SET CURPOS 0, 1 : PRINT 2 !, TAB (2); "Input your answer for angle C";
10990 PRINT h2 !, TAB (2); "Input your answer for angle C";

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11000 SET WRITING 2 : INPUT Angle
11010 PRINT k2, Angle
11020 X := Opp / Hyp
11030 Angle1 := 90 - (ATN(X / SQR(1 - X * X + 1)))
11040 IF ABS(Angle1 - Angle) < 1e-02 THEN SET BRUSH 1 : PLOT "CORRECT", 80, 10 SIZE 3 ELSE 11070
11050 IF ABS(Angle1 - Angle) < 1e-02 THEN PRINT k2, "CORRECT"
11060 FOR I := 1 TO 2000 : NEXT I : CLS 2 : IF ABS(Angle1 - Angle) < 1e-02 THEN 11150
11070 PRINT 2, TAB (2) "No! That is not right,try again"
11080 PRINT k2, TAB (2) "No! That is not right,try again"
11090 FOR I := 1 TO 1000 : NEXT I
11100 CLS 2
11110 Total := Total + 1
11120 IF Total < 3 THEN 10980
11130 GOSUB 11180
11140 GOTO 10850
11150 Count := Count + 1
11160 IF Count < 4 THEN 10920
11170 GOTO 11270
11180 SET CURPOS 0, 1 : PRINT 2 : TAB (1) "THIS IS THE CORRECT METHOD OF SOLUTION"
11190 PRINT k2 !, TAB (1) "THIS IS THE CORRECT METHOD OF SOLUTION"
11200 PRINT 2 !, TAB (7) "ANGLE C =ArcCos(a/b)"
11210 PRINT k2 !, TAB (7) "ANGLE C =ArcCos(a/b)"
11220 PRINT 2, TAB (2) "ArcCos("; Opp; "/" ; Hyp; ")="; Angle1; "deg5"
11230 PRINT k2, TAB (2) "ArcCos("; Opp; "/" ; Hyp; ")="; Angle1; "deg5"
11240 PRINT 2 !, TAB (6); "PRESS SPACE-BAR TO CONTINUE"
11250 Answer$ := GET$(1)
11260 RETURN
11270 ENDPROC
11280 PROCEDURE Gamma

```

```

11290 Triangle
11300 Total := 0 : Count := 0
11310 SET WRITING 1 TO 1, 11; 40, 15
11320 SET WRITING 2 TO 1, 16; 40, 25
11330 LINE 0, 150; 319, 150
11340 SET WRITING 1 : SET PAPER 15
11350 SET WRITING 1 : CLS : SET WRITING 2 : CLS : SET PEN 6
11360 Opp := RND(100) + 20
11370 Adj := RND(100) + 10
11380 PRINT 1 !, TAB (5); "If a ="; Opp; "cm and c ="; Adj; "cm then"
11390 PRINT k2 !, TAB (5); "If a ="; Opp; "cm and c ="; Adj; "cm then"
11400 PRINT 1; TAB (3); "calculate angle A."
11410 PRINT k2, TAB (3); "calculate angle A."
11420 SET CURPOS 0, 1 : PRINT 2 !, TAB (2); "Input your answer for angle A";
11430 PRINT k2 !, TAB (2); "Input your answer for angle A";
11440 SET WRITING 2 : INPUT Angle
11450 PRINT k2, Angle
11460 X := Opp / Adj
11470 Angle1 := ATN(X)
11480 IF ABS(Angle1 - Angle) < 1e-02 THEN SET BRUSH 1 : PLOT "CORRECT", 80, 10 SIZE 3 ELSE 11510
11490 IF ABS(Angle1 - Angle) < 1e-02 THEN PRINT k2, "CORRECT"
11500 FOR I := 1 TO 2000 : NEXT I : CLS 2 : IF ABS(Angle1 - Angle) < 1e-02 THEN 11590
11510 PRINT 2, TAB (2) "No! That is not right,try again"
11520 PRINT k2, TAB (2) "No! That is not right,try again"
11530 FOR I := 1 TO 1000 : NEXT I
11540 CLS 2
11550 Total := Total + 1
11560 IF Total < 3 THEN 11420
11570 GOSUB 11620

```

```

11580 GOTO 11290

11590 Count := Count + 1

11600 IF Count < 4 THEN 11350

11610 GOTO 11710

11620 SET CURPOS 0, 1 : PRINT 2 ! TAB (1) "THIS IS THE CORRECT METHOD OF SOLUTION"

11630 PRINT A2 !, TAB (1) "THIS IS THE CORRECT METHOD OF SOLUTION"

11640 PRINT 2 !, TAB (7) "ANGLE A =ArcTan(a/c)"

11650 PRINT A2 !, TAB (7) "ANGLE A =ArcTan(a/c)"

11660 PRINT 2, TAB (2) "ArcTan("; Opp; "/" ; Adj; ")="; Angle1; "degS"

11670 PRINT A2, TAB (2) "ArcTan("; Opp; "/" ; Adj; ")="; Angle1; "degS"

11680 PRINT 2 !, TAB (6); "PRESS SPACE-BAR TO CONTINUE"

11690 Answer$ := GET$( )

11700 RETURN

11710 ENDPROC

11720 PROCEDURE Alpha1

11730 Triangle

11740 Total := 0 : Count := 0

11750 SET WRITING 1 TO 1, 11; 40, 15

11760 SET WRITING 2 TO 1, 16; 40, 25

11770 LINE 0, 150; 319, 150

11780 SET WRITING 1 : SET PAPER 15

11790 SET WRITING 1 : CLS : SET WRITING 2 : CLS : SET PEN 6

11800 Opp := RND(100) + 20

11810 Angle := INT(RND(1) * 90) + 1

11820 PRINT 1 !, TAB (4); "If a =" ; Opp; "cm and A=" ; Angle; "degrees then"

11830 PRINT A2 !; TAB (4); "If a =" ; Opp; "cm and A=" ; Angle; "degrees then"

11840 PRINT 1; TAB (3); "calculate side b."

11850 PRINT A2; TAB (3); "calculate side b."

11860 SET CURPOS 0, 1 : PRINT 2 !, TAB (2); "Input your answer for side b";

```

```

11870 PRINT A2 !, TAB (2); "Input your answer for side b";
11880 SET WRITING 2 : INPUT B
11890 PRINT A2, B
11900 SET DEG TRUE
11910 Sideb := Opp / SIN(Angle)
11920 IF ABS(Sideb - B) < 1e-02 THEN SET BRUSH 1 : PLOT "CORRECT", 80, 10 SIZE 3 ELSE 11950
11930 IF ABS(Sideb - B) < 1e-02 THEN PRINT A2, "CORRECT"
11940 FOR I := 1 TO 2000 : NEXT I : CLS 2 : IF ABS(Sideb - B) < 1e-02 THEN 12030
11950 PRINT 2, TAB (2) "No! That is not right,try again"
11960 PRINT A2, TAB (2) "No! That is not right,try again"
11970 FOR I := 1 TO 1000 : NEXT I
11980 CLS 2
11990 Total := Total + 1
12000 IF Total < 3 THEN 11860
12010 GOSUB 12060
12020 GOTO 11730
12030 Count := Count + 1
12040 IF Count < 4 THEN 11800
12050 GOTO 12150
12060 SET CURPOS 0, 1 : PRINT 2 ! TAB (1) "THIS IS THE CORRECT METHOD OF SOLUTION"
12070 PRINT A2 !, TAB (1) "THIS IS THE CORRECT METHOD OF SOLUTION"
12080 PRINT 2 !, TAB (7) "Side b = a/SinA"
12090 PRINT A2 !, TAB (7) "Side b = a/SinA"
12100 PRINT 2, TAB (2) "b ="; Opp; " / Sin"; Angle; " = "; Sideb; "cm"
12110 PRINT A2, TAB (2) "b ="; Opp; " / Sin"; Angle; " = "; Sideb
12120 PRINT 2 !, TAB (6); "PRESS SPACE-BAR TO CONTINUE"
12130 Answer$ := GET$(1)
12140 RETURN
12150 ENDPROC

```

```

12160 PROCEDURE Epsilon
12170   Triangle
12180   Total := 0 : Count := 0
12190   SET WRITING 1 TO 1, 11; 40, 15
12200   SET WRITING 2 TO 1, 16; 40, 25
12210   LINE 0, 150; 319, 150
12220   SET WRITING 1 : SET PAPER 15
12230   SET WRITING 1 : CLS : SET WRITING 2 : CLS : SET PEN 6
12240   Adj := RND(100) + 20
12250   Angle := INT(RND(1) * 80) + 1
12260   PRINT 1 !, TAB (4); "If c ="; Adj; "cm and A="; Angle; "degrees then"
12270   PRINT #2 !; TAB (4); "If c ="; Adj; "cm and A="; Angle; "degrees then"
12280   PRINT 1; TAB (3); "calculate side b."
12290   PRINT #2; TAB (3); "calculate side b."
12300   SET CURPOS 0, 1 : PRINT 2 !, TAB (2); "Input your answer for side b";
12310   PRINT #2 !, TAB (2); "Input your answer for side b";
12320   SET WRITING 2 : INPUT B
12330   PRINT #2, B
12340   SET DEG TRUE
12350   Sideb := Adj / COS(Angle)
12360   IF ABS(Sideb - B) < 1e-02 THEN SET BRUSH 1 : PLOT "CORRECT", 80, 10 SIZE 3 ELSE 12390
12370   IF ABS(Sideb - B) < 1e-02 THEN PRINT #2, "CORRECT"
12380   FOR I := 1 TO 2000 : NEXT I : CLS 2 : IF ABS(Sideb - B) < 1e-02 THEN 12470
12390   PRINT 2, TAB (2) "No! That is not right,try again"
12400   PRINT #2, TAB (2) "No! That is not right,try again"
12410   FOR I := 1 TO 1000 : NEXT I
12420   CLS 2
12430   Total := Total + 1
12440   IF Total < 3 THEN 12300

```

```

12450 GOSUB 12500

12460 GOTO 12170

12470 Count := Count + 1

12480 IF Count < 4 THEN 12240

12490 GOTO 12590

12500 SET CURPOS 0, 1 : PRINT 2 ! TAB (1) "THIS IS THE CORRECT METHOD OF SOLUTION"

12510 PRINT h2 !, TAB (1) "THIS IS THE CORRECT METHOD OF SOLUTION"

12520 PRINT 2 !, TAB (7) "Side b = c/CosA"

12530 PRINT h2 !, TAB (7) "Side b = c/CosA"

12540 PRINT 2, TAB (2) "b =" ; Adj ; " / Cos" ; Angle ; " = " ; Sideb ; "cm"

12550 PRINT h2, TAB (2) "b =" ; Adj ; " / Cos" ; Angle ; " = " ; Sideb

12560 PRINT 2 !, TAB (6) ; "PRESS SPACE-BAR TO CONTINUE"

12570 Answer$ := GET$( )

12580 RETURN

12590 ENDPROC

12600 PROCEDURE Phi

12610 Triangle

12620 Total := 0 : Count := 0

12630 SET WRITING 1 TO 1, 11; 40, 15

12640 SET WRITING 2 TO 1, 16; 40, 25

12650 LINE 0, 150; 319, 150

12660 SET WRITING 1 : SET PAPER 15

12670 SET WRITING 1 : CLS : SET WRITING 2 : CLS : SET PEN 6

12680 Opp := RND(100) + 20

12690 Angle := INT(RND(1) * 80) + 1

12700 PRINT 1 !, TAB (4) ; "If c =" ; Opp ; "cm and C=" ; Angle ; "degrees then"

12710 PRINT h2 !, TAB (4) ; "If c =" ; Opp ; "cm and C=" ; Angle ; "degrees then"

12720 PRINT 1; TAB (3) ; "calculate side a."

12730 PRINT h2; TAB (3) ; "calculate side a."

```

```

12740 SET CURPOS 0, 1 : PRINT 2 !, TAB (2); "Input your answer for side a";
12750 PRINT h2 !, TAB (2); "Input your answer for side a";
12760 SET WRITING 2 : INPUT A
12770 PRINT h2, A
12780 SET DEG TRUE
12790 Sidea := Opp / TAN(Angle)
12800 IF ABS(Sidea - A) < 1e-02 THEN SET BRUSH 1 : PLOT "CORRECT", 80, 10 SIZE 3 ELSE 12830
12810 IF ABS(Sidea - A) < 1e-02 THEN PRINT h2, "CORRECT"
12820 FOR I := 1 TO 2000 : NEXT I : CLS 2 : IF ABS(Sidea - A) < 1e-02 THEN 12910
12830 PRINT 2, TAB (2) "No! That is not right,try again"
12840 PRINT h2, TAB (2) "No! That is not right,try again"
12850 FOR I := 1 TO 1000 : NEXT I
12860 CLS 2
12870 Total := Total + 1
12880 IF Total < 3 THEN 12740
12890 GOSUB 12940
12900 GOTO 12610
12910 Count := Count + 1
12920 IF Count < 4 THEN 12680
12930 GOTO 13030
12940 SET CURPOS 0, 1 : PRINT 2 ! TAB (1) "THIS IS THE CORRECT METHOD OF SOLUTION"
12950 PRINT h2 !, TAB (1) "THIS IS THE CORRECT METHOD OF SOLUTION"
12960 PRINT 2 !, TAB (7) "Side a = c/TanC"
12970 PRINT h2 !, TAB (7) "Side a = c/TanC"
12980 PRINT 2, TAB (2) "a ="; Opp; " / tan"; Angle; " = "; Sidea; "cm"
12990 PRINT h2, TAB (2) "a ="; Opp; " / tan"; Angle; " = "; Sidea
13000 PRINT 2 !, TAB (6); "PRESS SPACE-BAR TO CONTINUE"
13010 Answer$ := GET$(1)
13020 RETURN

```


13030 SET WRITING 0

13040 ENDPROC

13050 PROCEDURE Triangle

13060 SET PAPER 1 : SET BORDER 10 : CLG

13070 SET BRUSH 15 : AREA 10, 170; 100, 230; 100, 170 STYLE 3

13080 LINE 90, 170; 90, 180; 100, 180

13090 PLOT "A", 5, 160 : PLOT "B", 105, 160 : PLOT "C", 105, 230

13100 SET BRUSH 10 : PLOT "a", 105, 195 : PLOT "b", 45, 205 : PLOT "c", 50, 160

13110 PLOT "Solve the problem.", 155, 195

13120 ENDPROC

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APPENDIX

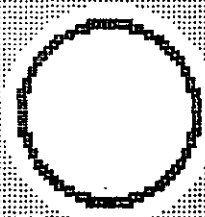
SCREEN DUMPS OF SOME OF THE DIAGRAMS AND GRAPHICS.

LOUGHBOROUGH UNIVERSITY OF TECHNOLOGY
M.Sc. COMPUTER EDUCATION
(C) R.E.FORD
CENTRE FOR ADVANCEMENT OF MATHEMATICAL
EDUCATION IN TECHNOLOGY

B/TEC MATHEMATICS
F & N LEVEL
FOR ENGINEERING
STUDENTS

A COMPUTER-AIDED
LEARNING PACKAGE

CANET



Hello,

Welcome to a mathematics revision session. You will be asked to select the topic of mathematics that you would like to revise, and as you work your way through the exercises an output to the printer will be created. If you are working on a NIMBUS NETWORK system then at the end of your session press ctrl/alt/prtsc keys simultaneously so that you can obtain your own individual printout with your name on it for easy recognition. Please tell me your name and I hope you find the revision session stimulating. Go for it!

What is your name ?

MENU
ENGINEERING MATHEMATICS

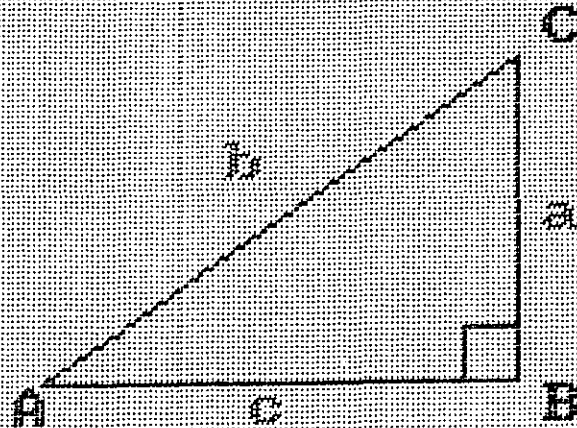
- | | | | |
|---|--------------------------------|-----|-------|
| 1 | TRI GONOMETRY | F | LEVEL |
| | | | |
| 2 | GRAPHS | F&H | LEVEL |
| | | | |
| 3 | 3 DIMENSIONAL
TRI GONOMETRY | F&H | LEVEL |
| | | | |
| 4 | PROPERTIES OF
THE CIRCLE | F | LEVEL |
| | | | |
| 5 | END SESSION | | |

SELECT THE NUMBER
OF YOUR CHOICE

**TRI GONDOMETRY
LEVEL**

INTRODUCTION TO TRIGONOMETRY

THE RIGHT-ANGLED TRIANGLE



$$\begin{aligned}\text{SINE } A &= a/b \\ \text{COSINE } A &= c/b \\ \text{TANGENT } A &= a/c\end{aligned}$$

$$\begin{aligned}\text{SINE } C &= c/b \\ \text{COSINE } C &= a/b \\ \text{TANGENT } C &= c/a\end{aligned}$$

From the above it
can be seen that
 $\text{SIN } A = \text{COS } C$
 $\text{COS } A = \text{SIN } C$

$$A = 90 - C$$

Worked example

If $a = 34.5$ cm and
 $c = 23.6$ cm,
solve the triangle.

$$\begin{aligned}\text{TAN } A &= a/c \\ \text{TAN } A &= 34.5/23.6 \\ \text{TAN } A &= 1.462\end{aligned}$$

$$\text{ARCTAN } 1.462 = A$$

$$A = 55.63 \text{ degs}$$

$$C = 90 - 55.63$$

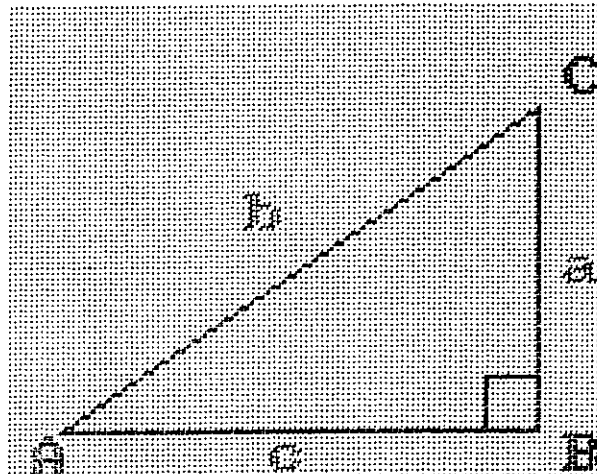
$$C = 34.37 \text{ degs}$$

$$\text{SIN } A = a/b$$

$$b = a/\text{SIN } A$$

$$b = 34.5/0.825$$

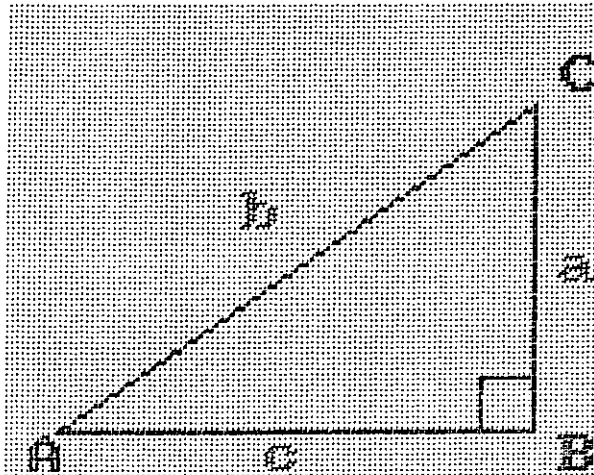
$$b = 41.80 \text{ cm}$$



Solve the problem.

If $a = 104$ cm and $b = 123$ then
calculate angle A.

Input your answer for angle A?_



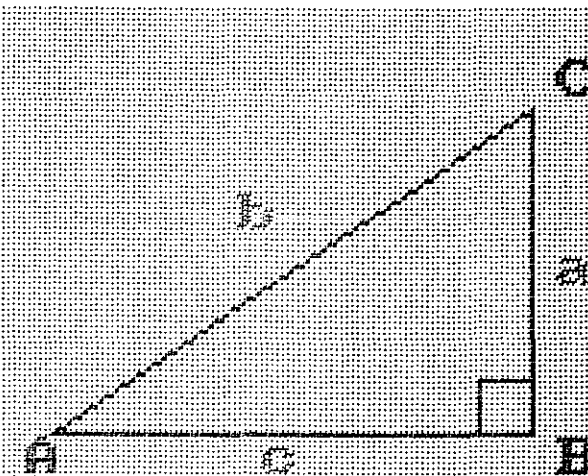
Solve the problem.

If $a = 104$ cm and $b = 123$ then
calculate angle A.

THIS IS THE CORRECT METHOD OF SOLUTION

$$\begin{aligned}\text{ANGLE A} &= \text{ArcSin}(a/b) \\ \text{ArcSin}(104 / 123) &= 57.72861 \text{ degs}\end{aligned}$$

PRESS SPACE-BAR TO CONTINUE



Solve the problem.

If $a = 24$ cm and $b = 39$ then
calculate angle A.

Input your answer for angle A? 37.979

CORRECT

GRAPHIS
F & N LEVEL

GRAPHS

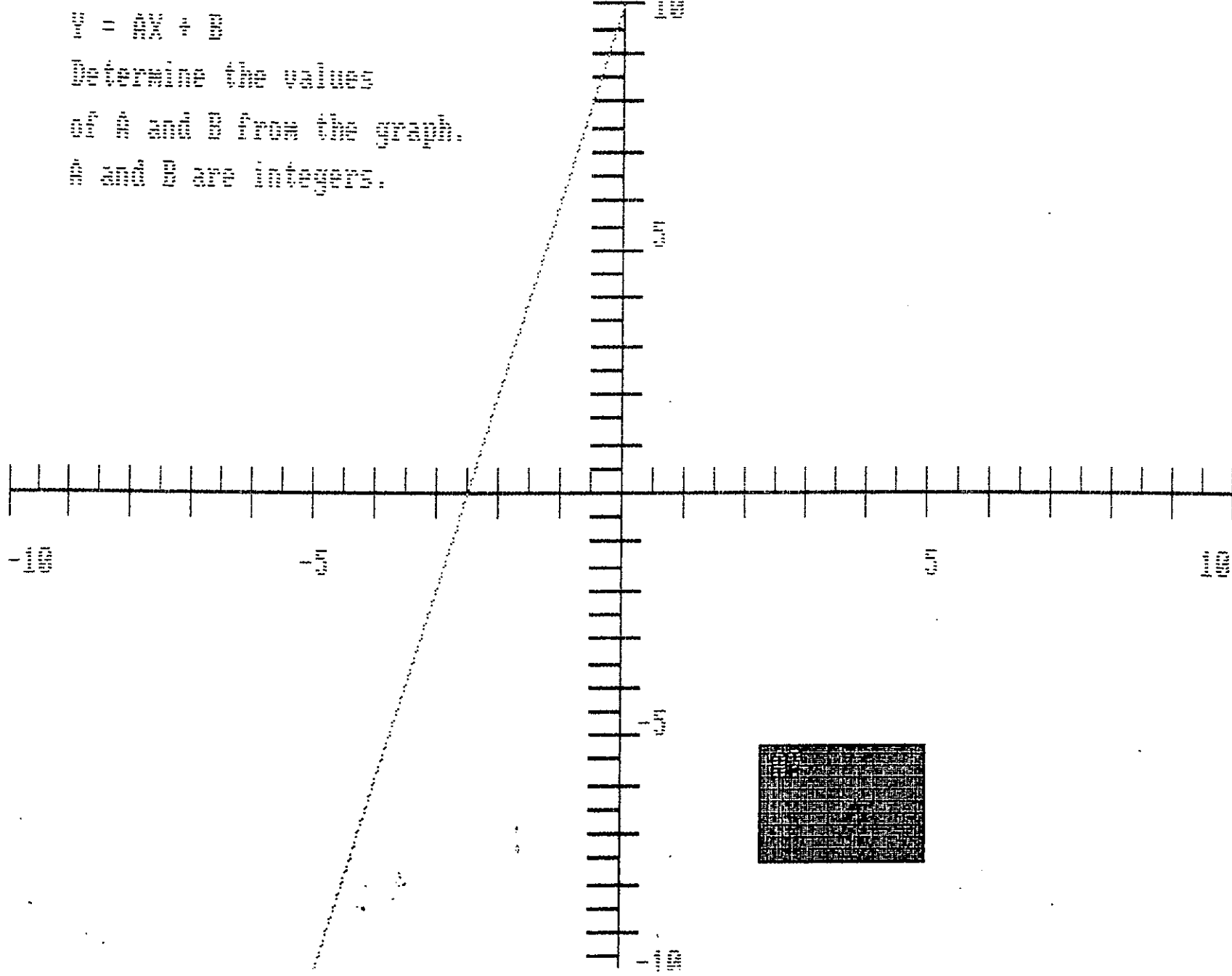
(1) STRAIGHT LINE GRAPHS: $Y = AX+B$

(2) QUADRATIC GRAPHS: $Y=AX^2+BX+C$

CHOOSE A NUMBER AND PRESS ENTER KEY.

YOU WILL NEED A CALCULATOR.

21



100 = 100% of 100

100 of 100 = 100% of 100

100 of 100 = 100% of 100

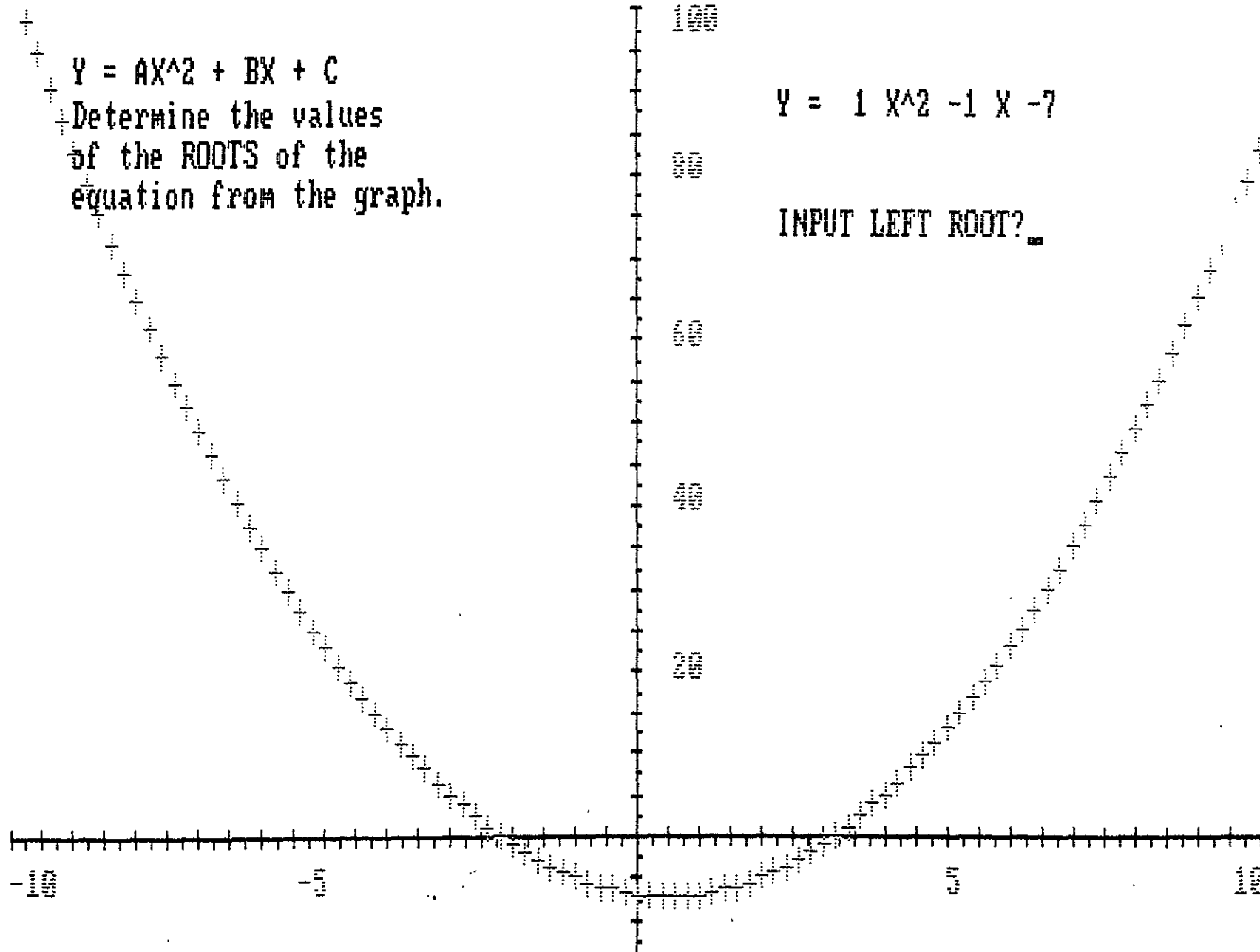
100 of 100 = 100% of 100

$$Y = AX^2 + BX + C$$

Determine the values
of the ROOTS of the
equation from the graph.

$$Y = 1 X^2 - 1 X - 7$$

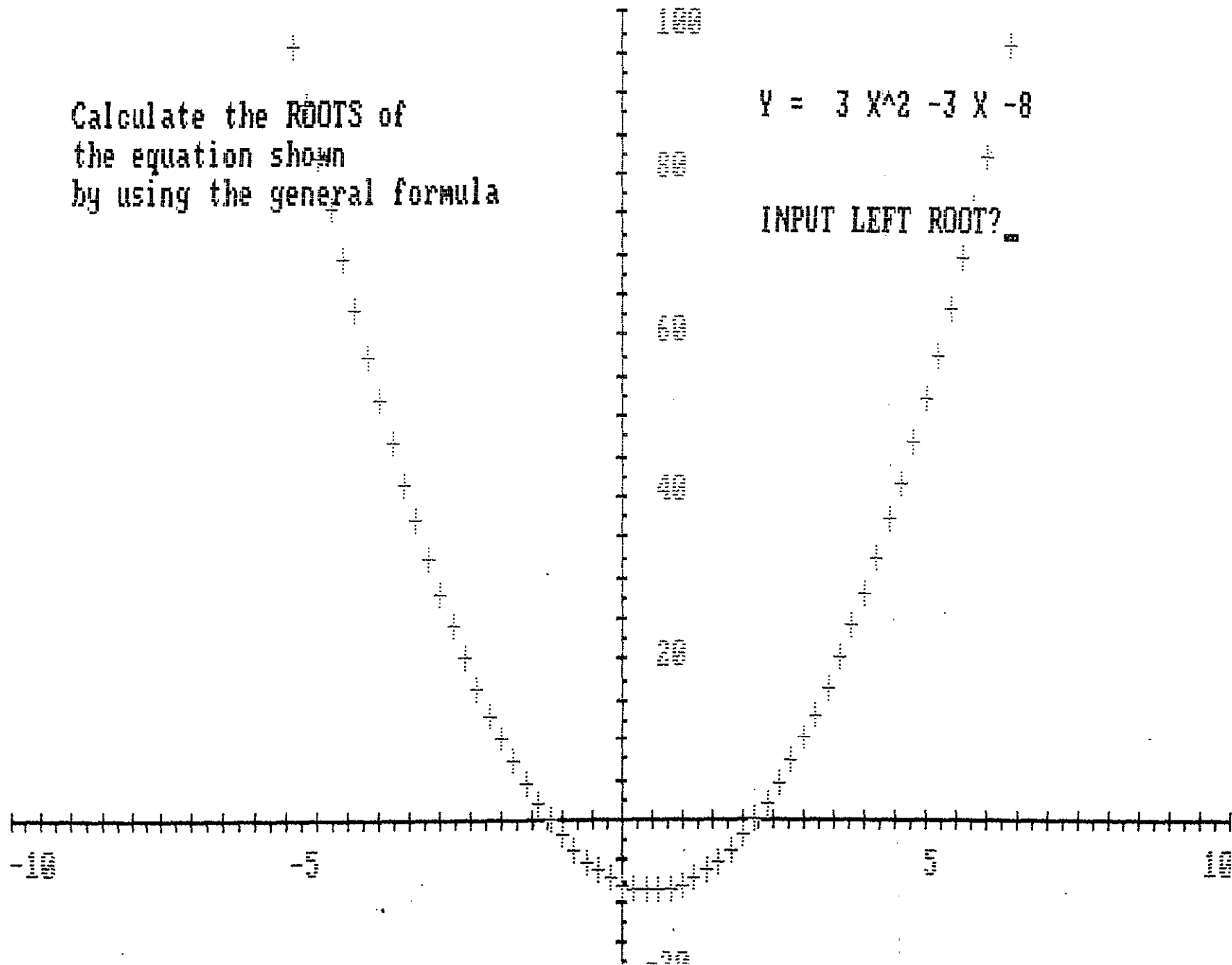
INPUT LEFT ROOT?



Calculate the ROOTS of
the equation shown
by using the general formula

$$Y = 3 X^2 - 3 X - 8$$

INPUT LEFT ROOT?



**3-DIMENSIONAL
TRIGONOMETRY**

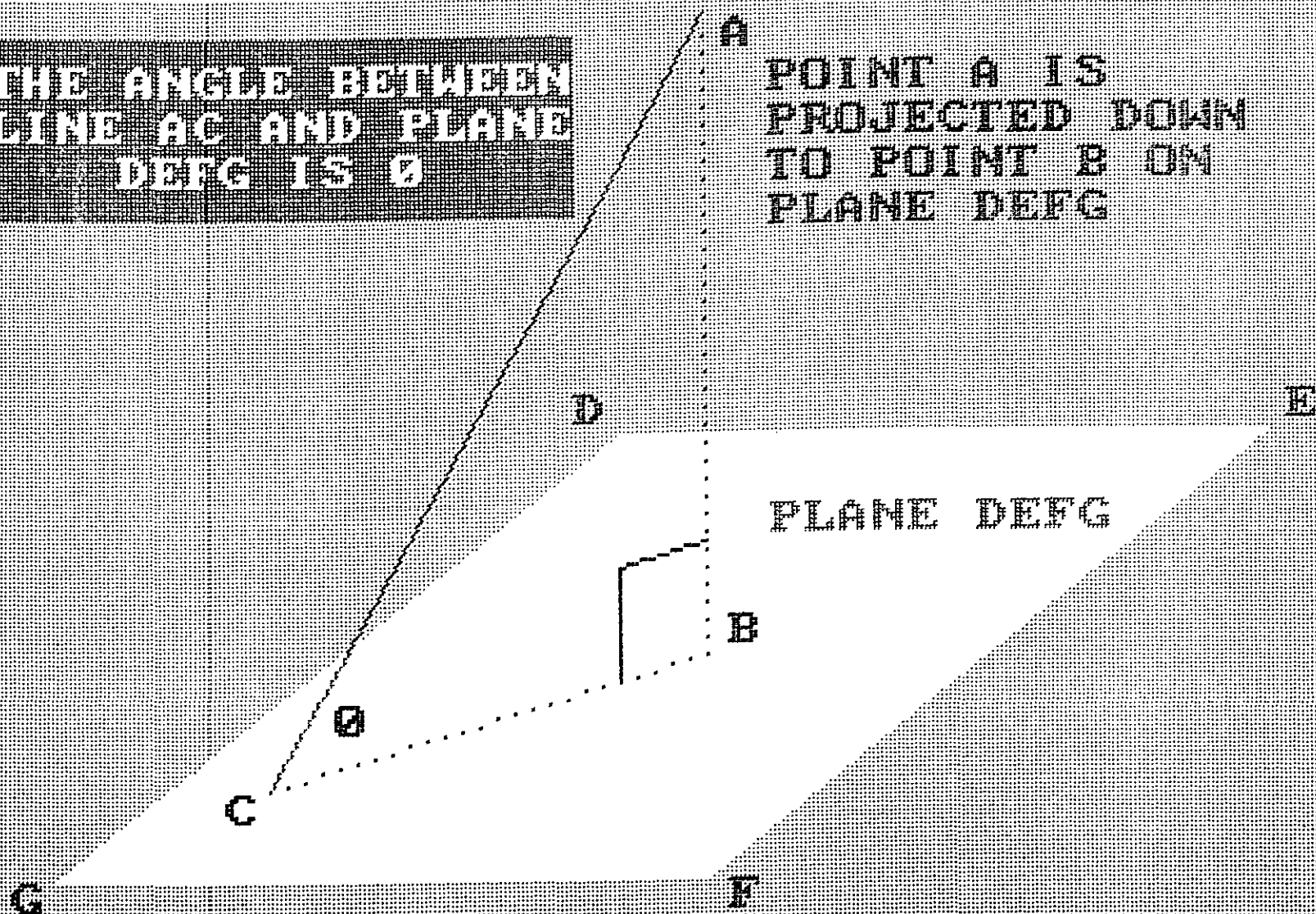
F & N LEVEL

This set of exercises is to help you understand some applications of ENGINEERING TRIGONOMETRY. The computer will create questions for you to answer. You will need a CALCULATOR. The diagrams are for revision purposes.

PRESS ANY KEY TO CONTINUE

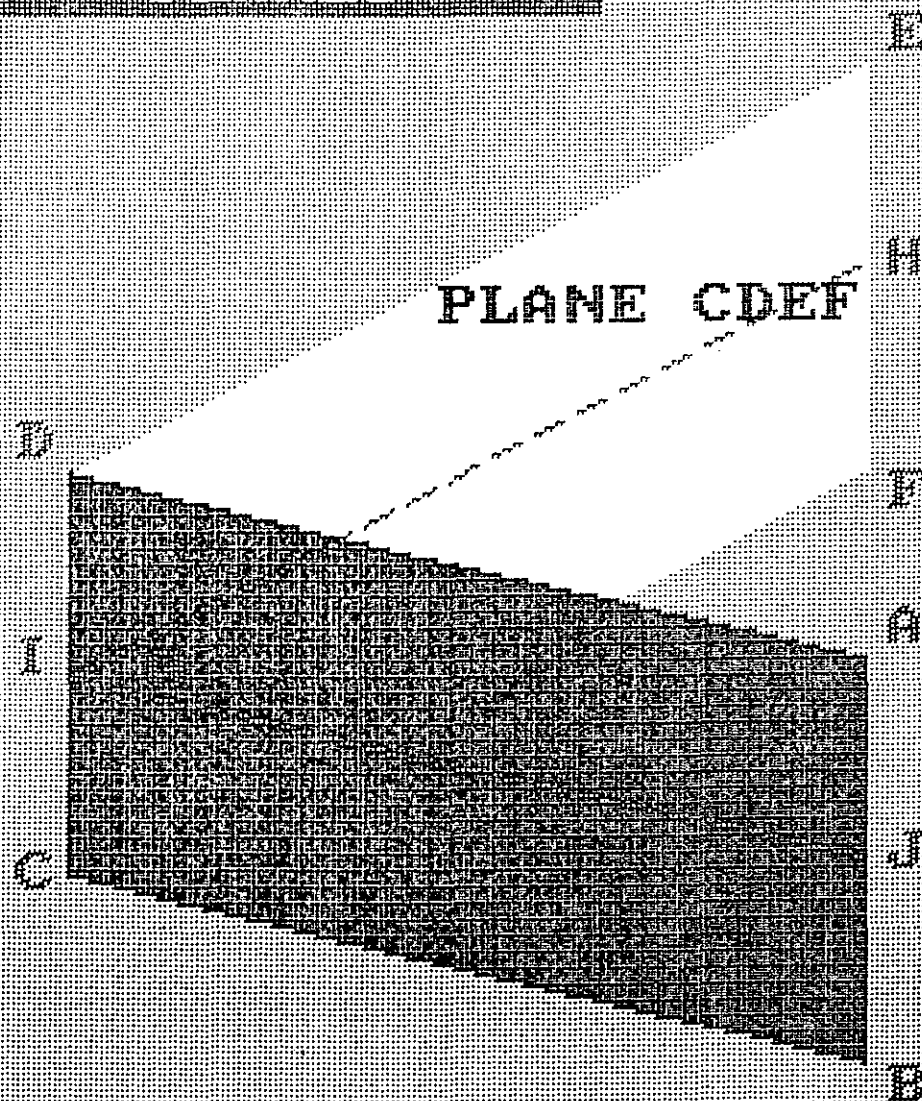
THE ANGLE BETWEEN
LINE AC AND PLANE
DEFG IS 0

POINT A IS
PROJECTED DOWN
TO POINT B ON
PLANE DEFG



PRESS ANY KEY TO CONTINUE

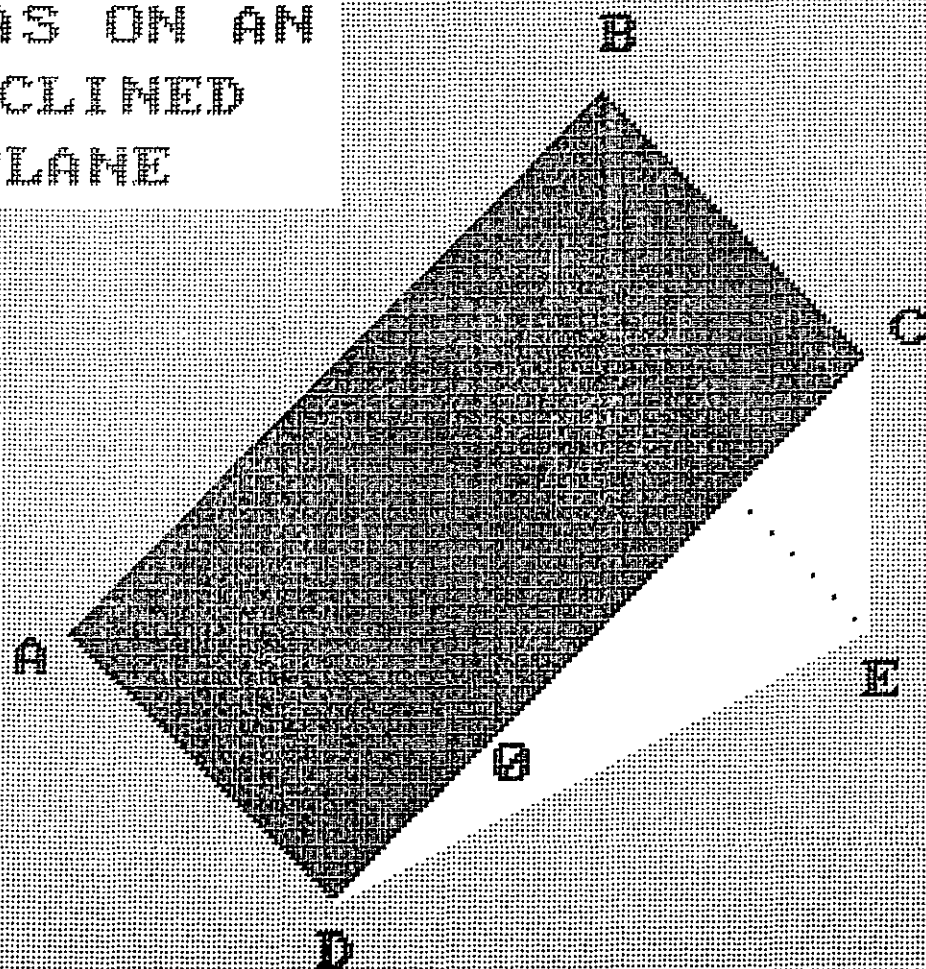
THE ANGLE BETWEEN
TWO INTERSECTING
PLANES



THE ANGLE
BETWEEN THE
TWO PLANES
IS ANGLE HIJ
SHOWN AS E

PRESS ANY KEY
TO CONTINUE

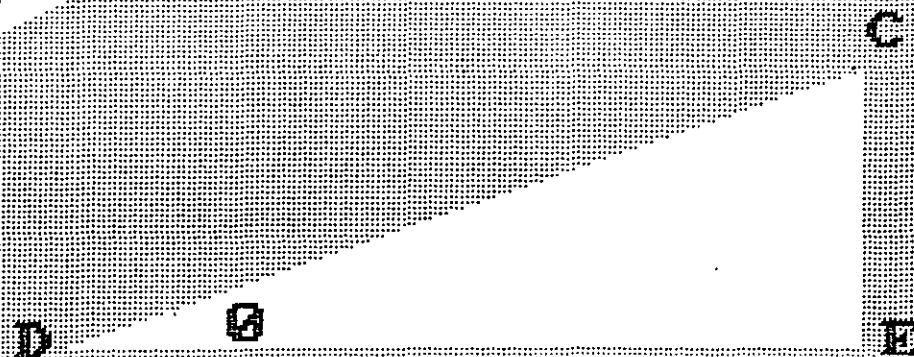
LENGTHS AND
AREAS ON AN
INCLINED
PLANE



$$\cos \theta = \frac{DE}{DC}$$

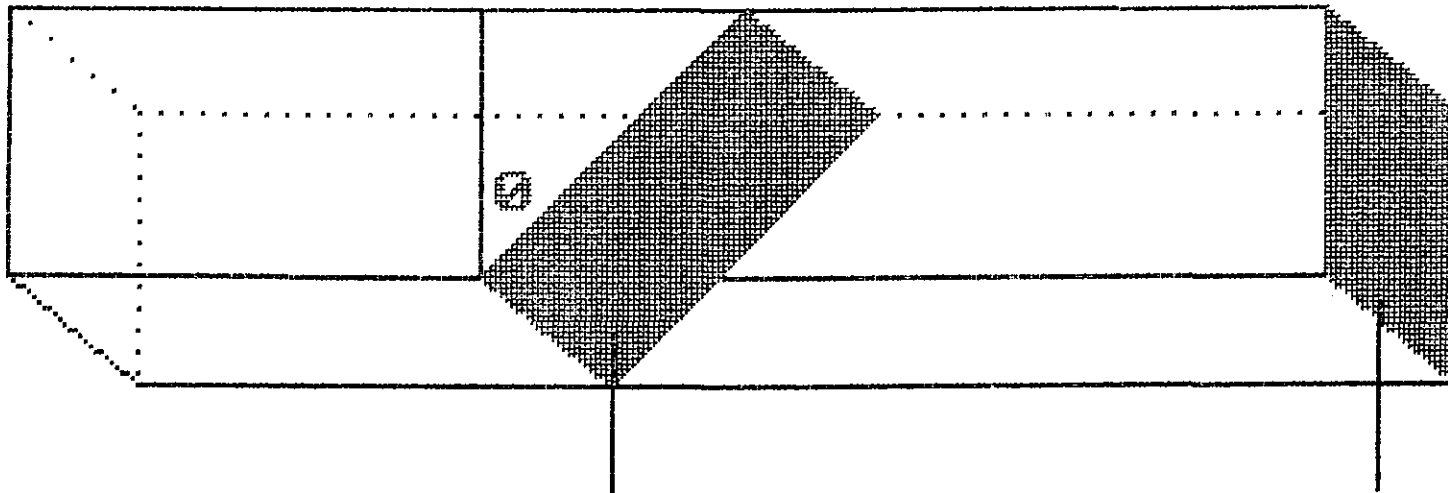
$$ABCD = \frac{AD \cdot DE}{\cos \theta}$$

PRESS ANY KEY
TO CONTINUE



THE OBLIQUE AREA OF A PRISM

$$\text{OBLIQUE AREA} = \frac{\text{CROSS-SECTIONAL AREA}}{\cos \theta}$$



OBLIQUE AREA. CROSS-SECT AREA.

PRESS ANY KEY TO CONTINUE

EXAMPLE
=====

CYLINDRICAL PRISM
=====

OBLIQUE AREA = $\text{PI} \times \text{RAD}^2 / \text{COS A}$

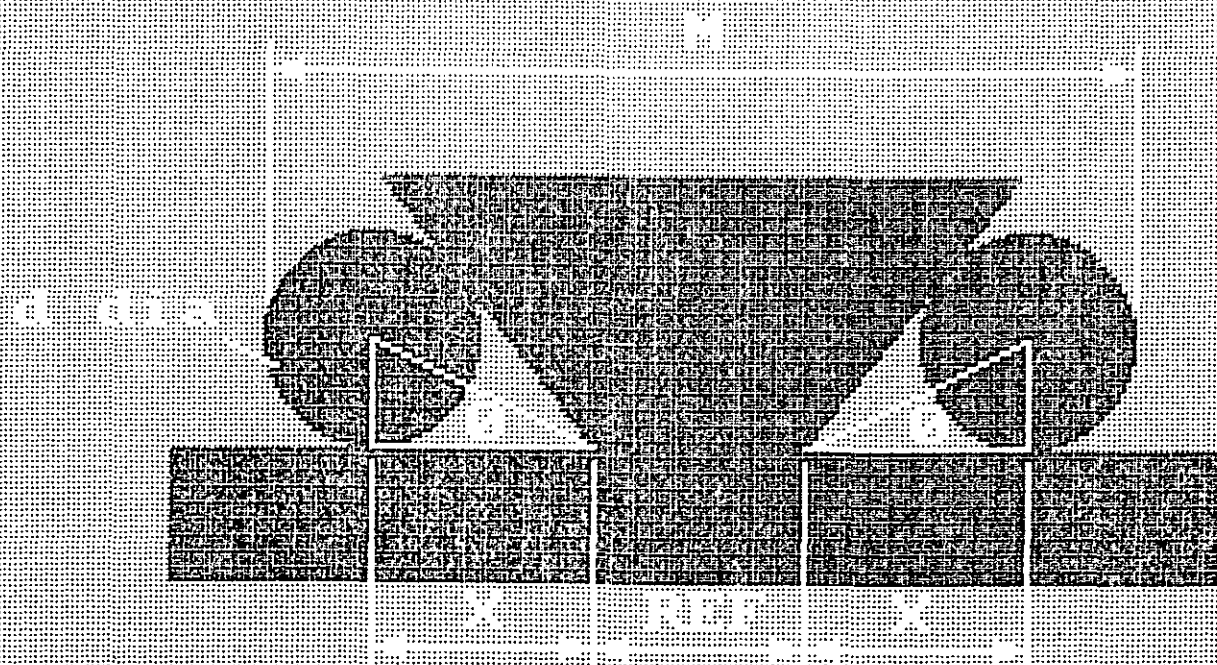
IF THE RADIUS IS = 84 MM
AND THE ANGLE IS = 39 DEGS

THEN CALCULATE THE OBLIQUE AREA

INPUT YOUR ANSWER ?28523.699

CORRECT

MEASUREMENT OF EXTERNAL DOVETAILED BY THE USE OF PRECISION ROLLERS



$$REF = M - 2(d/2 + X)$$

$$\tan A = d/2X : 2X = d/\tan A : 2X = d \cdot \cot A$$

$$REF = M - d(1 + \cot A)$$

PRESS ANY KEY TO CONTINUE

EXAMPLES

=====

$$REF = M - d(1 + \cot \alpha)$$

IF THE READING M IS 161 mm,

THE DIAMETER, $d=25$ mm

AND THE ANGLE, $\alpha=30$ deg

THEN CALCULATE THE VALUE OF REF

INPUT YOUR ANSWER 732.698

CORRECT

$$REF = M - d(1 + \cotan A)$$

IF THE READING M IS 123 mm,

THE DIAMETER, $d=25$ mm

AND THE ANGLE, $A=30$ deg

THEN CALCULATE THE VALUE OF REF

INPUT YOUR ANSWER?2

NO! That is NOT right, try again

INPUT YOUR ANSWER?2

NO! That is NOT right, try again

INPUT YOUR ANSWER?2

NO! That is NOT right, try again

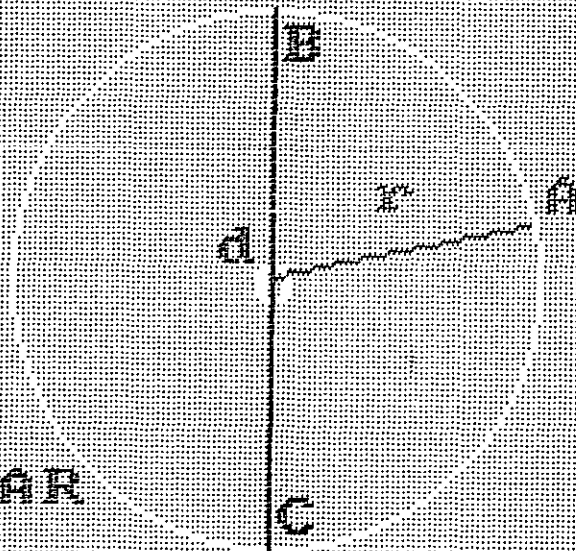
THIS IS THE CORRECT METHOD OF SOLUTION

$$REF = M - d(1 + \cotan A)$$

$$123 - 25(1 + \cotan 30) = 54.69873 \text{ mm}$$

**TERMINOLOGY
AND PROPERTIES OF
THE CIRCLE
OF TRUTH**

TERMINOLOGY & PROPERTIES OF THE CIRCLE

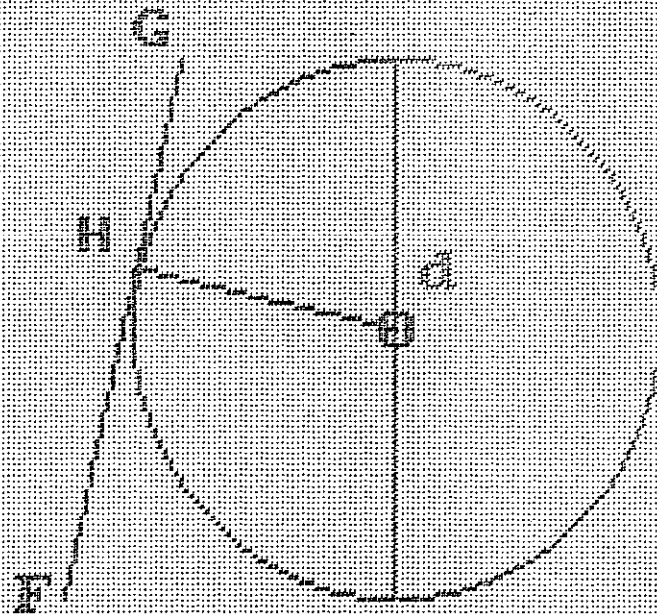


PRESS SPACE-BAR
TO CONTINUE

A circle is a plane figure enclosed by a curved line, every point on which is equidistant from a point within called the CENTRE. O is the centre of the circle.

The distance from the centre to the curve, OA, is called the RADIUS, r , of the circle.

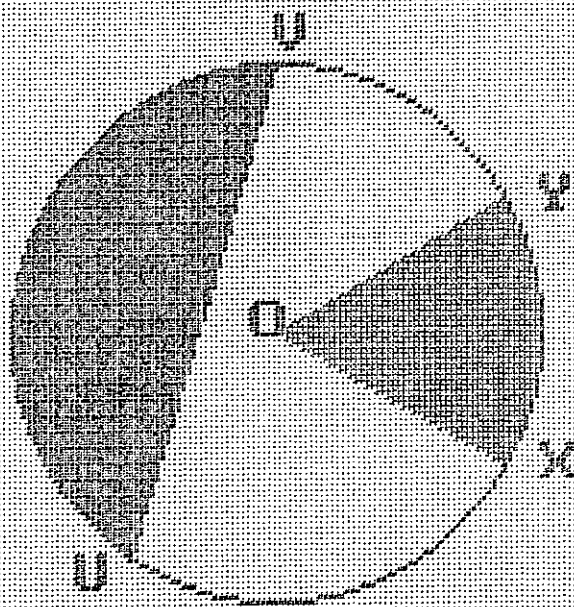
Any straight line passing through the centre and touching the circumference at each end as BC does is called the DIAMETER, d . The diameter is twice the length of the radius. $d=2r$.



The boundary of a circle, that is the perimeter, is called the CIRCUMFERENCE, $c.c/d$ is equal to the constant π . $\pi=3.142$ to three decimal places.

A TANGENT to a circle is a straight line which meets the circle at one point, H. FG is a Tangent to the circle. If radius OH is drawn then FHO is a RIGHT-ANGLE.

PRESS SPACE-BAR TO CONTINUE.



The shaded portion OXY is called a SECTOR.

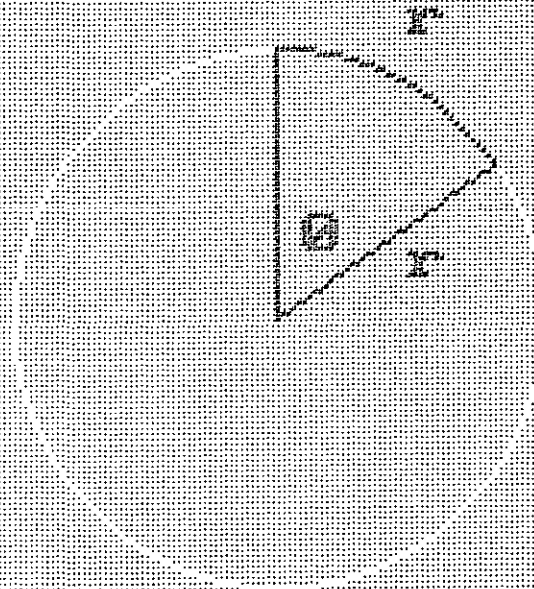
If the sector is less than a semi-circle it is a MINOR SECTOR. If larger than a semi-circle it is a MAJOR SECTOR.

The line UU is a CHORD.

The shaded portion UU is a SEGMENT.

The shortest distance between U and U along the circumference is called the MINOR ARC. The remaining part of the circumference is the MAJOR ARC.

PRESS THE SPACE BAR TO CONTINUE.

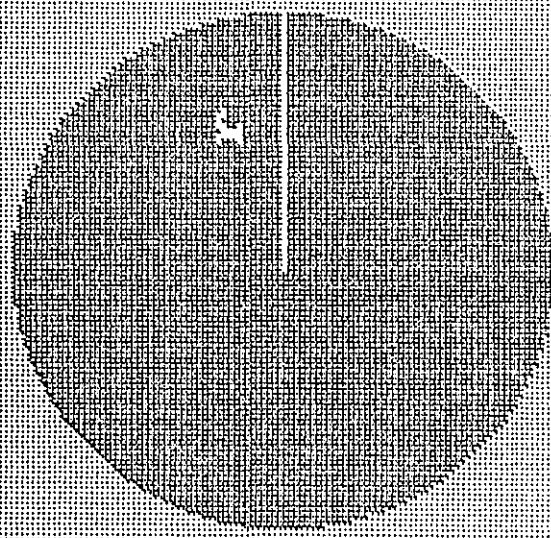


An angle can be measured in DEGREES or RADIANS. A RADIAN is defined as the angle formed at the centre of a circle by an ARC equal in length to the RADIUS.

$$\theta = 1 \text{ radian} = 57.3 \text{ deg.}$$

$$2\pi \text{ radians} = 360 \text{ degs.}$$

PRESS SPACE BAR TO CONTINUE



THE HISTORY OF THE

WARRIORS

OF THE

WARRIORS

The disc accompanying this Thesis is held with the archive copy in the cage on Level 2. Please enquire in the Information Office on Level 3 if you wish to borrow it.

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